

# Generating Graph Snapshots from Streaming Edge Data

Sucheta Soundarajan\*   Acar Tamersoy†   Elias B. Khalil†   Tina Eliassi-Rad‡  
Duen Horng Chau†   Brian Gallagher§   Kevin Roundy‡

\*Syracuse University   †Georgia Institute of Technology   ‡Rutgers University  
§Lawrence Livermore National Laboratory   ‡Symantec Inc.

\*susounda@syracuse.edu   †{tamersoy, lyes, polo}@gatech.edu  
‡eliassi@cs.rutgers.edu   §bgallagher@llnl.gov   ‡kevin\_roundy@symantec.com

## ABSTRACT

We study the problem of determining the proper aggregation granularity for a stream of time-stamped edges. Such streams are used to build time-evolving networks, which are subsequently used to study topics such as network growth. Currently, aggregation lengths are chosen arbitrarily, based on intuition or convenience. We describe ADAGE, which detects the appropriate aggregation intervals from streaming edges and outputs a sequence of structurally mature graphs. We demonstrate the value of ADAGE in automatically finding the appropriate aggregation intervals on edge streams for belief propagation to detect malicious files and machines.

## General Terms

Algorithms, Design, Performance, Experimentation.

## Keywords

Aggregating edge streams, time-evolving networks.

## 1. INTRODUCTION

We address the problem of determining proper intervals for aggregating a stream of time-stamped edges into a sequence of structurally mature networks. We define a structurally mature network as one that has stabilized with respect to a network statistic, such as the exponent of the degree distribution. Current literature in time-evolving networks<sup>1</sup> frequently selects an arbitrary fixed-length aggregation interval (e.g., one day). This approach has three shortcomings. (1) If the interval is too short, the graph may lack sufficient structure for analysis (e.g., consider running belief propagation on a set of disconnected edges). (2) If the interval is too long, fine-grained changes get lost. (3) If the data streams at a variable rate, a fixed-length interval may not be appropriate. To address these issues, we introduce ADAGE,

<sup>1</sup>We use the terms graph and network interchangeably.

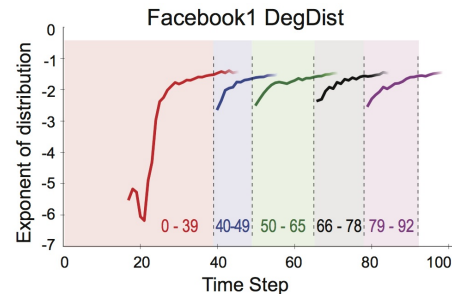


Figure 1: Dashed lines depict intervals found by ADAGE, using degree distribution exponent, on Facebook wall-postings. Each time step is one hour.

the Adaptable Graph Edge Interval Method, which automatically identifies variable-length aggregation intervals, each giving rise to a structurally mature graph. We report results on an edge stream from Symantec, for the task of malicious file/machine detection via belief propagation.

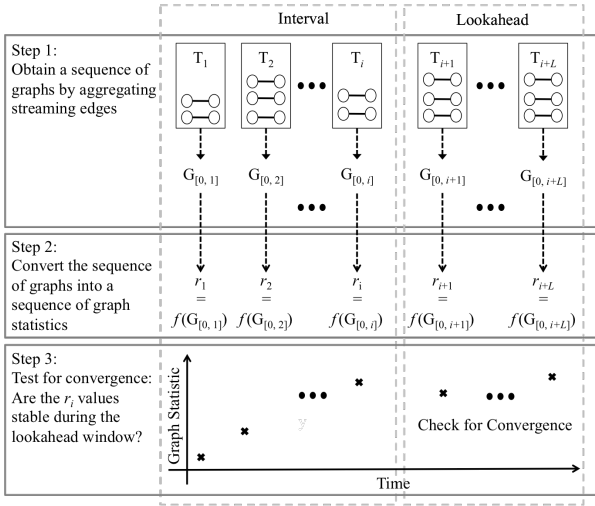
## 2. RELATED WORK

The literature on partitioning a data stream is vast. For example, Kiernan et al. [3] identify disjoint summaries of an event stream. Keogh et al. [2] present a solution for time series segmentation. The DAPPER algorithm [1] partitions a timeline of streaming network data into disjoint interval snapshots by examining edge persistence for change-points. Unlike ADAGE, DAPPER finds locations where the streaming data suddenly changes, as opposed to structurally mature snapshots, and requires the entire timeline upfront.

## 3. PROPOSED METHOD: ADAGE

ADAGE is an online method for aggregating streaming edges into a sequence of structurally mature networks. Given a network statistic (e.g., exponent of the degree distribution), ADAGE aggregates streaming edges into a network until the value of the statistic converges. Figure 1 depicts the time intervals detected by ADAGE on Facebook wall-postings vs. the exponent of the degree distribution of the composed graphs. In this graph, an edge represents that a user posted on another user's wall. Each time step is an hour. 40 hours worth of data were required to compose a graph with a stable degree distribution exponent. 10 hours were needed to generate the next structurally mature graph.

