



Seoul, Korea

WWW 2014

The 23<sup>rd</sup> International World Wide Web Conference

April 7-11, 2014 coex

# Trust in Social Computing

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<http://www.public.asu.edu/~jtang20/tTrust.htm>

April 7, 2014



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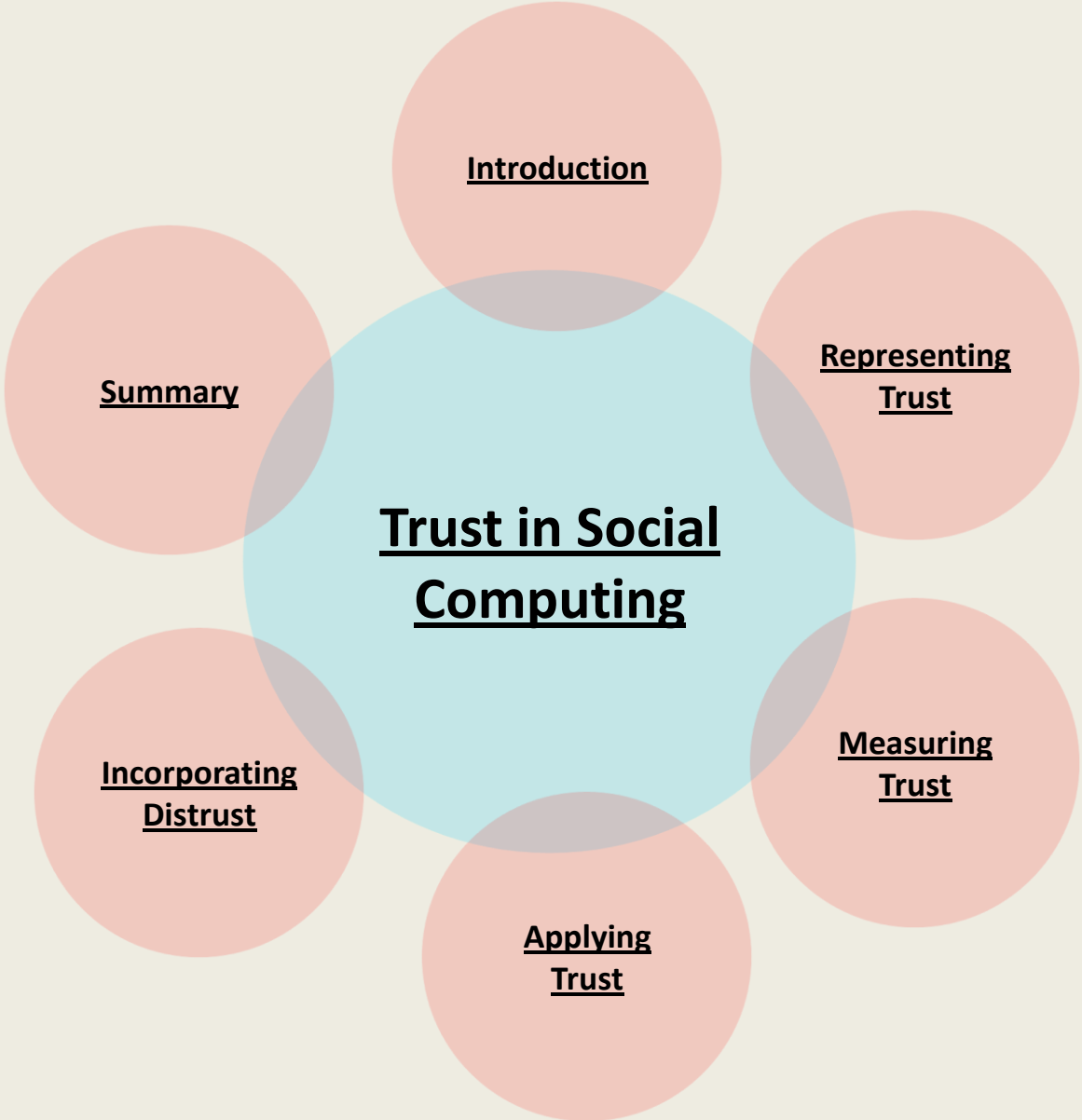
# Trust in Social Media

Jiliang Tang  
Huan Liu

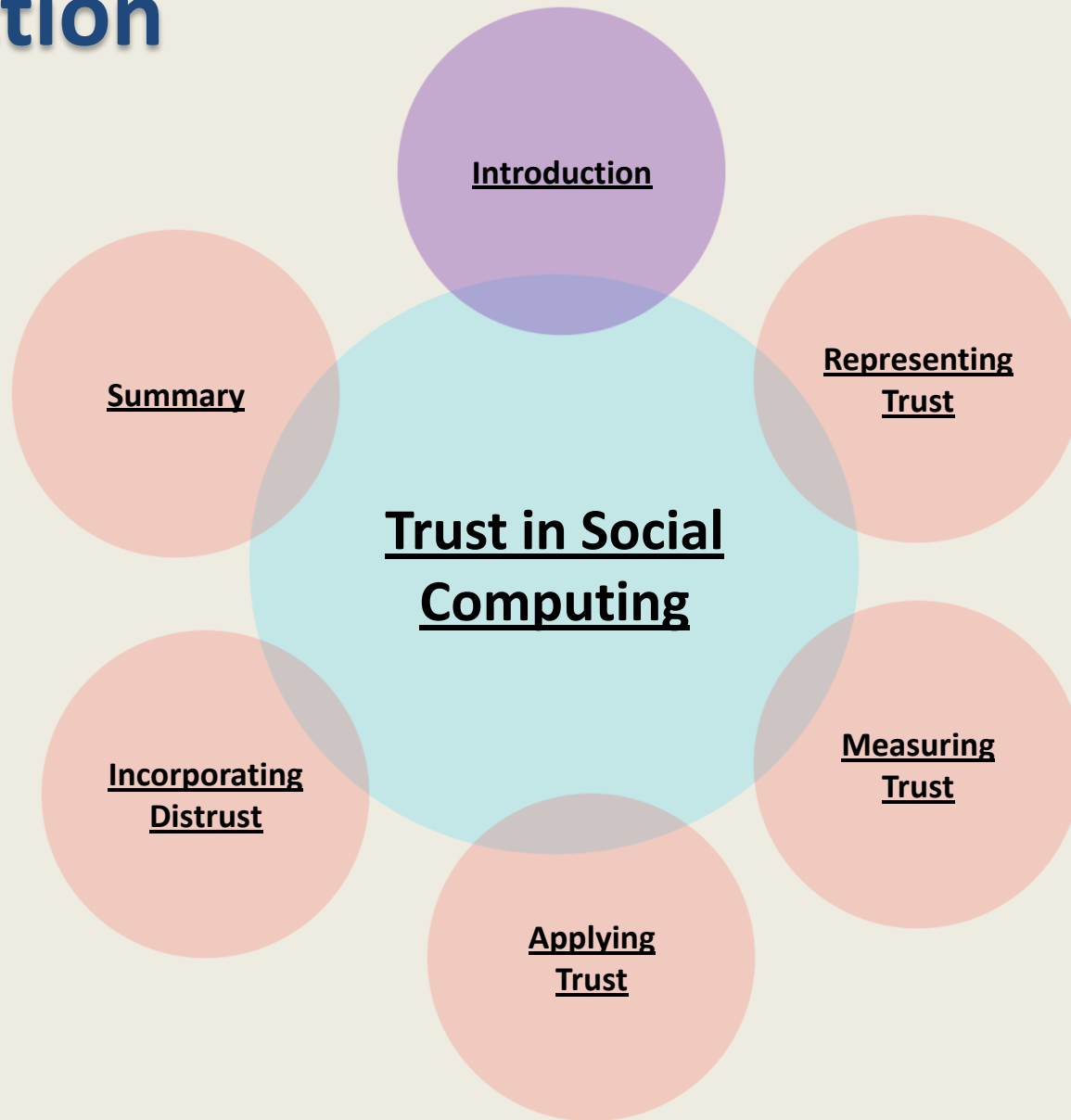
*SYNTHESIS LECTURES ON  
INFORMATION SECURITY, PRIVACY, AND TRUST*

Elisa Bertino & Ravi Sandhu, *Series Editors*

# Outline



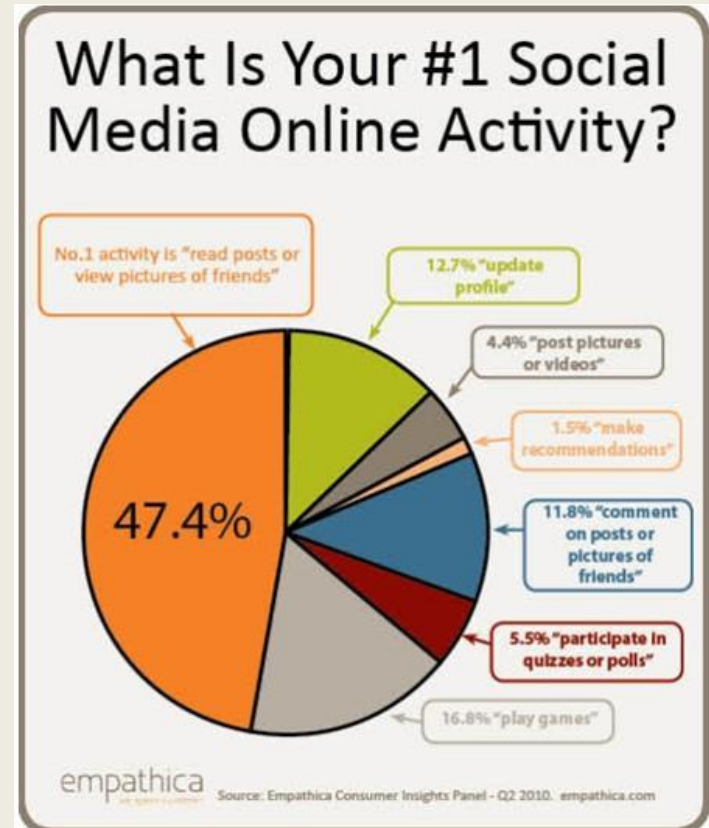
# Introduction





# Social Media

- Social media greatly enables people to participate in online activities
  - Networking, tagging and commenting
- It shatters the barrier for online users to create and share information in any place at any time



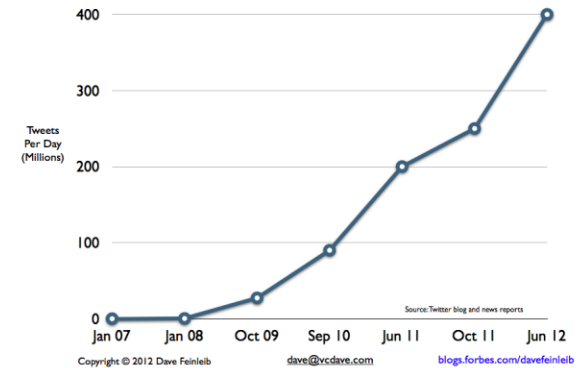
<http://www.marketingprofs.com/charts/2010/4101/social-media-brand-followers-hunting-for-deals>

# Information Overload

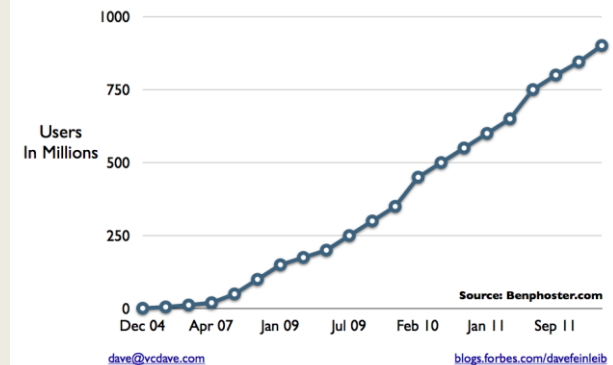
- User generated content increases at an unprecedented rate
  - Given the big-data problem, how can we find relevant content?

- Anyone can publish content in social media
  - With so many grass-roots authors, from whom I should collect information useful to me

Twitter: Tweets Per Day



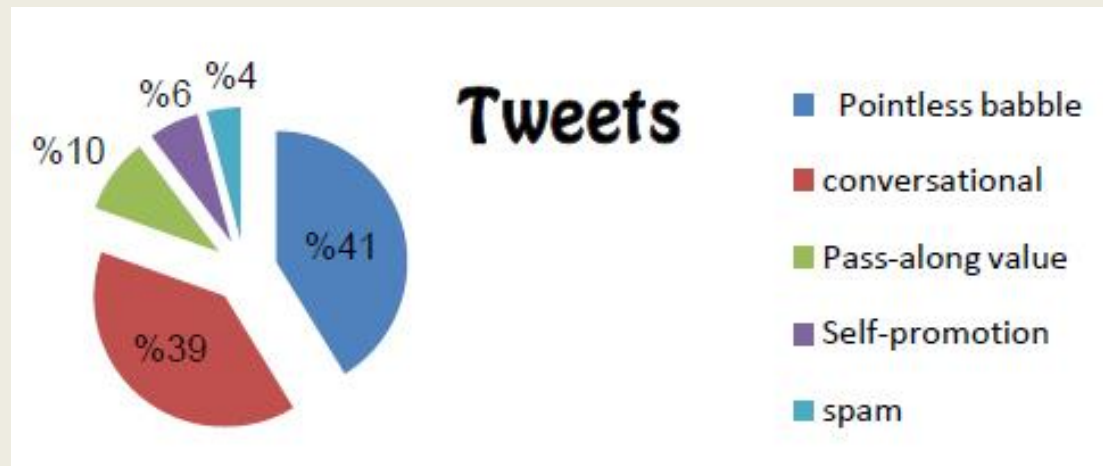
Facebook User Growth



<http://www.forbes.com/sites/davefeinleib/2012/07/09/the-3-is-of-big-data/>

# Information Credibility

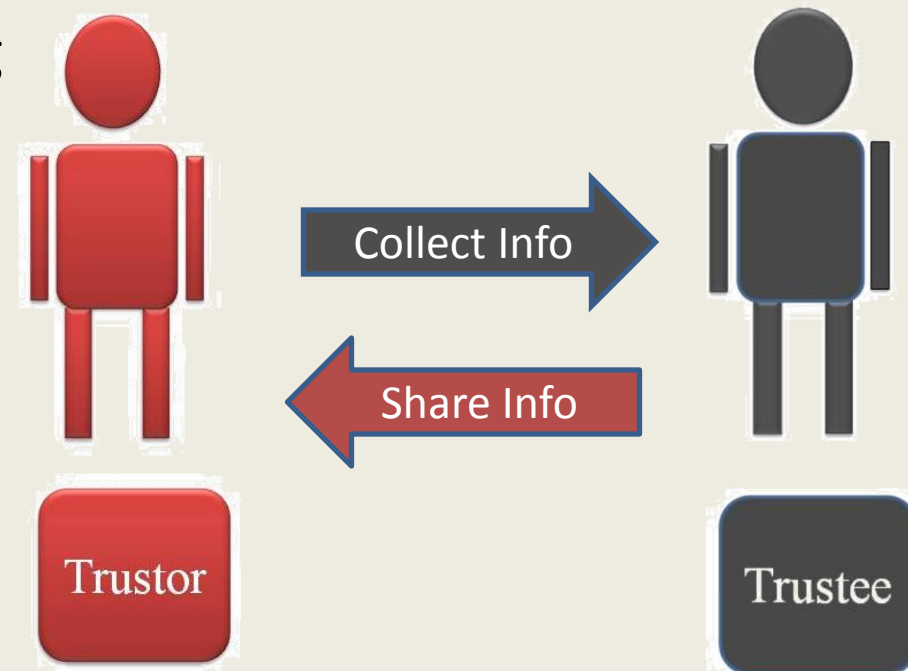
- The quality of user generated content varies widely
  - From excellent content to abuse and spam
  - How to find reliable information fast
- Anyone may access my content
  - With whom should I share information?