ADAGE takes as input a sequence of edge sets  $E_1, E_2, \dots$  arriving at times  $T_1, T_2, \dots$ , and a function  $f(G)$ , which out-



**Figure 2: ADAGE Overview: Edges are aggregated until convergence is detected on the chosen statistic.**

puts the value of a specified statistic on graph  $G$ . At each time  $T_i$ ,  $f$  is applied to the current aggregated graph  $G_i$  to obtain value  $r_i$ . These values are inspected for convergence.

ADAGE can take any network statistic, such as exponent of degree distribution, number of nodes in the largest connected component, etc. The choice of statistic depends on the nature of phenomenon under study. For example, the exponent of the degree distribution is a good statistic if the phenomenon is expected to exhibit the Pareto principle.

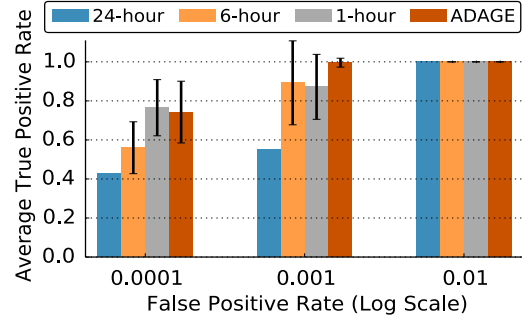
Figure 2 provides an overview of ADAGE, which begins at time  $T_1$  and aggregates data until the statistic converges. To determine whether convergence has occurred at time  $T_i$ , ADAGE examines the value  $r_i$  and the set of values  $\{r_{i+1}, \dots, r_k\}$  seen during the lookahead window  $[T_{i+1}, T_{i+L}]$ . The length  $L$  of the lookahead window is calculated using a parameter  $b$ , where  $L = b \times i$  ( $L$  depends on the length of the interval so far).<sup>2</sup> The allowed deviation in values  $r_i, \dots, r_k$  is controlled by threshold parameter  $c$ : the difference between the largest and smallest values cannot exceed threshold  $t$ , which is equal to  $c$  times the smallest value (assuming all values are positive).<sup>3,4</sup> Once convergence is detected, ADAGE outputs the graph and restarts the aggregation process.

To avoid computing the statistic on every snapshot, ADAGE uses a binary search to choose which values to compare. Suppose ADAGE is considering time  $T_i$ , and so examines values  $r_i, \dots, r_k$ . The allowed deviation of the statistic among these values is represented by the threshold  $t = c \times \min(\{r_i, \dots, r_k\})$  (where  $c$  is the threshold parameter.) Let  $T_j$  be the midpoint between  $T_i$  and  $T_k$ . ADAGE calculates an estimate  $\hat{t}$  on  $t$ , where  $\hat{t}$  is equal to  $c \times \min(\{r_i, r_j, r_k\})$ . If  $\max(\{r_i, r_j, r_k\}) - \min(\{r_i, r_j, r_k\}) \leq \hat{t}$ , then ADAGE calculates all intermediate values  $r_i, \dots, r_k$  to check for convergence. Otherwise,  $\max(\{r_i, r_j, r_k\}) - \min(\{r_i, r_j, r_k\}) > \hat{t}$  and ADAGE cannot possibly have converged at time  $T_i$ . In this case, ADAGE recalculates a new estimate on  $t$  as follows. If  $|r_j - r_k| >$

<sup>2</sup>To avoid detecting convergence after very short intervals, we set the window length to be at least 10.

<sup>3</sup>We assume values are all positive or all negative.

<sup>4</sup>A parameter study suggested setting  $b, c = 0.1$ . Automatically selecting these parameters is part of our future work.



**Figure 3: Detecting malicious files/machines via belief propagation on Symantec edge streams. ADAGE intervals have the best performance.**

$c \times \min(\{r_j, r_k\})$ , then convergence is not possible at any time between  $T_i$  and  $T_j$ ; thus values  $r_{i+1}, \dots, r_{j-1}$  are not calculated. This process is repeated by looking at the midpoint value between  $r_j$  and  $r_k$ , and so on. In this way, ADAGE finds the earliest time when convergence might occur.

## 4. EVALUATION AND DISCUSSION

Evaluation of ADAGE is challenging, as we lack a ground truth. Here, we evaluate ADAGE on the task of detecting malicious files and machines via belief propagation. (Data provided by Symantec.) The dataset consists of an edge stream of file  $i$  resides on machine  $j$ .<sup>5</sup> We have a total of 3M edges connecting 0.6M nodes. Some files or machines are known to be malicious, and we use belief propagation to predict which others are likely to be malicious. We choose the exponent of the degree distribution as the statistic used by ADAGE, because we assume that mature file  $\times$  machine graphs have power-law degree distributions. Figure 3 shows 10-fold cross-validation results of various aggregation methods. ADAGE automatically finds intervals that match or outperform fixed-length intervals. ADAGE took on average 4.19 seconds to detect each interval, each with  $\approx 0.5M$  edges.

By detecting convergence of a statistic of interest, ADAGE automatically identifies the proper aggregation granularity on streams of edges. Our future work includes being able to