<https://infomagnet.wordpress.com/2012/05/04/a-comparison-among-the-top-3-social-networks/>

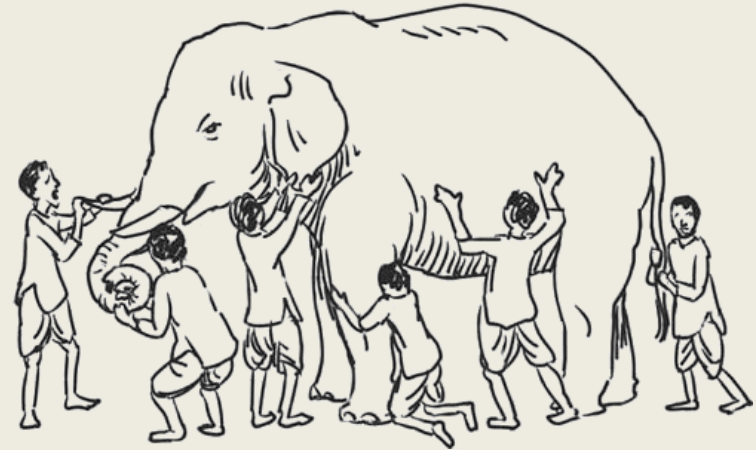
# Trust in Social Media

- Trust provides information to find answers like
  - From whom we should collect information
  - With whom we should share information
- It offers a mental shortcut for direct information seeking
  - Without being overwhelmed by excessive information, thus mitigating information overload
  - With credible information due to the trust placed on the information provider, or increasing information credibility



# Trust – A Hard to Define Concept [McKnight et al. 2001]

- Trust is a very broad and complex concept
  - Multidisciplinary
  - More than 60 definitions in the literature
- Each discipline has its own perspective of trust
  - Personality in Psychology
  - Social structures in Sociology
  - Rational choice in Economics



- Let's first look at what happens in social media before we settle on a definition

# Online Trust Systems [Massa, 2007]

- E-marketplaces
  - Selling and buying items



- Opinion and activity sharing sites
  - Sharing opinions



- Business/job networking sites
  - Sharing job skills



- Social/entertainment sites
  - Networking and sharing UGC



- News sites (e.g., Slashdot)
  - Posting news and stories



- There are two types of users - sellers and buyers
- Buyers assess the trustworthiness of sellers according to the reliability of the services or products they provide

**zyderstores** (69★)  
97.1% positive feedback

+ Follow

Based in United States, zyde

**Feedback ratings** ⓘ

★★★★★	33	Item as described	+ 34	3	1
★★★★★	30	Communication	Positive	Neutral	Negative
★★★★★	32	Shipping time			
★★★★★	37	Shipping charges			

Feedback from the last 12 months

<http://www.ebay.com/usr/zyderstores>



- There are two roles of users in Epinions – reviewers (who write reviews) and raters (who rate the helpfulness of reviews)
- Raters add a reviewer into their trust circle if they think her reviews are helpful

### Web of Trust

**jankp trusts:**

1. TheSmartTraveler
2. mizsallyforth
3. majenta
4. merle\_levy
5. thewisefool

▶ View all 598 members whom **jankp trusts**

---

**jankp is trusted by:**

1. kirbylee
2. HawgWyld
3. barryergang
4. rajaahmed
5. MamaMiaEtc

▶ View all 530 members who **trust jankp**

### jankp's Profile

**About jankp**

**TOP REVIEWER** in Music, Movies, Books

**POPULAR AUTHOR** - Top 100

Member: **Jan Peregrine**

Epinions.com ID: **jankp**

Google Profile: **Jan Peregrine**

Location: **Lincoln, NE**

Member Since: **Dec 17, 1999**

Homepage: **Getting To Know Jan...**

Favorite Websites: [Climate Change W-O](#)  
[Graphic Novel Bust-Out](#)  
[Artistic Inspiration W-O](#)

Published From [Out\\_of\\_the\\_Desert](#); on amazon.com now!  
[more](#)

<http://www.epinions.com/user-jankp>



- Advogato is a community site of free software developers
- Developers share their developing skills and raters will rate them with three trust levels – Master, Journeyer and Apprentice

Others have certified badvogato as follows:

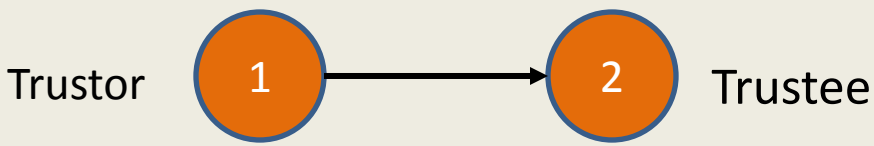
- [dragotown](#) certified badvogato as Master
- [beto](#) certified badvogato as Master
- [esteve](#) certified badvogato as Journeyer
- [aerry13](#) certified badvogato as Master
- [dmitri](#) certified badvogato as Master
- [michaelemma](#) certified badvogato as Journeyer
- [sashako](#) certified badvogato as Journeyer
- [Tofu](#) certified badvogato as Apprentice
- [sulaiman](#) certified badvogato as Journeyer
- [ekashp](#) certified badvogato as Journeyer
- [hereticmessiah](#) certified badvogato as Master
- [pencechp](#) certified badvogato as Journeyer
- [wardv](#) certified badvogato as Journeyer
- [nixnut](#) certified badvogato as Master
- [garym](#) certified badvogato as Master
- [nikole](#) certified badvogato as Master
- [mirwin](#) certified badvogato as Master
- [mglazer](#) certified badvogato as Journeyer

<http://www.advogato.org/person/badvogato/>

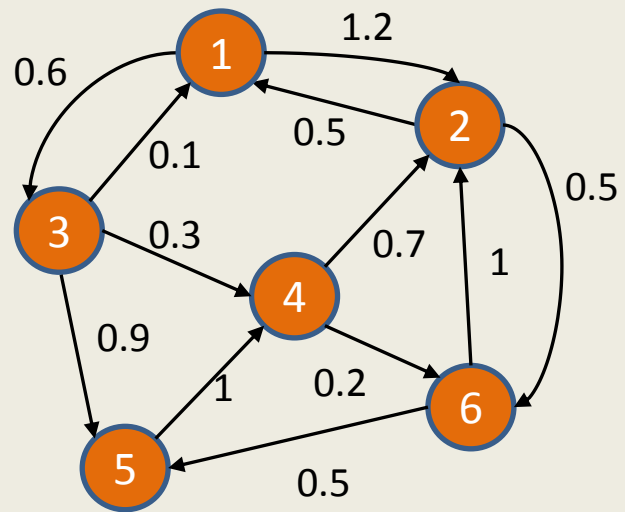
# A Definition of Trust [Massa, 2007]

The explicit opinion expressed by a user about another user regarding the perceived quality of a certain characteristic of this user

– Inter-personal trust



– Network representation



# Challenges in Studying Trust in Social Computing

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- Challenge 1: Social media data is based on passive observations
  - A large number of online users
  - Lack of some information other disciplines use to study trust
  - Traditional methods require interaction with users (or subjects)
  - Study trust with only passive observation
  
- Challenge 2: Social media data is social
  - A new type of social data
  - Big, noisy, and incomplete
  - To handle big social media data for trust research, we need effective and efficient computational tools

# Computational Tasks for Trust

- The challenges from social media also offer opportunities to study trust from a computational perspective

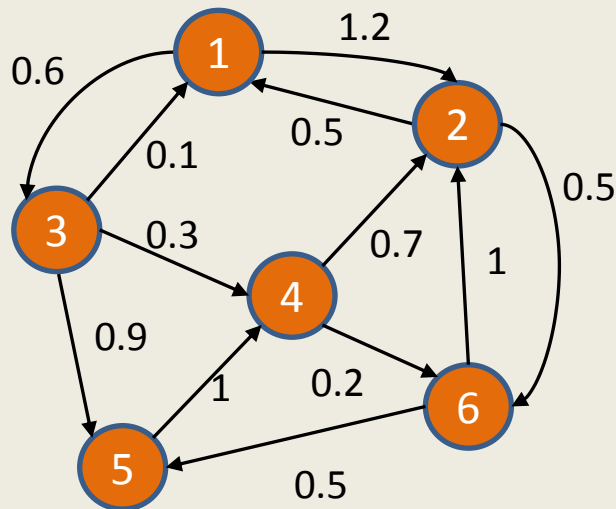
- Four major computational tasks

- Representing trust
- Measuring trust
- Applying trust
- Incorporating distrust



# Representing Trust

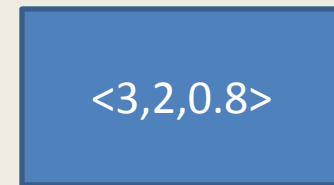
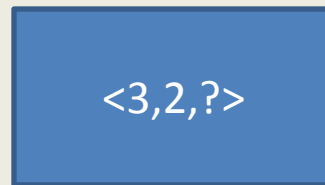
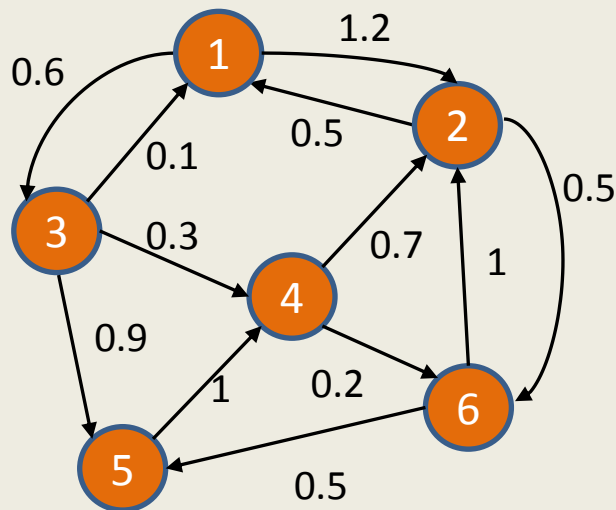
- It aims to represent trust relations among users
- **Given:** a trust network
- **Output:** a mathematical representation that is computable



	1	2	3	4	5	6
1	0	1.2	0.6	0	0	0
2	0.5	0	0	0	0	0.5
3	0.1	0	0	0.3	0.9	0
4	0	0.7	0	0	0	0.2
5	0	0	0	1	0	0
6	0	1	0	0	0.5	0

# Measuring Trust

- It aims to measure how much a user can be trusted by another user in the same trust network
- **Given:** a trust network and a user pair  $\langle u, v, ? \rangle$
- **Output:** the missing trust value is found  $\langle u, v, t \rangle$

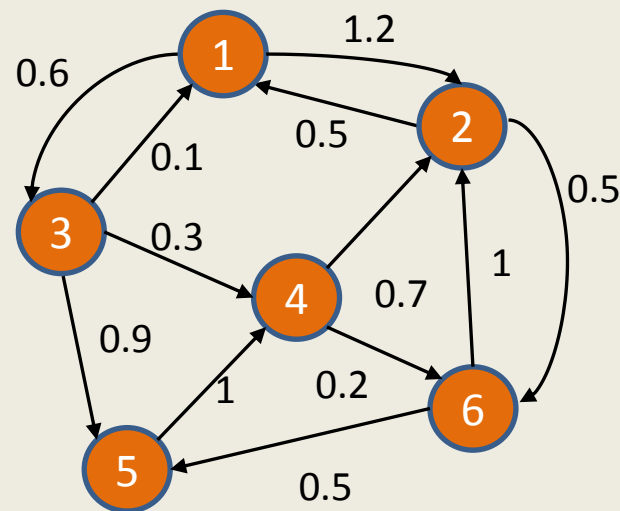


# Applying Trust

- It aims to incorporate trust to facilitate online applications such as online recommendation
- Trust-aware recommendation aims to incorporate trust information in traditional recommender systems
  - User-user trust information
  - User-item rating information

$$\begin{bmatrix} 3 & ? & ? & 5 & ? & 4 \\ ? & 2 & 5 & 4 & 1 & ? \\ ? & ? & ? & ? & ? & ? \\ 2 & 1 & ? & 4 & 2 & ? \\ 3 & 1 & 5 & ? & 2 & ? \\ ? & ? & 4 & ? & 1 & 4 \end{bmatrix}$$

User-item rating information

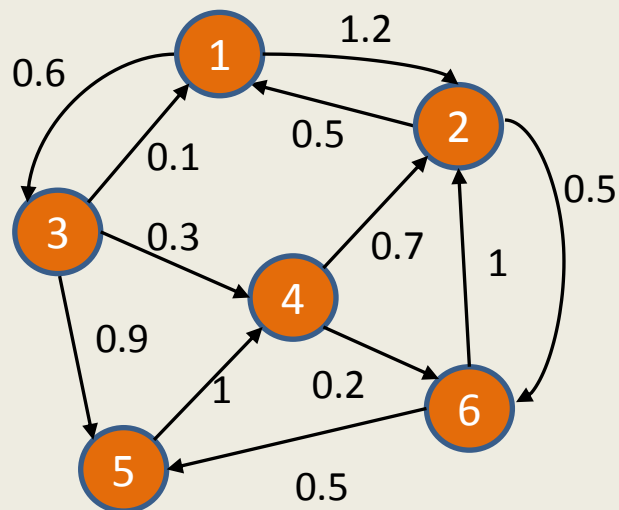


User-user trust information

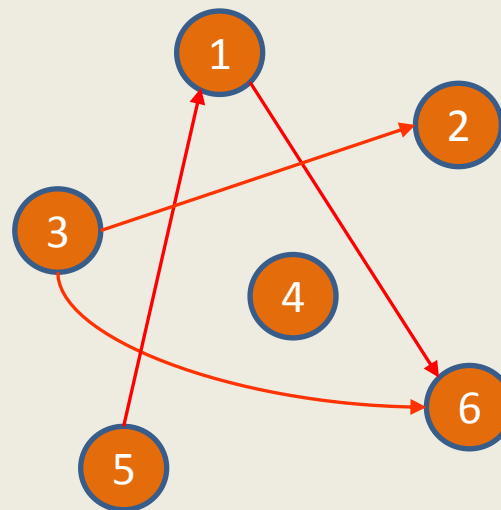
# Incorporating Distrust

It studies how to incorporate distrust in improving trust computation

- Computational understanding of distrust
- Representing distrust with trust
- Measuring distrust with trust
- Applying distrust to improve trust computation



User-user trust information



User-user distrust information



# A Real-World Dataset for Studying Computational Trust

## Epinions

- Trust/distrust relations
- Item ratings
- Helpfulness ratings
- Review content

**Web of Trust**

**sleeper54 trusts:**  
219 hidden members

**sleeper54 is trusted by:**

1. brroberts2
2. tbrown
3. csmithesq
4. beefcake
5. aohcapablanca

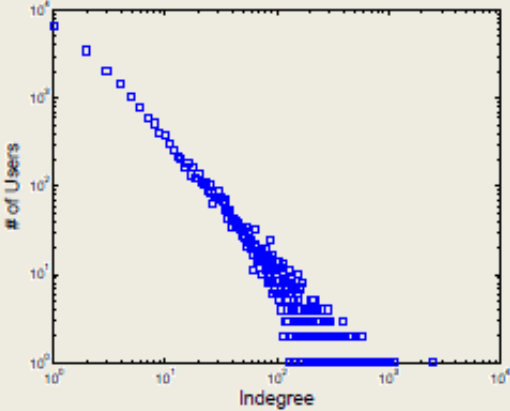
▶ View all 568 members who trust sleeper54

Review Title	Product / Topic	Product Rating	Review Rating
Mickey and Willie: the Parallel Lives of Baseball's Golden Age	Mickey and Willie : Mantle and Mays, the Parallel Lives of Baseball's Golden Age by Allen Barra (2013, Hardcover) in Books	★★★★☆	Very Helpful

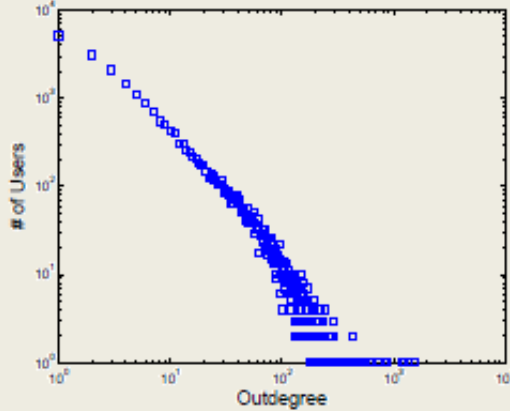
# of Users	30,455
# of Trust	363,773
# of Distrust	46,196
# of Users Receiving Distrust	9,513
# of Users Creating Distrust	5,324
# of Items	89,270
# of Ratings	562,355
Avg of Rating Score	3.9053

# Trust and Distrust Distributions

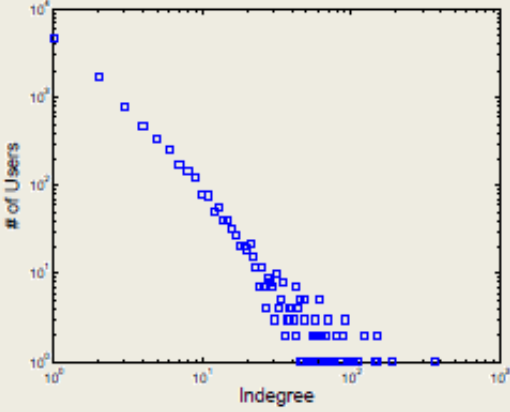
- Distributions follow a power-law-like distribution
  - A typical distribution for networks in social media



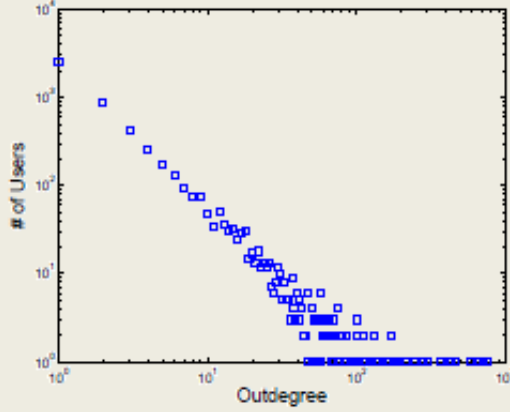
(a) Indegree of Trust



(b) Outdegree of Trust

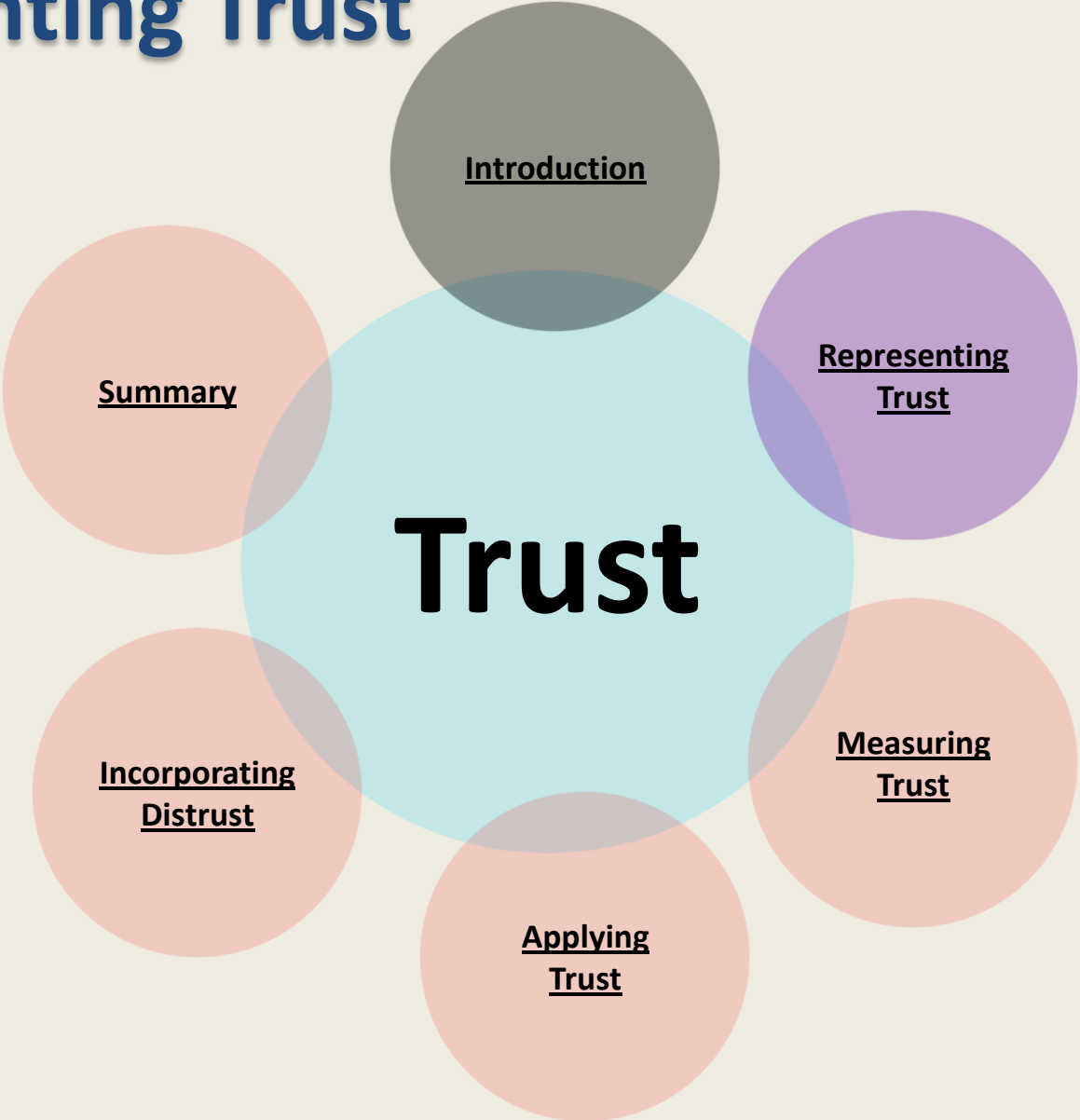


(c) Indegree of Distrust



(d) Outdegree of Distrust

# Representing Trust



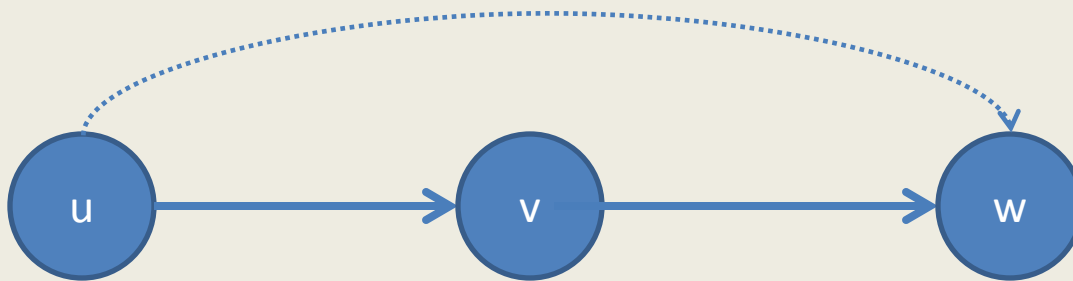
# Importance of Representing Trust

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- Any algorithms in measuring trust, applying trust, and incorporating distrust are based on certain trust representations
- Representing trust is the first step to make trust computable
- Properties of trust serve as the foundation of trust representations
  - Single vs multi-dimensional trust representations
- Some important properties include
  - Transitivity and composability
  - Asymmetry, and correlation with similarity

# Transitivity [Golbeck, 2005]

- Transitivity allows trust to propagate along paths to reach other users
- If  $u$  trusts  $v$  and  $v$  trusts  $w$ , it can be inferred that  $u$  might also trust  $w$  to some extent



- Trust is not perfectly transitive in the mathematical sense and is conditionally transitive
  - Trust networks in social media are large
  - Users in trust networks are world-widely distributed
  - There are many pairs who do not know each other in trust networks

# Transitivity Illustration

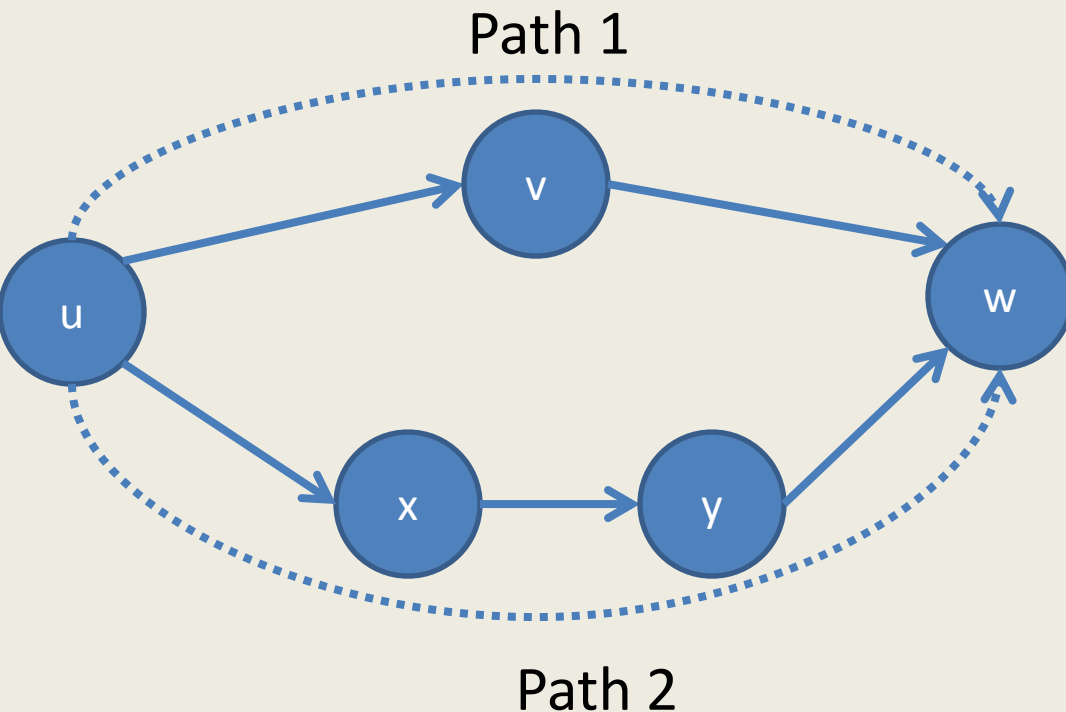
- If  $u+v$  and  $v+w$ , there are 88.34% of  $u$  and  $w$  without trust relations
- If we can observe relations between  $u$  and  $w$ , 97.75% of them are trust relations
- $P1 = \{ \#(u?w) \} / \{ \#(u+w) + \#(u-w) + \#(u?w) \}$
- $P2 = \{ \#(u+w) \} / \{ \#(u+w) + \#(u-w) \}$

Types	Number	P1	P2
$\langle u+v, v+w \rangle, u?w$	25,584,525	88.34%	N.A
$\langle u+v, v+w \rangle, u+w$	3,320,991	11.46%	97.75%
$\langle u+v, v+w \rangle, u-w$	76,613	0.2%	2.25%

$u+v$ ,  $u-v$ , and  $u?v$  represent  $u$  and  $v$  with trust, distrust, and missing relations, respectively

# Composability [Golbeck, 2005]

- Transitivity describes how trust can be passed through one path
- Composability describes that a user should combine the different trust values received from different paths

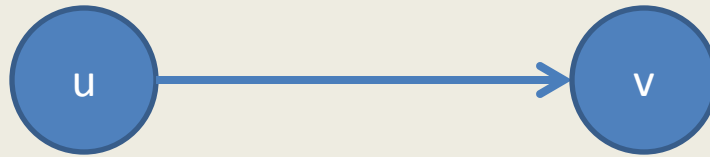


For  $(u,w)$ , there are two paths  $(u+v+w$  and  $u+x+y+w)$ .

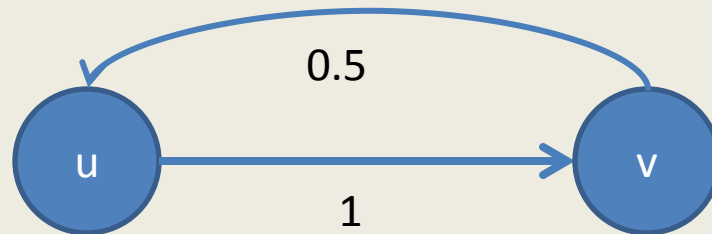
$u$  should compose trust values from both  $u+v+w$  and  $u+x+y+w$  for  $w$

# Asymmetry [Golbeck, 2005]

- For two people involved in a trust relation, trust is not necessarily identical in both directions
- The trust value from user  $u$  to user  $v$  is not necessarily equal to that from user  $v$  to user  $u$ 
  - One way trust for binary trust



- Different trust values for continuous trust



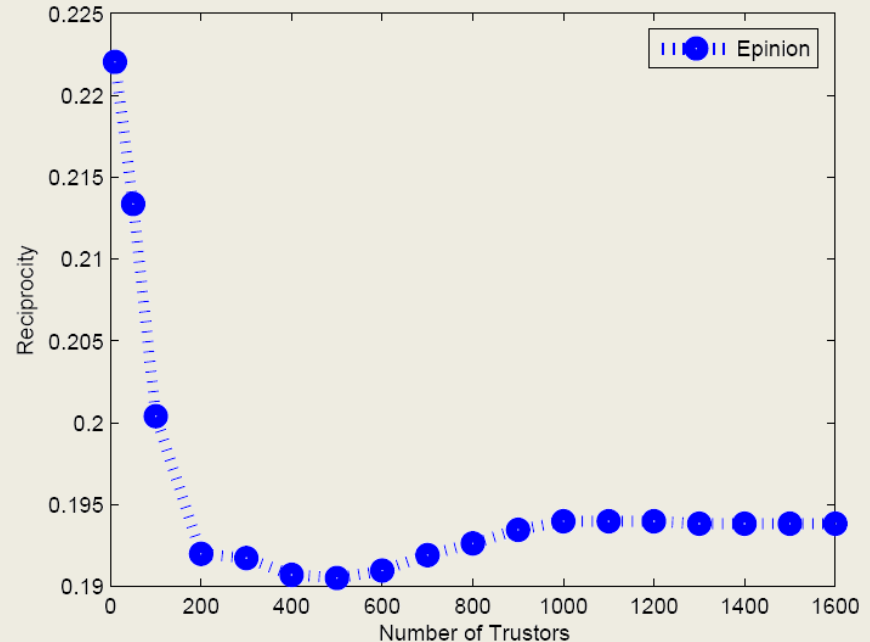


# Asymmetry Illustration

- There are 37.61% of pairs of users with mutual trust relations

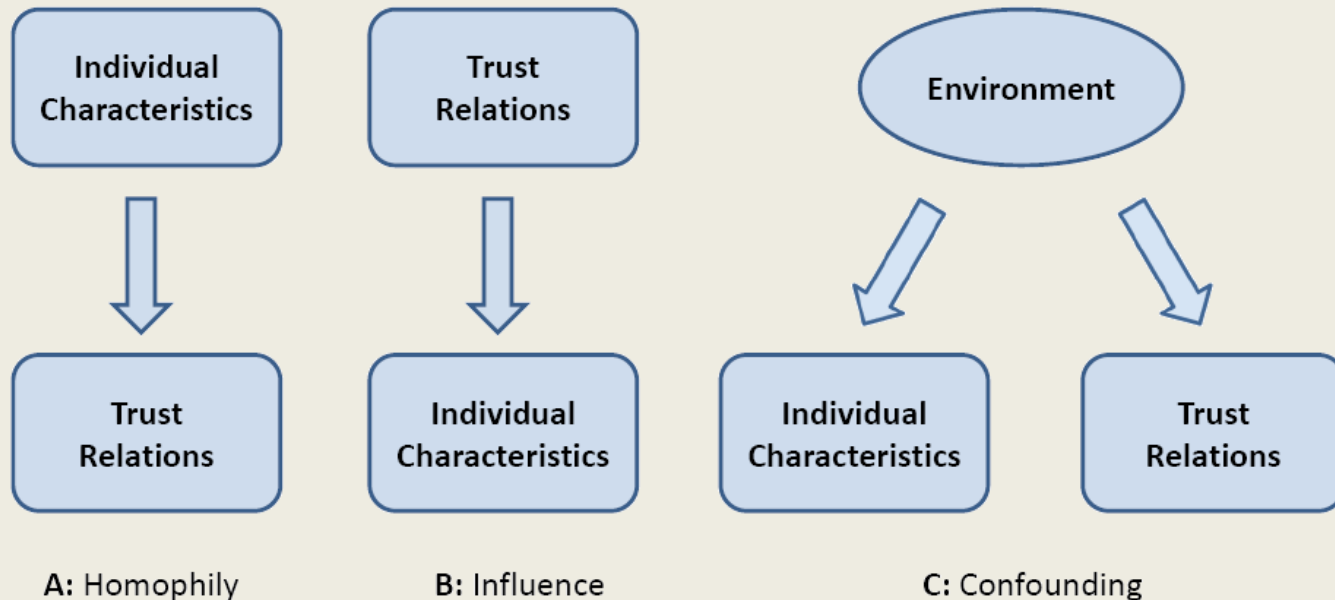
	$v+u(\%)$	$v-u(\%)$	$v?u(\%)$
$u+v$	136,806(37.61)	967(0.27)	226,000(62.13)

- Trustees who have fewer trustors are more likely to trust their trustors [Tang et al. 2012]



# Correlation with Similarity [Ziegler and Golbeck, 2007]

- There is a strong correlation between trust and similarity
  - Users with trust relations are likely to be similar
- Social correlation theories can explain this correlation
  - Homophily, influence and confounding

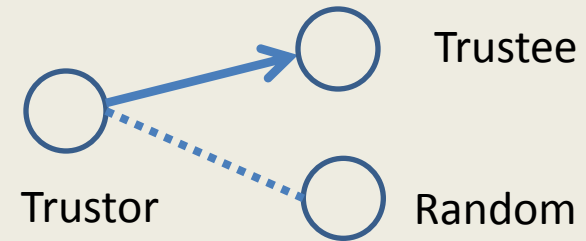


# Verifying the Correlation

- For each trust relation, we calculate two similarities

- Similarity1: trustor and trustee

- Similarity2: trustor and a randomly chosen user



- We define two vectors  $\mathbf{s} = \{\text{similarity1}\}$  and  $\mathbf{t} = \{\text{similarity2}\}$

- We conduct a two-sample t-test on  $\mathbf{s}$  and  $\mathbf{t}$

$$H_0: \mathbf{s} \leq \mathbf{t};$$

$$H_1: \mathbf{s} > \mathbf{t}$$

The null hypothesis is rejected at significance level 0.01 with p-value of  $3.76e^{-21}$  in Epinions

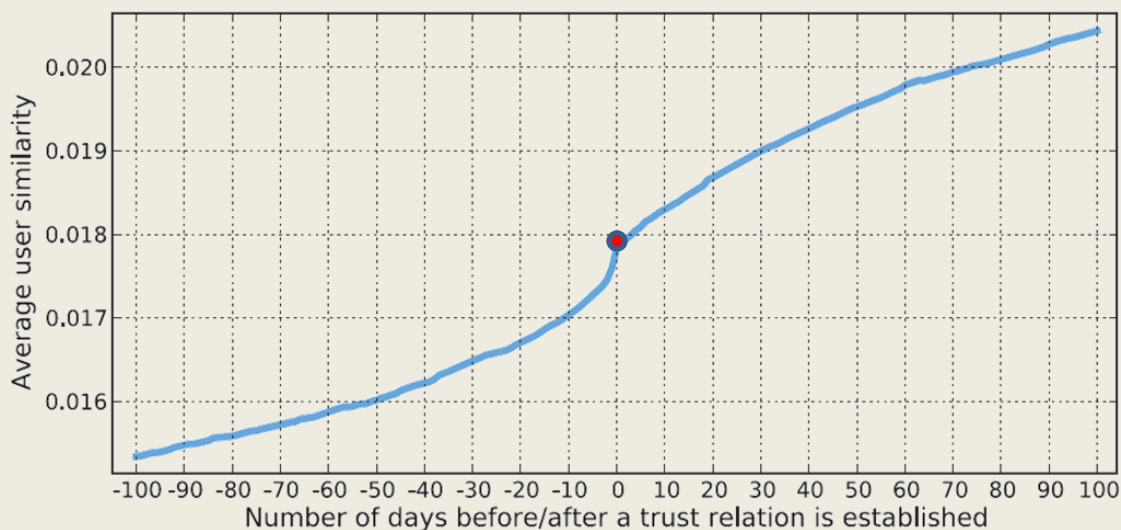
# Homophily [Tang et al., 2013]

- Similar users are more likely to establish trust relations
- Verification of homophily
  - Sort trust relations based on the creation time in chronological order
  - Split data into  $m$  pieces with equal size and time points are  $\{t_1, t_2, \dots, t_m\}$
  - Divide pairs of users without trust relations until time  $t_i$  into two equal groups – high-similarity group  $H$  and low-similarity group  $L$
  - Compute the numbers of pairs creating trust relations  $h_i$  and  $l_i$  at time  $t_{i+1}$  for  $H$  and  $L$ , respectively
  - $\mathbf{h} = \{h_i\}$  and  $\mathbf{l} = \{l_i\}$
  - A two sample t-test is conducted on  $\mathbf{h}$  and  $\mathbf{l}$ 
    - $H_0: \mathbf{h} \leq \mathbf{l};$
    - $H_1: \mathbf{h} > \mathbf{l}$

The null hypothesis is rejected at significance level 0.01 with p-value of  $7.51e^{-64}$  in Epinions

# Influence [Yeung and Iwata, 2011]

- Users tend to follow the behaviors of trusted users and users with trust relations are likely to exhibit similar behaviors
- Changes of users' cosine similarity 100 days before and after trust relations were established
  - Similarity increases before they trust each other, and continues to increase after that



(a) Average user cosine similarity

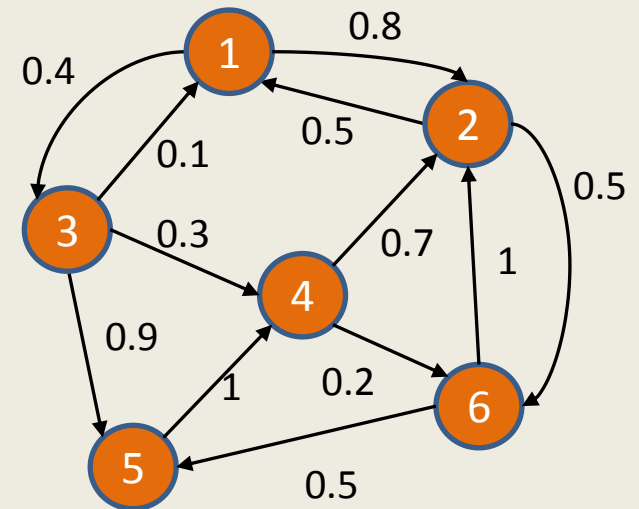
# Trust Representation Classifications

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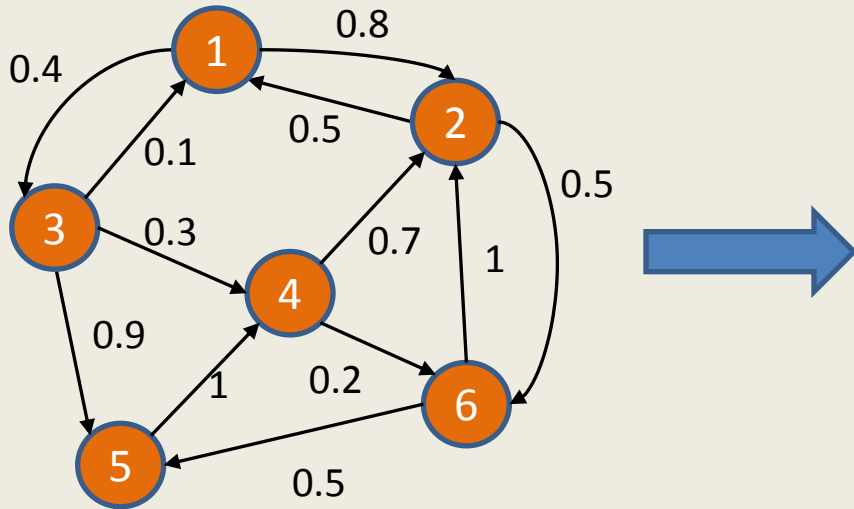
- Trust representations can be classified from different perspectives
- Probabilistic vs. gradual trust representations
  - From an interpretation perspective

# Probabilistic Representations [Victor et al., 2011]

- Probabilistic representations use probabilities to indicate how much trust is placed by a user to another
  - Stronger trust corresponds to a higher probability
  - $(u,v,p)$  represents the probability  $p$  of  $u$  trusting  $v$
  - $p = 1$  represents full trust while  $p = 0$  indicates no trust
- Weights in the trust network represent the probability
  - $(u,v,0)$  is represented no link between  $u$  and  $v$  in the trust network
  - Probabilities usually follow a certain distribution such as beta distribution



# Illustrations of Probabilistic Representations



	1	2	3	4	5	6
1	0	0.8	0.4	0	0	0
2	0.5	0	0	0	0	0.5
3	0.1	0	0	0.3	0.9	0
4	0	0.7	0	0	0	0.2
5	0	0	0	1	0	0
6	0	1	0	0	0.5	0

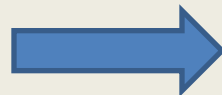
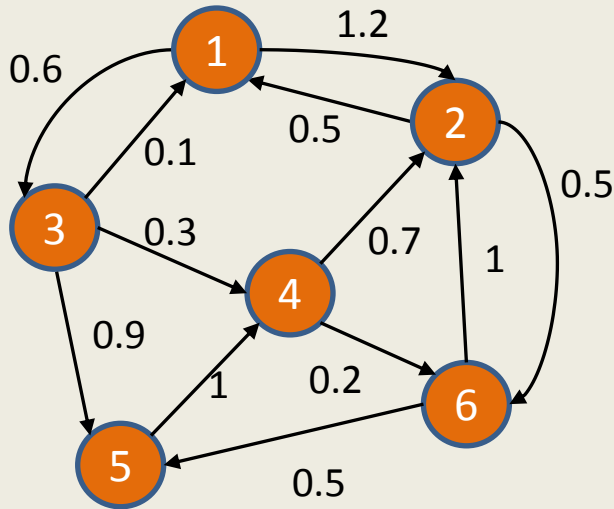
Probabilistic Matrix



# Gradual Representations [Victor et al., 2011]

- Trust is often interpreted as a gradual phenomenon in real life
  - Trusting someone “very much”, “more or less”, “little”...
  - Gradual representations become increasingly popular
- Gradual representations use continuous values to represent trust
  - The values can be any values so they cannot be explained as probabilities
  - The values directly indicate trust strengths
  - $(u,v,t)$  denotes that the trust value from  $u$  to  $v$  is  $t$
  - Weights in the trust network denote trust values
  - $t = 0$  indicates no trust and there is no link in the trust network

# Illustrations of Gradual Models



	1	2	3	4	5	6
1	0	1.2	0.6	0	0	0
2	0.5	0	0	0	0	0.5
3	0.1	0	0	0.3	0.9	0
4	0	0.7	0	0	0	0.2
5	0	0	0	1	0	0
6	0	1	0	0	0.5	0

Trust Value Matrix

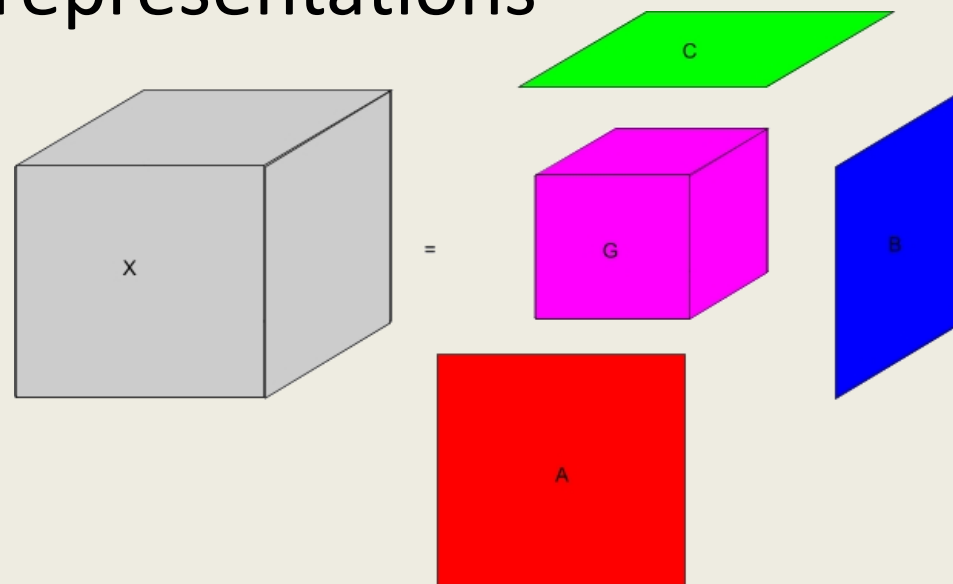
# Trust Representation Classifications

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- Trust representations can be classified from different perspectives
- Probabilistic vs. gradual trust representations
  - From an interpretation perspective
- Single vs. multi-dimensional trust representations
  - From a dimension perspective

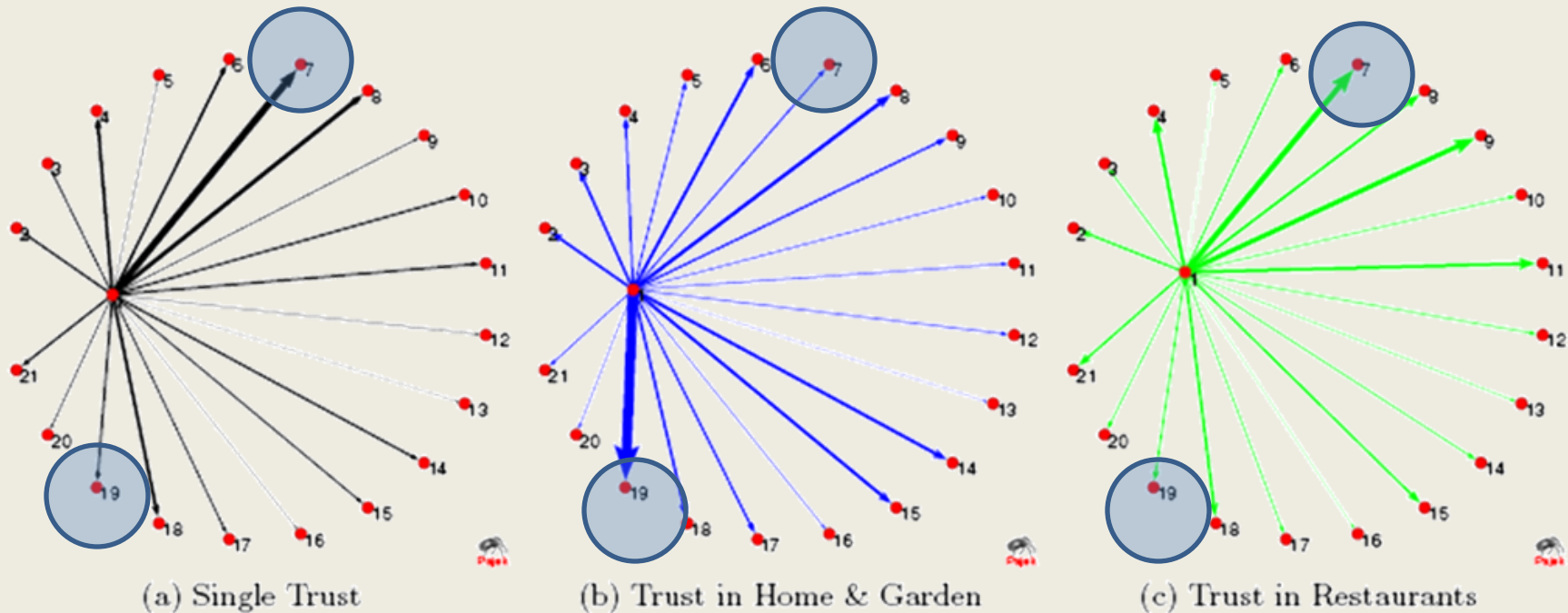
# Multi-dimensional trust representations

- Trust is a complex concept with multiple dimensions
  - Multi-faceted trust
  - Trust evolution
- We need to extend single trust representations to multi-dimensional trust representations



# Multi-Faceted Trust [Tang et al., 2012]

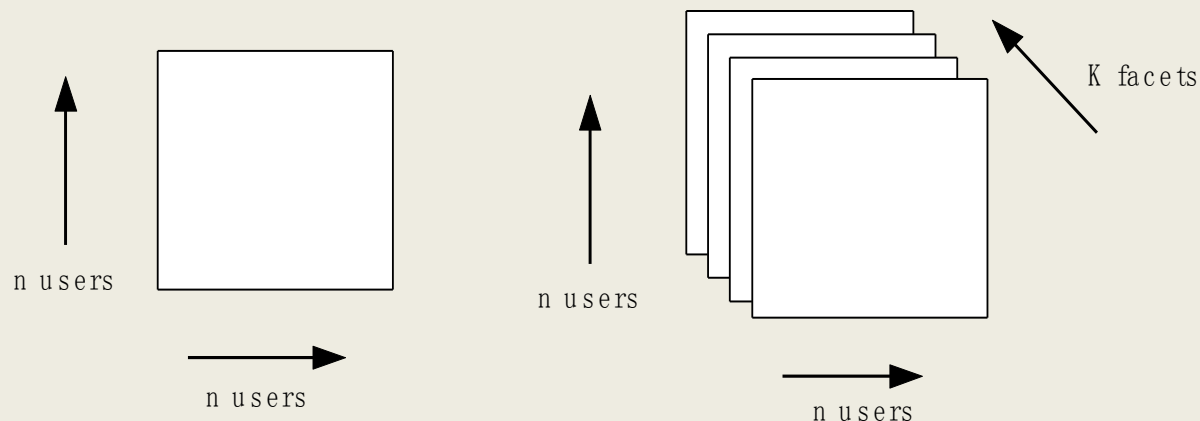
- Trust is context dependent
  - Trusting someone on one topic does not necessarily mean he will be trusted on others
- An illustrative example using the Epinions dataset



# Multi-faceted Trust Representation

A matrix representation can be extended to a tensor representation for multi-faceted trust

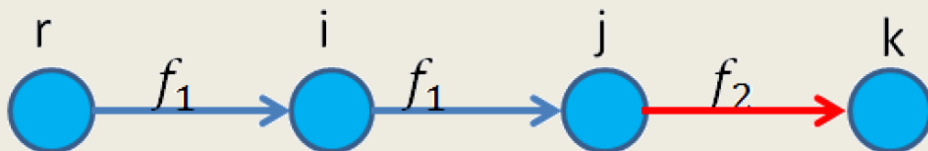
- $\langle u, v, f, p \rangle$
- For probabilistic models,  $u$  trusts  $v$  with probability  $p$  in the facet  $f$
- For gradual models, the trust value between  $u$  and  $v$  in the facet  $f$  is  $p$



# Findings from Multi-faceted Trust Representation

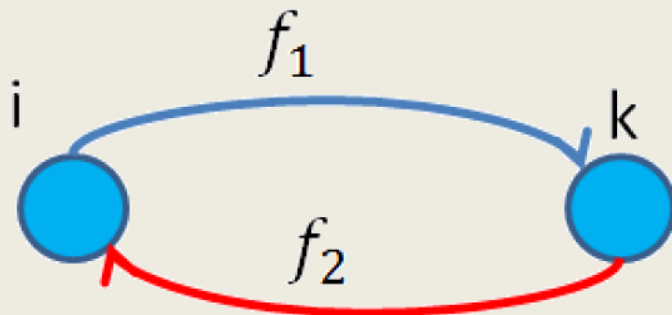
- Heterogeneous transitive trust

- User  $i$  trusts user  $j$  in  $f_1$  and user  $j$  trusts user  $k$  in  $f_2$
- 22.3% transitive trust relations are heterogeneous



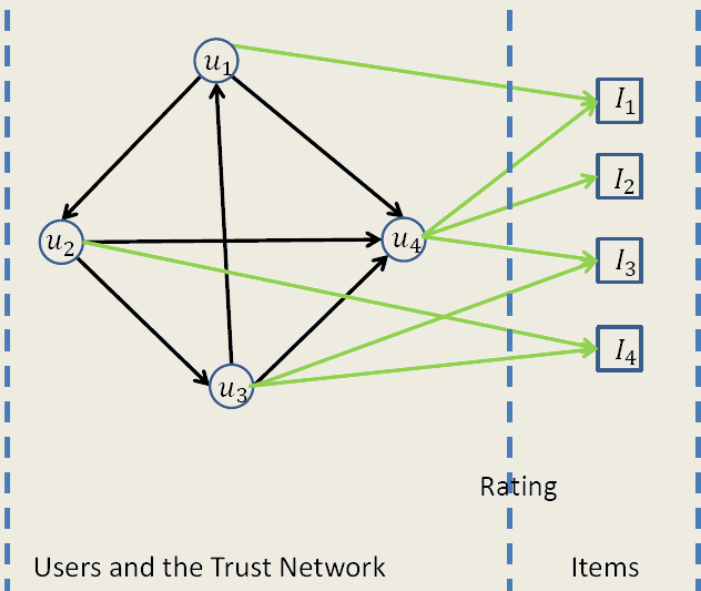
- Heterogeneous reciprocal trust

- User  $i$  trusts user  $k$  in  $f_1$  and user  $k$  trusts  $i$  in  $f_2$
- 23.5% of reciprocal trust relations are heterogeneous

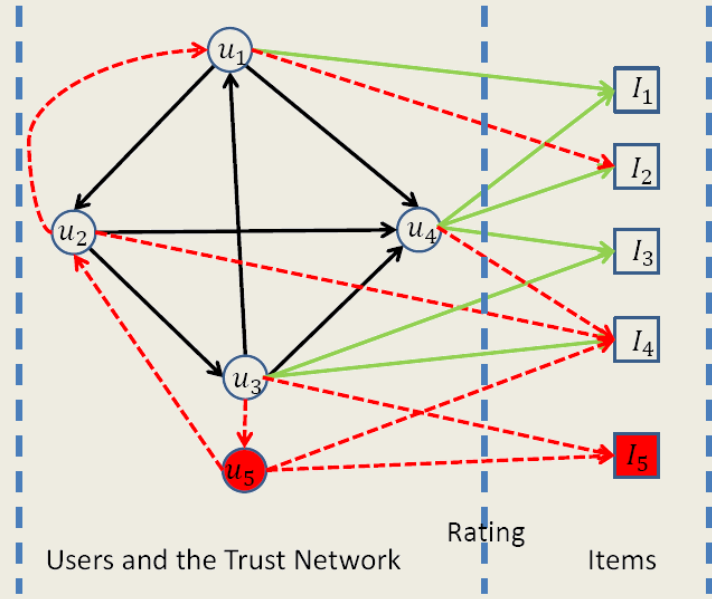


# Trust Evolution [Tang et al. 2012]

- Social sciences suggest that trust evolves as humans interact
- An example from an online rating system Epinions



(a) Rating System at  $T_1$



(b) Rating System at  $T_2$



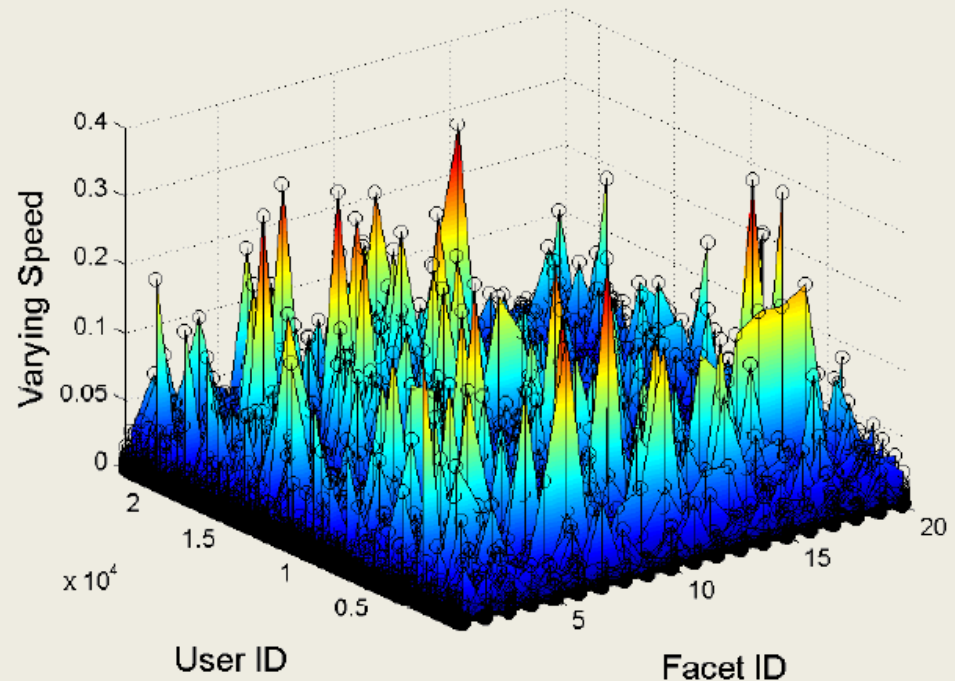
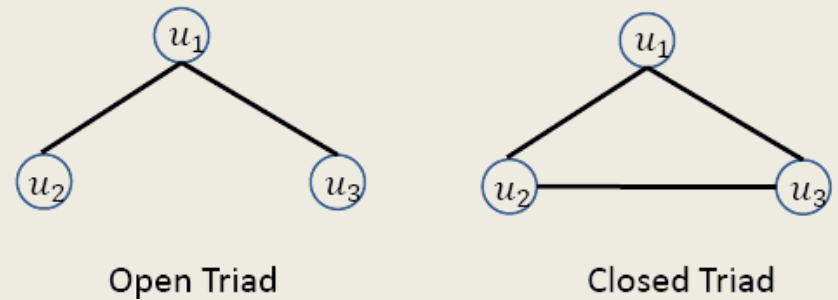
# Trust Evolution Representations

---

- 3-order tensor representations for trust evolution
  - $\langle u, v, T, p \rangle$
  - For probabilistic models,  $u$  trusts  $v$  with probability  $p$  at time  $T$
  - For gradual models, the trust value between  $u$  and  $v$  at time  $T$  is  $p$
- 4-order tensor representations for multi-faceted and evolved trust
  - $\langle u, v, f, T, p \rangle$
  - For probabilistic models,  $u$  trusts  $v$  with probability  $p$  in the facet  $f$  at time  $T$
  - For gradual models, the trust value between  $u$  and  $v$  in the facet  $f$  at time  $T$  is  $p$

# Findings of Trust Evolution

- Trust strength in an open triad evolves faster than that in a close triad
- Trust evolves over time with the changes of user preferences
- Trust evolves differently in different facets

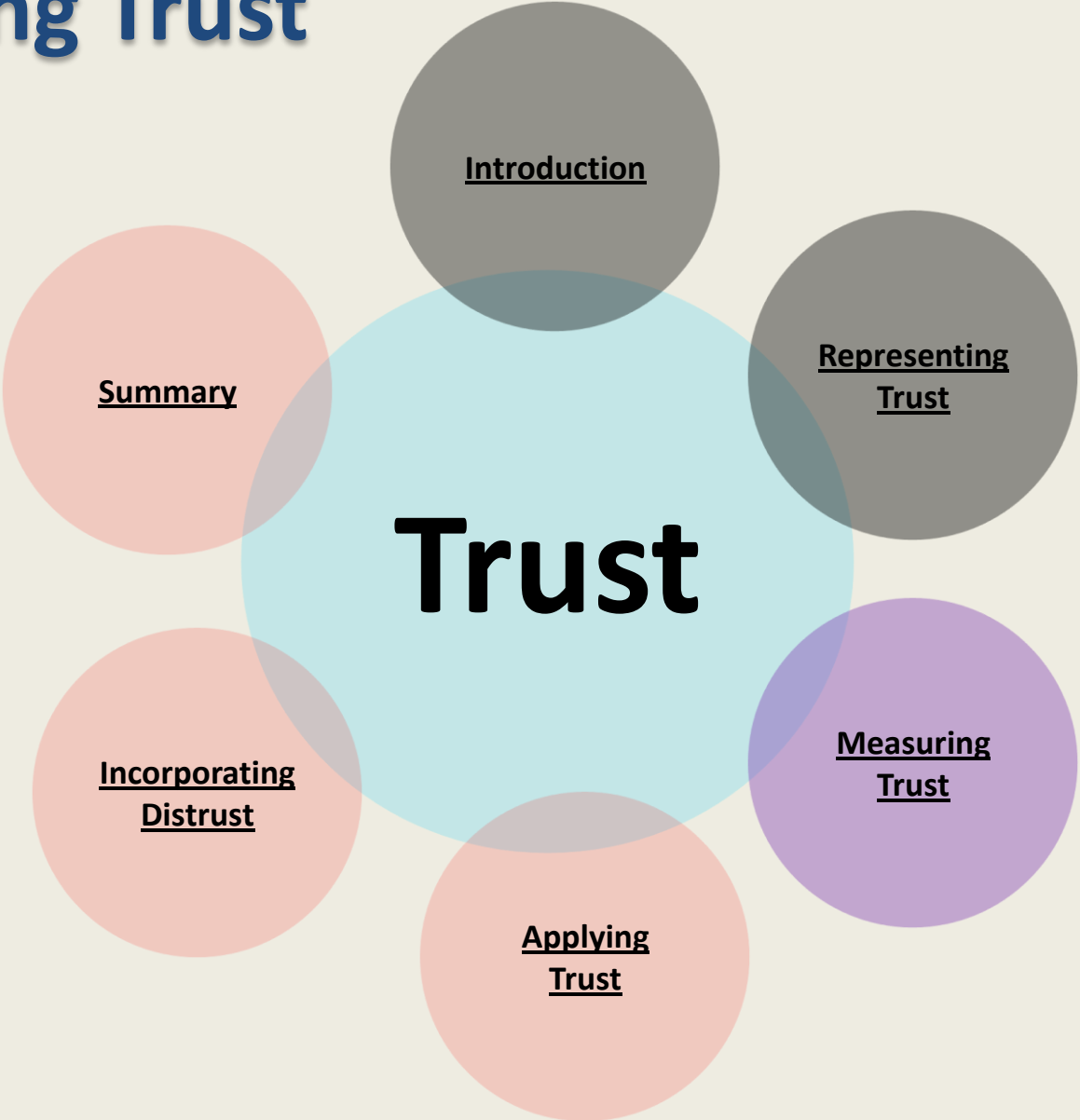


# Trust Representation Classifications

---

- Trust representations can be classified from different perspectives
- Probabilistic vs. gradual trust representations
  - From a interpretation perspective
- Single vs. multi-dimensional trust representations
  - From a dimension perspective
- Trust vs. trust and distrust representations
  - From a network perspective

# Measuring Trust



# Definitions

---

- A trust metric measures how much a certain user can be trusted by the other users for the community
  - Measuring, inferring and predicting trust
  
- Propagation is assumed in most trust metrics
  - We trust our trustees more than a stranger
  - A trustee of our trustee is possibly more trustworthy than a random stranger

# Classifications [Ziegler and Lausen, 2005]

---

- Trust metrics can be classified from different perspectives
- Global and local trust metrics
  - From a personalization perspective
- Supervised vs unsupervised trust metrics
  - From a methodology perspective
- Binary or continuous trust metrics
  - From a network perspective

# Global and Local Metrics

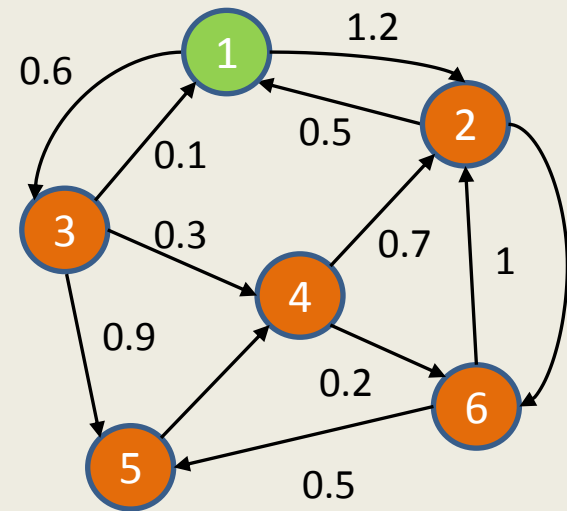
- Global metrics predict the same trust of a given user for all users
  - Each user with a global trust value
  - E.g., Reputation systems



- Local metrics provide a personalized trust score that depends on the point of view of the evaluating user
  - Each pair of users with a trust score
  - Personalized trust
  - Users may have completely different opinions about the same user

# PageRank [Page et al., 1999]

- PageRank is a global metric
- PageRank is from trustees' perspective
- The trustworthiness of a trustee is aggregated from her trustors
  - Trustors' trustworthiness
  - Trust values



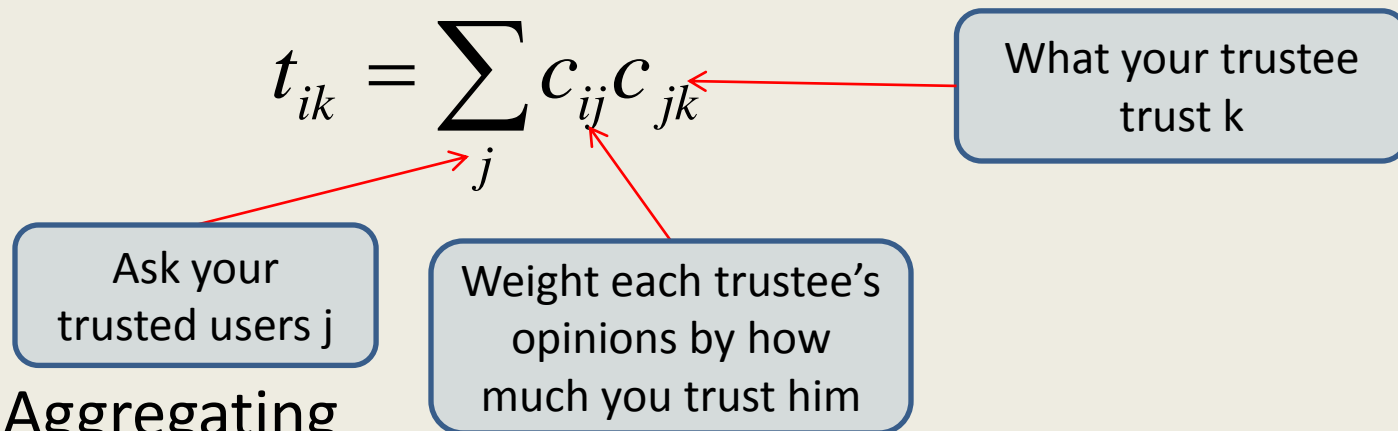
User 1 will give more her trustworthiness to user 2 compared to user 3

$$x_i = \alpha \sum_j x_j \frac{T_{ij}}{\sum_j T_{ij}} + (1 - \alpha) \beta$$



# EigenTrust [Kamvar et al., 2003]

- Asking your trustees and aggregating trust for trustees



- Iterative Aggregating

– Ask your trustees:  $\mathbf{t} = C^T \mathbf{c}_i$

– Ask trustees' trustees:  $\mathbf{t} = (C^T)^2 \mathbf{c}_i$

– Keep asking until  $\mathbf{t}$  converges:  $\mathbf{t} = (C^T)^n \mathbf{c}_i$

$$C = [c_{ij}]$$

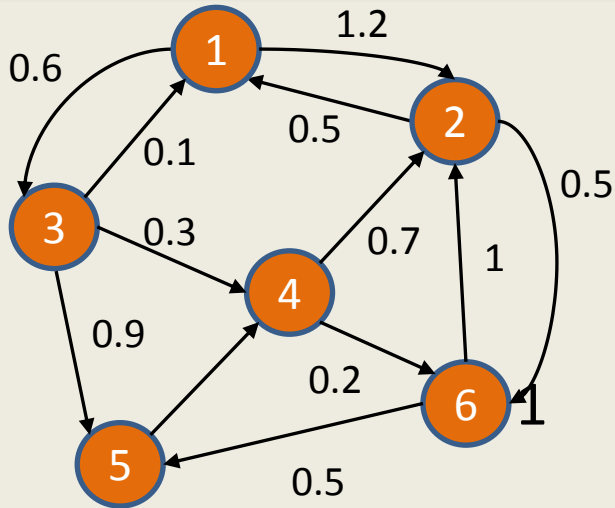
$$c_{i1} + c_{i2} + \dots + c_{in} = 1$$

- When  $n$  is large,  $\mathbf{t}$  converges to the same vector for every user

–  $\mathbf{t}$  is the eigenvector of  $C$

$$\mathbf{t}^{(k+1)} = C^T \mathbf{t}^{(k)}$$

# An Illustration Example of EigenTrust



Normalization

$$C = \begin{bmatrix} 0 & 0.67 & 0.33 & 0 & 0 & 0 \\ 0.5 & 0 & 0 & 0 & 0 & 0.5 \\ 0.08 & 0 & 0 & 0.23 & 0.69 & 0 \\ 0 & 0.78 & 0 & 0 & 0 & 0.22 \\ 0 & 0 & 0 & 1 & 0 & 0 \\ 0 & 0.67 & 0 & 0 & 0.33 & 0 \end{bmatrix}$$

$$t^0 = \begin{bmatrix} 0.1667 \\ 0.1667 \\ 0.1667 \\ 0.1667 \\ 0.1667 \\ 0.1667 \end{bmatrix} \quad t^1 = C^T t^0 = \begin{bmatrix} 0.0967 \\ 0.3534 \\ 0.0550 \\ 0.2050 \\ 0.1700 \\ 0.1200 \end{bmatrix} \quad t^2 = C^T t^1 = \begin{bmatrix} 0.1811 \\ 0.3051 \\ 0.0319 \\ 0.1827 \\ 0.0776 \\ 0.2218 \end{bmatrix} \quad \dots \quad \begin{bmatrix} 0.1764 \\ 0.3434 \\ 0.0582 \\ 0.1188 \\ 0.1055 \\ 0.1979 \end{bmatrix}$$

# TidalTrust [Golbeck, 2006]

- TidalTrust is guided by two observations
  - Shorter propagation paths produce more accurate trust estimates
  - Paths with higher trust values create better results
- For a pair of users  $i$  and  $s$  who are not directly connected, a trust value is aggregated from the trust value from  $i$ 's direct neighbors to  $s$ , weighted by the direct trust values from  $i$  to her direct neighbors

The diagram illustrates the TidalTrust formula for calculating the trust value  $t_{is}$  between users  $i$  and  $s$ . The formula is:

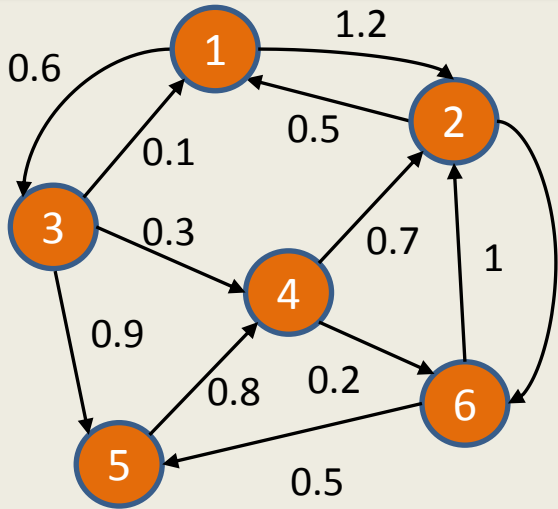
$$t_{is} = \frac{\sum_{j \in \text{adj}(j) \mid t_{ij} \geq \text{max}} t_{ij} t_{js}}{\sum_{j \in \text{adj}(j) \mid t_{ij} \geq \text{max}} t_{ij}}$$

Two callout boxes are present:

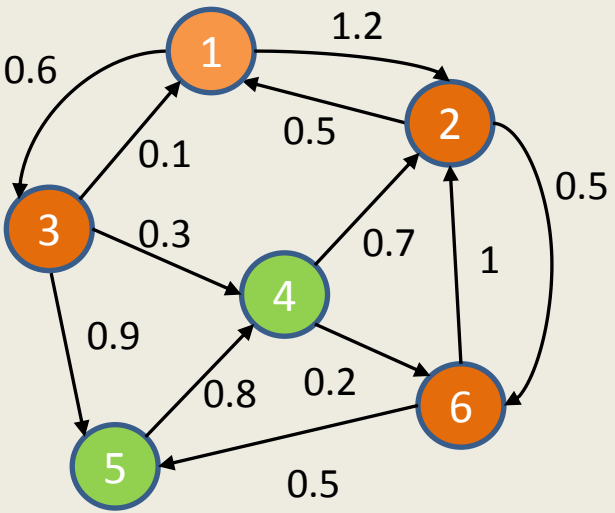
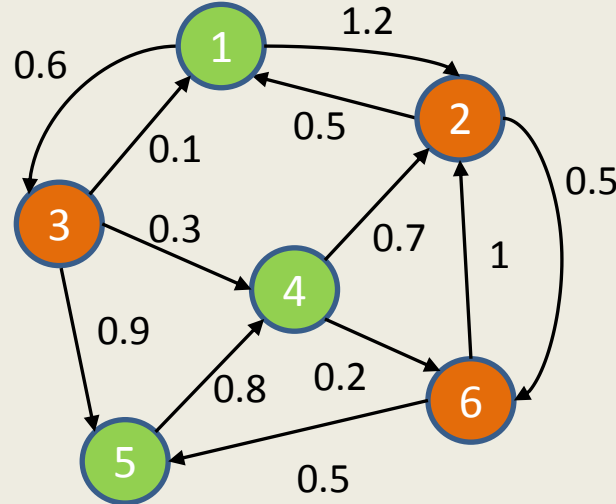
- A box labeled "Neighbors" has a red arrow pointing to the set of neighbors  $j \in \text{adj}(j) \mid t_{ij} \geq \text{max}$  in the numerator and denominator.
- A box labeled "Higher trust values" has a red arrow pointing to the trust value  $t_{js}$  in the numerator.

The length of a path is determined by the number of edges the source must traverse before reaching the sink

# An Illustration Example of TidalTrust



$t_{36} = ?$   
 $\max = 0.15$



$t_{31} < \max$

$$t_{36} = \frac{t_{34} * t_{46} + t_{35} * t_{56}}{t_{34} + t_{35}} = \frac{0.3 * 0.2 + 0.9 * t_{56}}{1.2}$$

$$t_{56} = \frac{t_{54} * t_{46}}{t_{54}} = 0.2$$

$$t_{36} = 0.2$$

# MoleTrust [Massa and Avesani, 2005]

---

- Cycles in a trust network are removed
  - The removal reduces the number of trust propagations
  - The trust network is transformed into a directed acyclic graph
  
- Trust values are calculated based on the directed acyclic graph by performing a simple graph random walk
  - The trust of the users at 1-hop away is computed
  - The trust of the users at 2-hop away, etc.

# Comparison between Global and Local Metrics

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- Global metrics

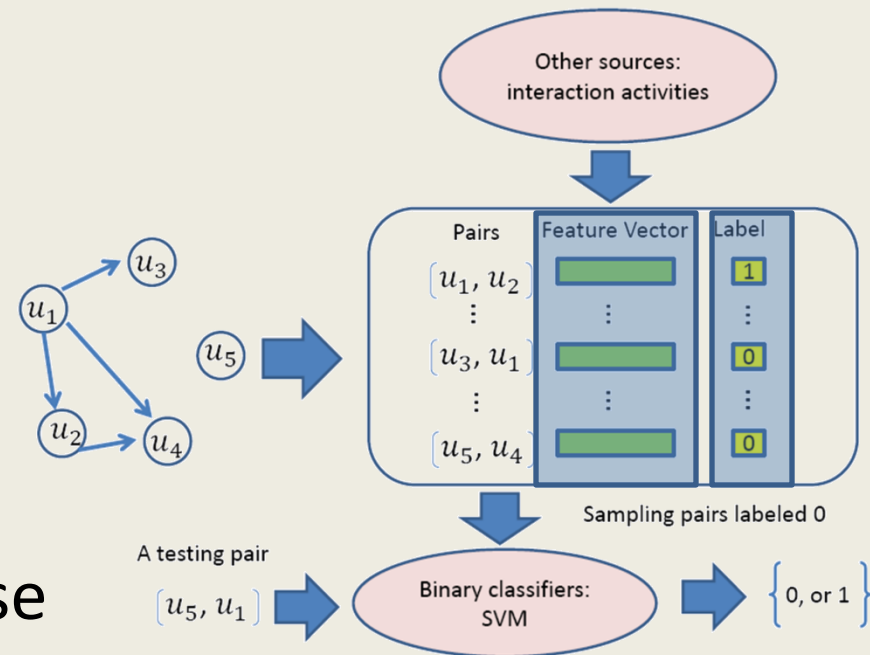
- For  $n$  users, we only need to compute  $n$  values
- Efficient to compute and maintain
- Providing a global view about a user's reputation

- Local metrics

- For  $n$  users, we have  $n*n$  pairs of users
- Providing personalized trust values
- Applying to controversial users

# Supervised Metrics

- Supervised metrics consider trust prediction as a classification problem
- Training data preparation
  - Trust as the positive label
  - Not trust as the negative label
- Feature extraction
  - Extracting a set of features from available sources to represent pairs of users
- Different supervised metrics use different feature sets and classifiers



# Method by Liu et al. [Liu et al., 2008]

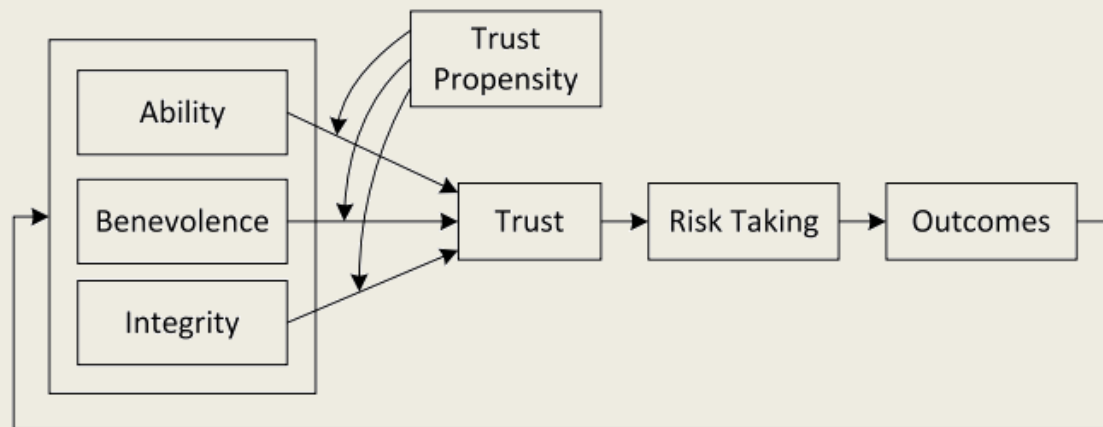
---

- It assumes there are two reasons a user trusts another user
  - The trustee has good reputation
  - There have been good personal interactions between the two users
- Each reason is captured by a set of features
  - Features based on user factors
  - Features based on interaction factors
- SVM and NB classifiers are trained to predict trust
- Interaction factors have greater impact on trust decisions than user factors
  - Trust is highly relevant to user interactions



# Method by Nguyen et al. [Nguyen et al., 2009]

- It is based on trust antecedent framework in management science
  - Ability, benevolence and integrity as key factors that leads to trust on a trustee
  - Trust propensity is a factor that determines how easy a trustor trusts someone
  - Once a trust is formed, the trustor is more willing to take more risk
  - The outcome of risk taking will serve as feedback to modify the perception about trustee's ability, benevolence and integrity

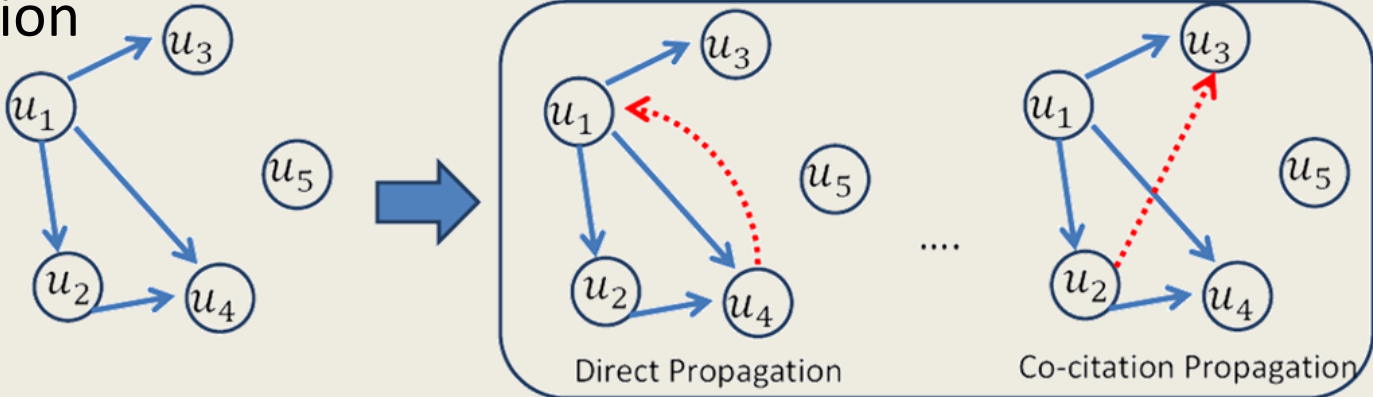


- Each factor is approximated through a set of quantitative features
  - Features for integrity: the number of trust statements the user receives
  - Features for ability: the number of reviews rated by the rater

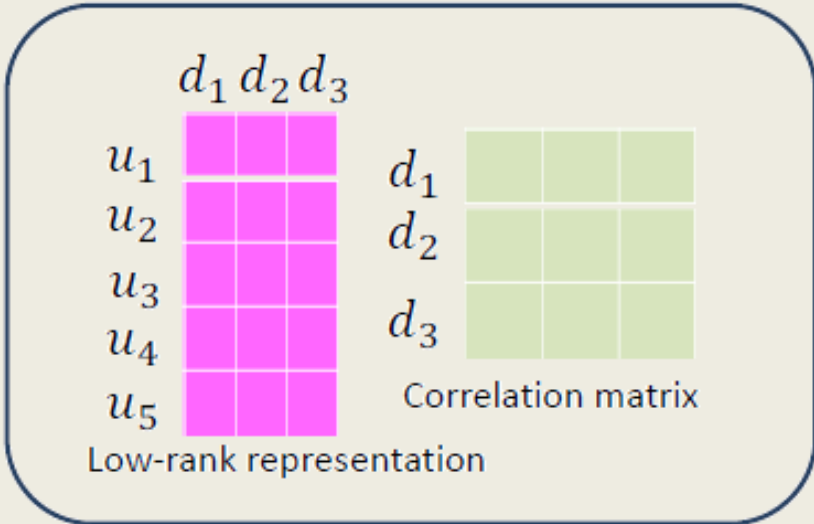
# Unsupervised Metrics

- Unsupervised methods are usually based on the connectivity of users in trust networks

- Trust Propagation

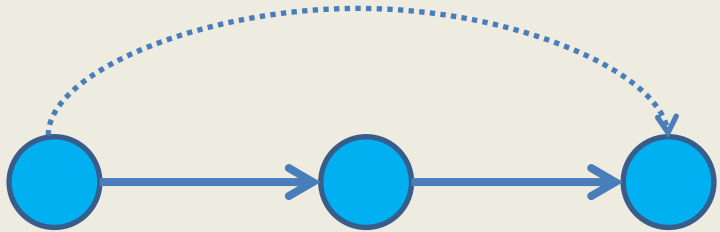


- Low-rank representations of trust networks

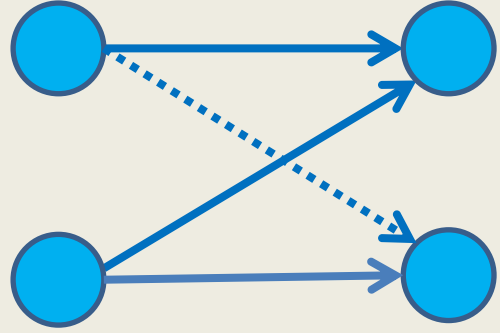


# Trust Propagation [Guha et al., 2004]

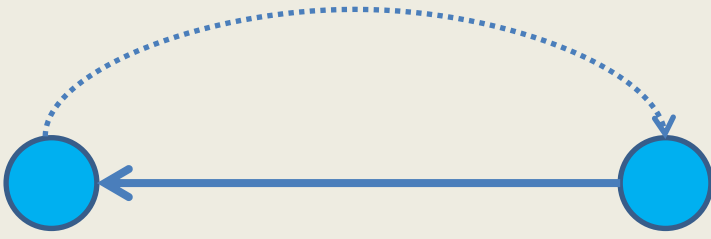
## Four types of atom trust propagations



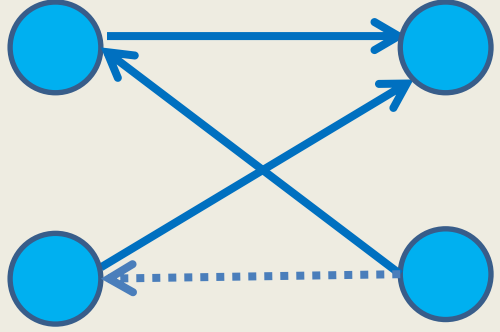
Direct propagation



Co-citation



Transpose trust



Trust Coupling

# Propagation Operations

Atomic Propagation	Operator	Description
Direct propagation	$T$	If A trusts B, and B trusts C, then A may trust C
Transpose trust	$T^T$	A's trust of B causes B to develop some level of trust towards A
Co-citation	$T^T T$	If A trusts B and C, D trusting B implies D should trust C
Trust Coupling	$TT^T$	If A and B trust C, trusting A should imply trusting B

# Trust Propagation Aggregation

- A combination of four types of propagations

$$C = aT + bT^T T + cT^T + dTT^T$$

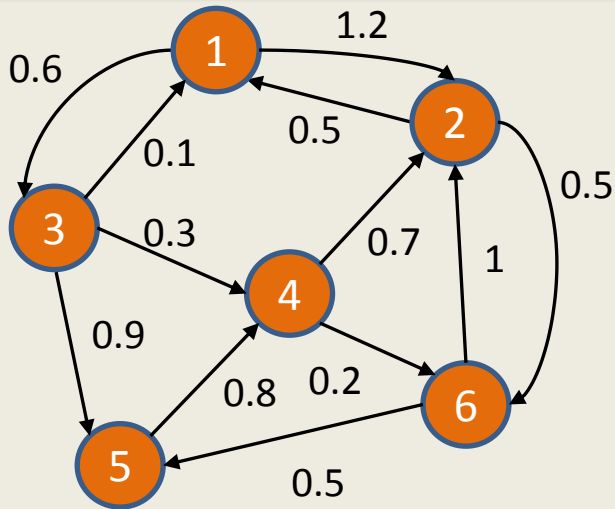
a, b, c, and d are the weights for these four types of propagation, respectively

- Aggregation after K-step propagation

$$\hat{T} = \sum_{k=1}^K r_k C_k$$

$r_k$  is the aggregation weight for the k-th propagation

# An Illustration of Trust Propagation



$a=b=c=d=0.25$   
 $r_1=r_2=0.5$

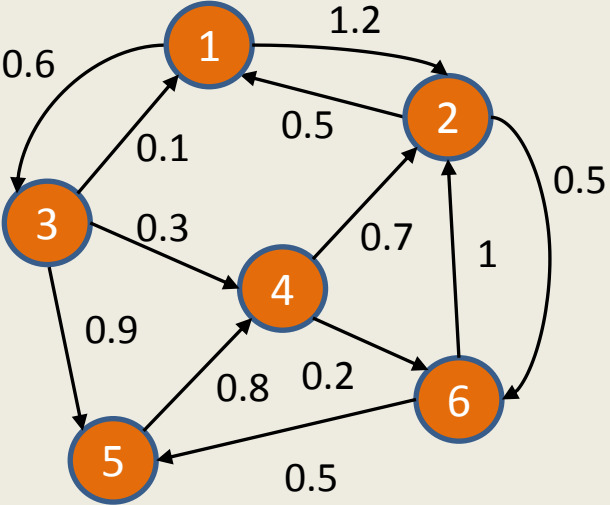


$$T = \begin{matrix} & \begin{matrix} 1 & 2 & 3 & 4 & 5 & 6 \end{matrix} \\ \begin{matrix} 1 \\ 2 \\ 3 \\ 4 \\ 5 \\ 6 \end{matrix} & \begin{bmatrix} 0 & 1.2 & 0.6 & 0 & 0 & 0 \\ 0.5 & 0 & 0 & 0 & 0 & 0.5 \\ 0.1 & 0 & 0 & 0.3 & 0.9 & 0 \\ 0 & 0.7 & 0 & 0 & 0 & 0.2 \\ 0 & 0 & 0 & 0.8 & 0 & 0 \\ 0 & 1 & 0 & 0 & 0.5 & 0 \end{bmatrix} \end{matrix}$$

$$C_1 = \begin{bmatrix} 0.51 & 0.42 & 0.17 & 0.22 & 0.02 & 0.36 \\ 0.42 & 0.86 & 0.19 & 0.20 & 0.12 & 0.41 \\ 0.17 & 0.19 & 0.32 & 0.07 & 0.28 & 0.11 \\ 0.22 & 0.20 & 0.07 & 0.31 & 0.27 & 0.22 \\ 0.02 & 0.12 & 0.28 & 0.27 & 0.42 & 0.12 \\ 0.36 & 0.41 & 0.11 & 0.22 & 0.12 & 0.38 \end{bmatrix}$$

$$C_2 = \begin{bmatrix} 0.58 & 0.62 & 0.23 & 0.29 & 0.12 & 0.47 \\ 0.62 & 1.02 & 0.29 & 0.33 & 0.28 & 0.58 \\ 0.23 & 0.29 & 0.29 & 0.15 & 0.28 & 0.19 \\ 0.29 & 0.33 & 0.15 & 0.31 & 0.27 & 0.29 \\ 0.12 & 0.23 & 0.28 & 0.27 & 0.39 & 0.19 \\ 0.47 & 0.58 & 0.19 & 0.29 & 0.19 & 0.45 \end{bmatrix}$$

# An Illustration Example of Trust Propagation



$$T = \begin{matrix} & \begin{matrix} 1 & 2 & 3 & 4 & 5 & 6 \end{matrix} \\ \begin{matrix} 1 \\ 2 \\ 3 \\ 4 \\ 5 \\ 6 \end{matrix} & \begin{bmatrix} 0 & 1.2 & 0.6 & 0 & 0 & 0 \\ 0.5 & 0 & 0 & 0 & 0 & 0.5 \\ 0.1 & 0 & 0 & 0.3 & 0.9 & 0 \\ 0 & 0.7 & 0 & 0 & 0 & 0.2 \\ 0 & 0 & 0 & 0.8 & 0 & 0 \\ 0 & 1 & 0 & 0 & 0.5 & 0 \end{bmatrix} \end{matrix}$$

$a=b=c=d=0.25$   
 $r_1=r_2=0.5$

$$\hat{T} = 0.5C_1 + 0.5C_2 = \begin{matrix} & \begin{matrix} 1 & 2 & 3 & 4 & 5 & 6 \end{matrix} \\ \begin{matrix} 1 \\ 2 \\ 3 \\ 4 \\ 5 \\ 6 \end{matrix} & \begin{bmatrix} 0.28 & 0.55 & 0.25 & 0.11 & 0.01 & 0.18 \\ 0.46 & 0.49 & 0.10 & 0.10 & 0.06 & 0.45 \\ 0.13 & 0.10 & 0.16 & 0.15 & 0.49 & 0.05 \\ 0.11 & 0.49 & 0.04 & 0.16 & 0.13 & 0.22 \\ 0.01 & 0.06 & 0.14 & 0.63 & 0.21 & 0.06 \\ 0.18 & 0.54 & 0.05 & 0.11 & 0.23 & 0.19 \end{bmatrix} \end{matrix}$$

# Low-rank Matrix Factorization [Tang-etal.,2013]

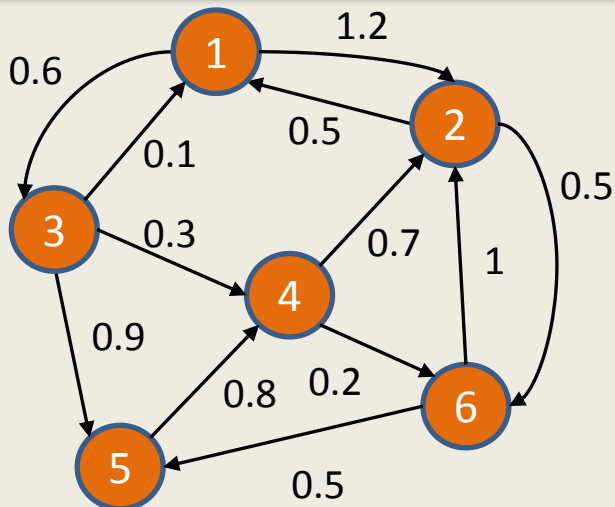
- Trust is multi-faceted and is correlated to user preferences
  - Assume  $\mathbf{U}_i$  is the k-dimensional preference vector of the user i
  - $\mathbf{V}$  is a K x K correlation matrix
  - A trust relation between user i and user j can be modeled as the interactions between their preferences by  $\mathbf{V}$  as

$$T_{ij} = U_i V U_j$$

- Low-rank matrix factorization model can capture the major properties of trust,
  - Multi-faceted
  - Correlation with user preferences
  - Transitivity and asymmetry



# An Illustration of Low-rank Matrix Factorization



$$T = \begin{bmatrix} 0 & 1.2 & 0.6 & 0 & 0 & 0 \\ 0.5 & 0 & 0 & 0 & 0 & 0.5 \\ 0.1 & 0 & 0 & 0.3 & 0.9 & 0 \\ 0 & 0.7 & 0 & 0 & 0 & 0.2 \\ 0 & 0 & 0 & 0.8 & 0 & 0 \\ 0 & 1 & 0 & 0 & 0.5 & 0 \end{bmatrix}$$

K=1

$$U = \begin{bmatrix} 0.4969 \\ 0.6635 \\ 0.2616 \\ 0.3229 \\ 0.2730 \\ 0.4534 \end{bmatrix} \quad V = 1.1511 \quad \hat{T} = UVU^T = \begin{bmatrix} 0.28 & 0.38 & 0.15 & 0.18 & 0.16 & 0.26 \\ 0.38 & 0.51 & 0.20 & 0.25 & 0.21 & 0.34 \\ 0.15 & 0.20 & 0.08 & 0.10 & 0.08 & 0.13 \\ 0.18 & 0.24 & 0.10 & 0.12 & 0.10 & 0.17 \\ 0.16 & 0.21 & 0.08 & 0.10 & 0.08 & 0.14 \\ 0.26 & 0.34 & 0.14 & 0.17 & 0.14 & 0.23 \end{bmatrix}$$

# Comparison of Supervised and Unsupervised Metrics

---

## ■ Supervised metrics

- The number of pairs without trust is much larger than those with
- The classification problem is highly imbalanced
- They need extra sources to extract features
- They usually outperform unsupervised metrics
- They can be applied to users with few trust relations

## ■ Unsupervised metrics

- They only depend on the structure of trust networks
- They may fail for users with few trust relations
- They can be applied to both binary and weighted trust networks

# Binary and Continuous Metrics

---

- Binary metrics are used to predict whether users are trusted or not trusted
  - {1:trust, 0: not trust}
  - For supervised metrics, trust and not trust are positive and negative labels to predict by learnt classifiers
  - For unsupervised metrics, trust values in a certain region are treated as trust, otherwise as not trust
  
- Continuous metrics are to infer trust values for pairs of users
  - Nonnegative real number
  - Continuous metrics are usually unsupervised methods

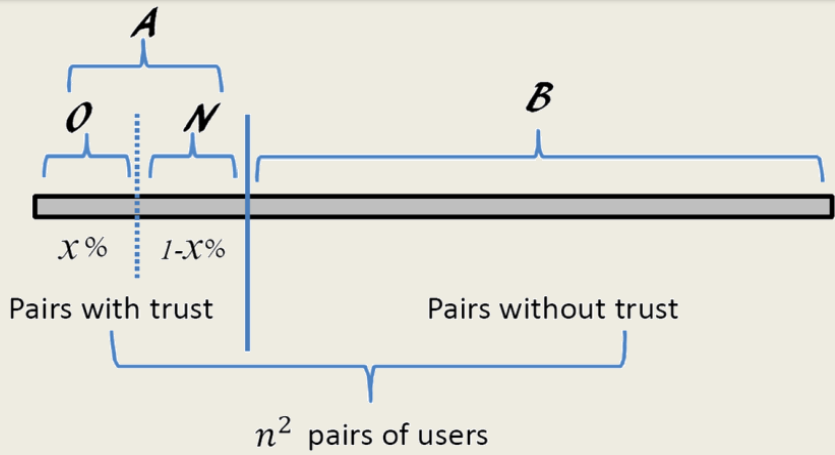
# Evaluations of Trust Metrics

---

- There are many evaluation metrics proposed to assess the performance of trust metrics
- Ranking-based evaluation
- RMSE evaluation
- Leave-one-out cross-validation evaluation
- F-measure evaluation

# Ranking-based Evaluation

- x% as old trust relations
- 1 - x% as new trust relations
- Ranking pairs of users in N and B
- Choosing top-|N| ranked pairs as C as predicted trust relations
- Calculating the prediction quality as



$$PA = \frac{|N \cap C|}{|N|}$$

N		C	
1	2	1	2
2	5	2	3
3	5	2	5
4	6	4	5
1	5	1	6

$$PA = \frac{1}{5} = 0.2$$

The value of PA is usually small and to demonstrate the significance of performance, randomly guessing predictor is usually used as a baseline method

# RMSE Evaluation

- $x\%$  as old trust relations  $O$
- $1 - x\%$  as new trust relations  $N$
- Computing trust values for pairs of users in  $N$
- Calculating RMSE as

$$RMSE = \sqrt{\frac{\sum_{\langle u_i, u_j \rangle \in N} (\hat{T}_{ij} - T_{ij})^2}{|N|}}$$

$T_{ij}$     $\hat{T}_{ij}$

0.2	0.2
0.4	0.5
0.5	0.5
0.7	0.6
0.4	0.5

$$RMSE = \sqrt{\frac{(0.2 - 0.2)^2 + (0.5 - 0.4)^2 + (0.5 - 0.5)^2 + (0.6 - 0.7)^2 + (0.5 - 0.4)^2}{5}} = 0.0775$$

# Leave-one-out Cross-validation

---

- Step 1: Given a full network, randomly hide one of the trust relations
- Step 2: Predict the existence of the hidden trust relation which has been suppressed
- Step 3: Repeat **Step 1** and **Step 2**  $n$  times
- Assume that the predictor infers these hidden relations correctly  $m$  of  $n$  times, then the accuracy is  $m/n$

# F-measure Evaluation

- Trust and not trust are treated as the positive and negative labels, respectively
- Precision, recall and F-measure are defined as

$$\text{precision} = \frac{tp}{tp + fp}$$

$$\text{recall} = \frac{tp}{tp + fn}$$

$$F1 = 2 \cdot \frac{\text{precision} \cdot \text{recall}}{\text{precision} + \text{recall}}$$

	p' (Predicted)	n' (Predicted)
P (Actual)	True Positive	False Negative
n (Actual)	False Positive	True Negative

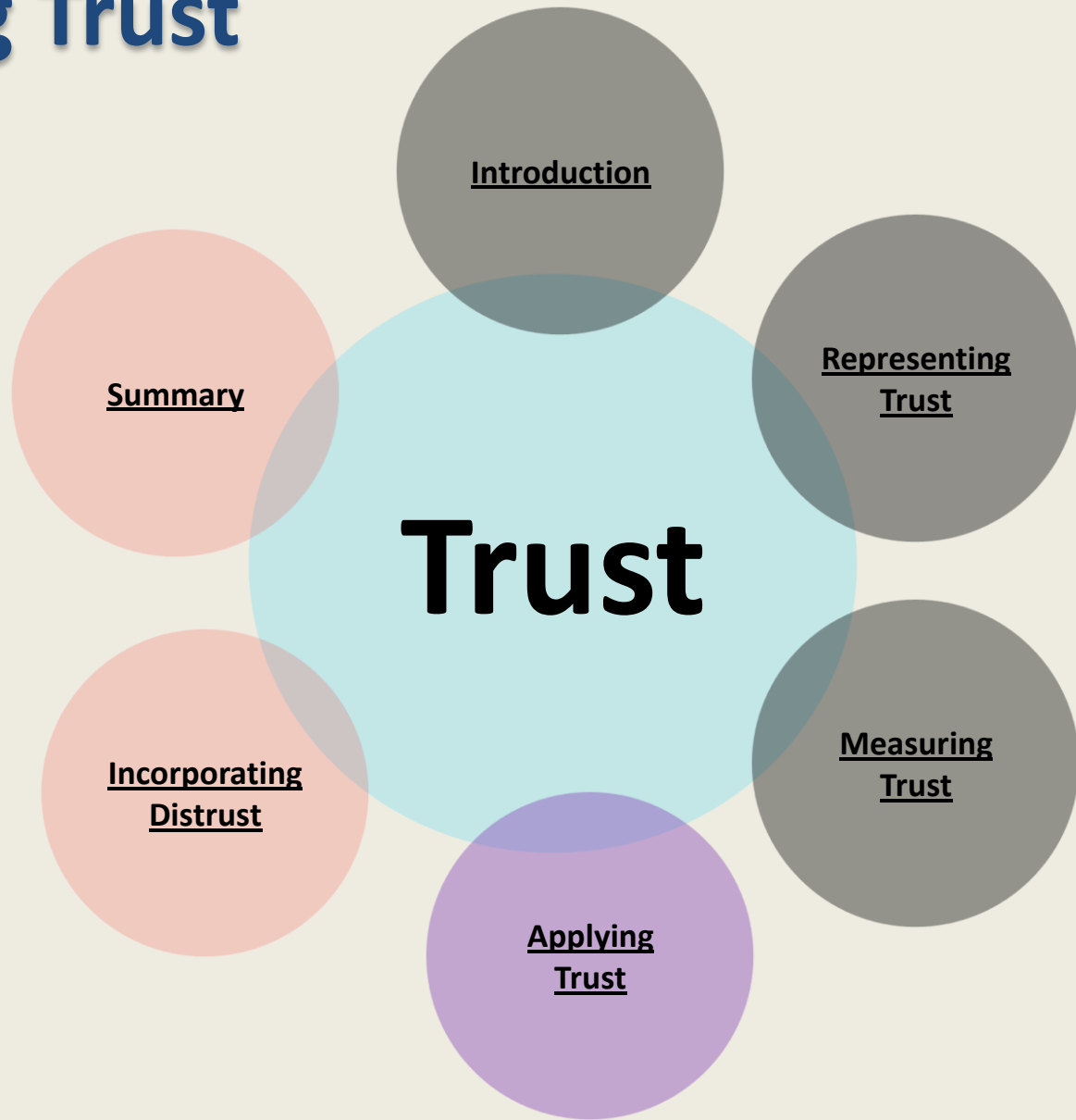


# Evaluation Metrics for Measuring Trust

---

- Ranking-based evaluation
  - Binary trust metrics
  - Unsupervised metrics
- RMSE evaluation
  - Continuous metrics
- Leave-one-out cross-validation evaluation
  - Supervised metrics
- F-measure evaluation
  - Supervised metrics

# Applying Trust



# Trust-aware Recommender Systems

---

- In this physical world, people seek recommendations from their trusted friends
- A user's preference is more likely to be similar to those of her trust network than to those of randomly chosen users
  - Trust information may provide preference context of a user
  - Homophily and influence
- Trust-aware recommender systems augment traditional recommender systems with trust information
  - User-item rating matrix  $\mathbf{R}$
  - User-user trust matrix  $\mathbf{T}$

# Traditional Recommender Systems

---

- Content-based recommender systems

- Recommend items similar to the ones that the user has preferred in the past

- Collaborative filtering (CF) -based recommender systems

- Using the user's past behavior to uncover user preferences and recommend items that match their preferences

- Only depending on users' past behaviors

- Memory-based CF and Model-based CF

# Memory-based Collaborative Filtering

---

- It uses either the whole user-item matrix or a sample to generate a prediction
  - Needing memory to store the user-item rating matrix  $R$
- User-oriented collaborative filtering
  - Calculating user-user similarity
  - Aggregating ratings from similar users
- Item-oriented collaborative filtering
  - Computing item-item similarity
  - Aggregating ratings from similar items

# An Illustration of User-oriented Collaborative Filtering

	A	B	C	D	E
1	5	3	4	?	?
2	?	3	4	4	?
3	1	?	2	2	5

2 and 3 are similar users to 1

A, B, C, D, and E are items

$R(1,D) = ?$

- Cosine similarity calculation

$$S(1,2) = \frac{3*3 + 4*4}{\sqrt{3*3 + 4*4} \sqrt{3*3 + 4*4}} = 1$$

$$S(1,3) = \frac{4*1 + 4*2}{\sqrt{1*1 + 2*2} \sqrt{4*4 + 4*4}} = 0.9487$$

- Aggregating ratings

$$R(1,D) = \frac{4*1 + 2*0.9487}{1 + 0.9487} = 3.03$$

# Model-based Collaborative Filtering

- It assumes a model to generate the ratings and learns the parameters of the model
  - Storing only parameters instead of the rating matrix
  - Using the assumed model with parameters to do prediction
- Matrix factorization methods are very competitive and are widely adopted to build recommender systems
  - $U_i$  is the  $k$ -dimensional user preference vector of user  $i$
  - $V_j$  is the  $k$ -dimensional item characteristic vector for item  $j$
  - A rating from user  $i$  to item  $j$  is modeled as

$$R_{ij} = U_i V_j^T$$

# An Illustration of Matrix Factorization based CF

	A	B	C	D	E
1	5	3	4	?	?
2	?	3	4	4	?
3	1	?	2	2	5

1,2 and 3 are users

A, B, C, D, and E are items

$R(1,D) = ?$

The latent dimension  $k = 1$

- Learning  $U$  and  $V$ , and reconstructing the rating matrix

$$\begin{array}{r}
 2.6308 \\
 U = 2.4109 \\
 1.4706
 \end{array}
 \quad
 \begin{array}{r}
 1.6252 \\
 1.2182 \\
 V = 1.5740 \\
 1.5990 \\
 2.5716
 \end{array}
 \quad
 \hat{R} = UV^T =
 \begin{array}{r}
 4.2756 \quad 3.2047 \quad 4.1408 \quad \boxed{4.2066} \quad 6.7654 \\
 3.9182 \quad 2.9368 \quad 3.7946 \quad 3.8550 \quad 6.1999 \\
 2.3901 \quad 1.7915 \quad 2.3147 \quad 2.3515 \quad 3.7819
 \end{array}$$

- $R(1,D)$  is predicted as 4.2066



# Challenges of Traditional Recommender Systems

---

- Data sparsity problem
  - Social media data is big data but the available data for most individuals is very limited
  - The user-item rating matrix is extremely sparse with less than 1% observed ratings
- Cold-start problem
  - The number of ratings for users follows a power-law distribution
  - There are many users with no or very few ratings
  - Existing recommender systems may fail to make recommendations for cold-start users

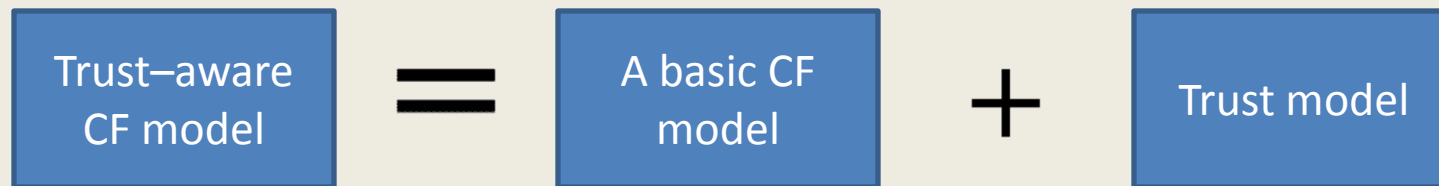
# Opportunities from Trust Information

---

- Trust provides an additional source for recommendation improvement
  - Overlap between one's similar users and trusted users is low (less than 10%)
  - Mitigating data sparsity problem
- Since a user has her trust network, we can do recommendation based on her trusted users
  - Users' preferences are similar to their trust networks
  - Reducing significantly the number of cold-start users

# Categorization [Tang et al., 2013]

- Most existing trust-aware recommender systems are CF-based methods



- We can categorize existing trust-aware systems based on their basic CF models
  - Memory-based trust-aware recommender systems
  - Model-based trust-aware recommender systems

# Memory-based Trust-aware Recommendation

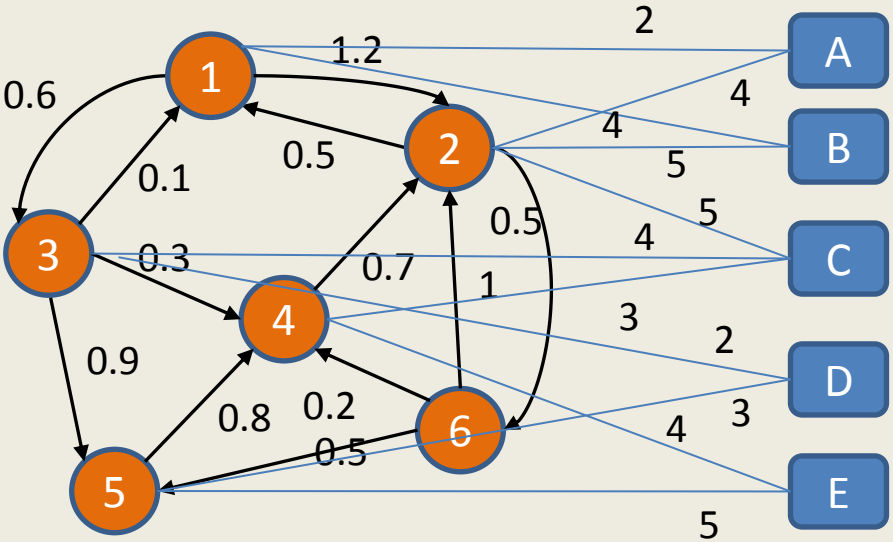
- It uses memory-based CF methods, especially user-oriented methods, as basic models
- It usually consists of two steps
  - Step 1: obtaining the trusted users  $N_i$  for a given user  $i$ ,
  - Step 2: aggregating ratings from the trusted users obtained by the first step to predict ratings for user  $i$
- Step 2 is the same as that in traditional memory-based methods, and different methods in this category provide different ways to obtain trusted users in Step 1

# TidalTrust vs MoleTrust

- TidalTrust only considers raters at the shortest distance
  - Trusted users  $N_i$  is the set of users at the shortest distance
  - Efficient
  - High precision
  - Low recall
- MoleTrust considers raters up to a maximum-depth  $d$ 
  - Trusted users  $N_i$  is the set of users within maximum-depth
  - Trade-off between precision and recall

$$\hat{\mathbf{R}}_{ij} = \bar{\mathbf{R}}_i + \frac{\sum_{u_k \in \mathcal{N}_i} \mathbf{S}_{ik} (\mathbf{R}_{kj} - \bar{\mathbf{R}}_k)}{\sum_{u_k \in \mathcal{N}_i} \mathbf{S}_{ik}}$$

# An Illustration of MoleTrust for Recommendation



$$T = \begin{bmatrix} 0 & 1.2 & 0.6 & 0 & 0 & 0 \\ 0.5 & 0 & 0 & 0 & 0 & 0.5 \\ 0.1 & 0 & 0 & 0.3 & 0.9 & 0 \\ 0 & 0.7 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0.8 & 0 & 0 \\ 0 & 1 & 0 & 0.2 & 0.5 & 0 \end{bmatrix}$$

$$R = \begin{bmatrix} 2 & 4 & ? & ? & ? \\ 4 & 5 & 5 & ? & ? \\ ? & ? & 4 & 2 & ? \\ ? & ? & 3 & ? & 4 \\ ? & ? & ? & 3 & 5 \\ ? & ? & ? & ? & ? \end{bmatrix}$$

Setting  $d = 2$  and predicting  $R(6,E) = ?$

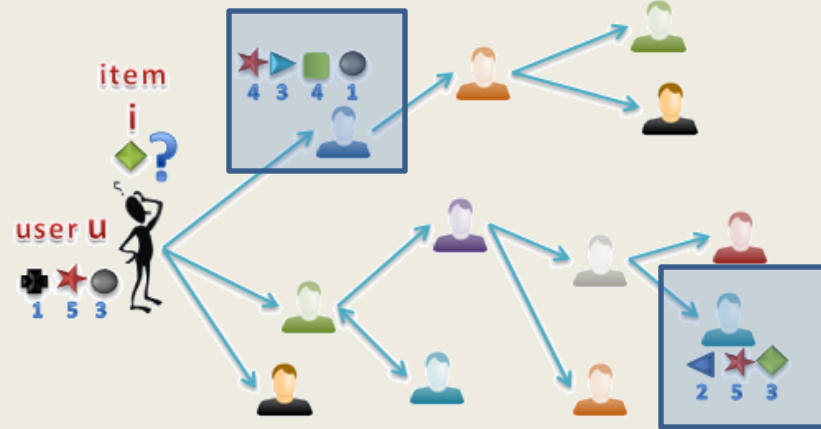
- The set of raters in the paths with length of 2 is  $\{5, 4, 2, 1\}$
- Only  $\{5,4\}$  rate item E

$$R(6, E) = \frac{T_{65}R(5, E) + T_{64}R(4, E)}{T_{65} + T_{64}} = \frac{0.5 * 5 + 0.2 * 4}{0.5 + 0.2} = 4.714$$

User 6 does not have any ratings and MoleTrust can do recommendations based on her trust network

# TrustWalker [Jamali and Ester, 2009]

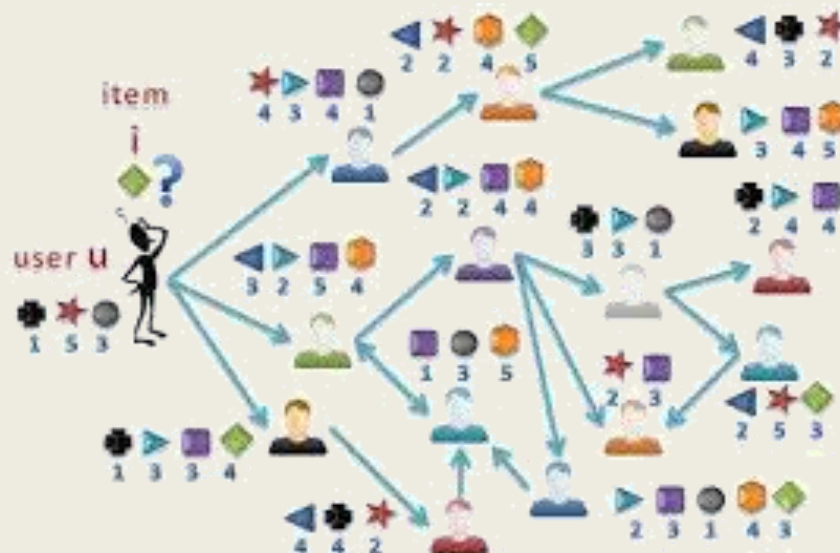
- Instead of distant neighbors who have rated the target item, it uses near neighbors who have rated similar items
  - Trusted friends on similar items
  - Distant users on the exact target item



- It combines item-based recommendation and trust-based recommendation via random walk
- Each random walk returns a rating of the target item or a similar item

# TrustWalker

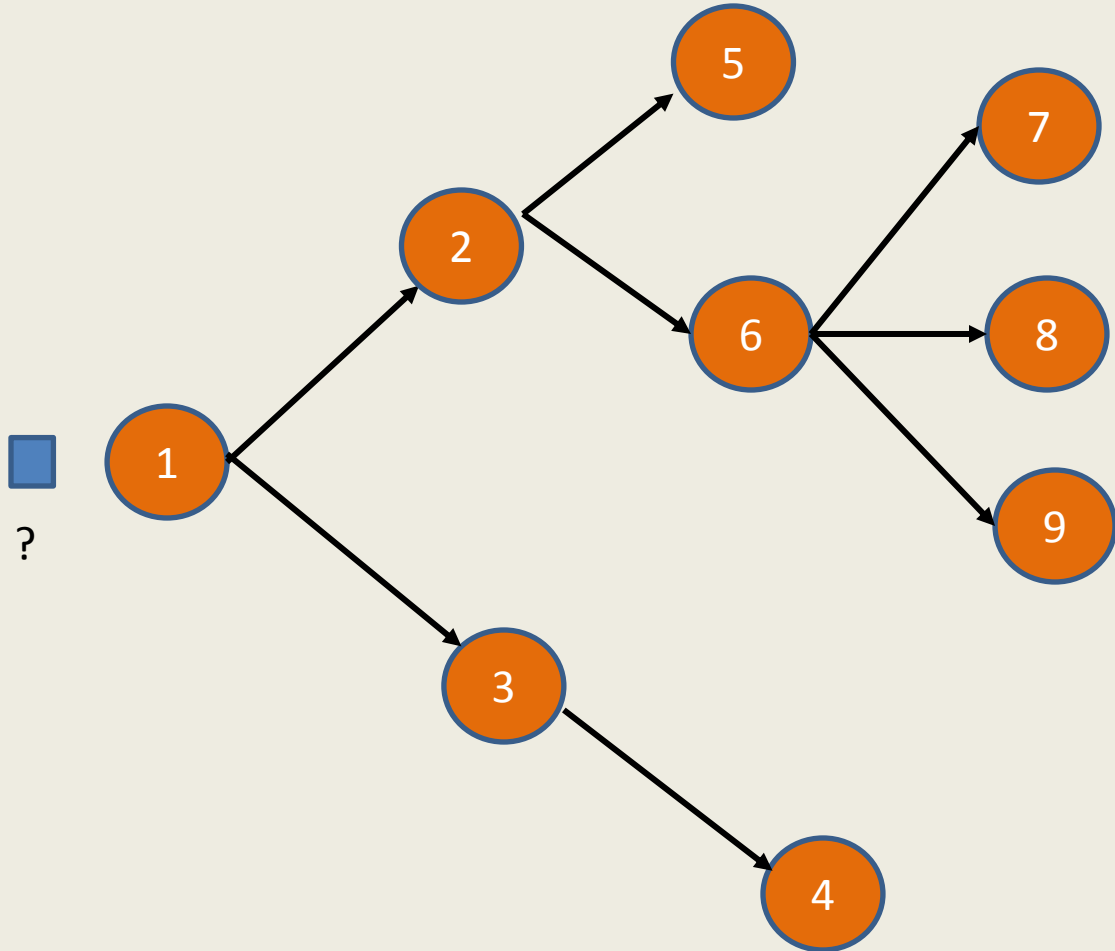
- Each random walk starts from a target user  $u$  to seek rating score for item  $i$



- In step  $k$  at node  $v$ :
  - If  $u$  has rated  $i$ , return  $R_{vi}$
  - With the probability  $\phi_{v,i,k}$ , stop random walk, select a similar item  $j$  rated by  $u$  and return  $R_{vj}$
  - With the probability  $1 - \phi_{v,i,k}$ , continue the random walk to a direct neighbor of  $v$

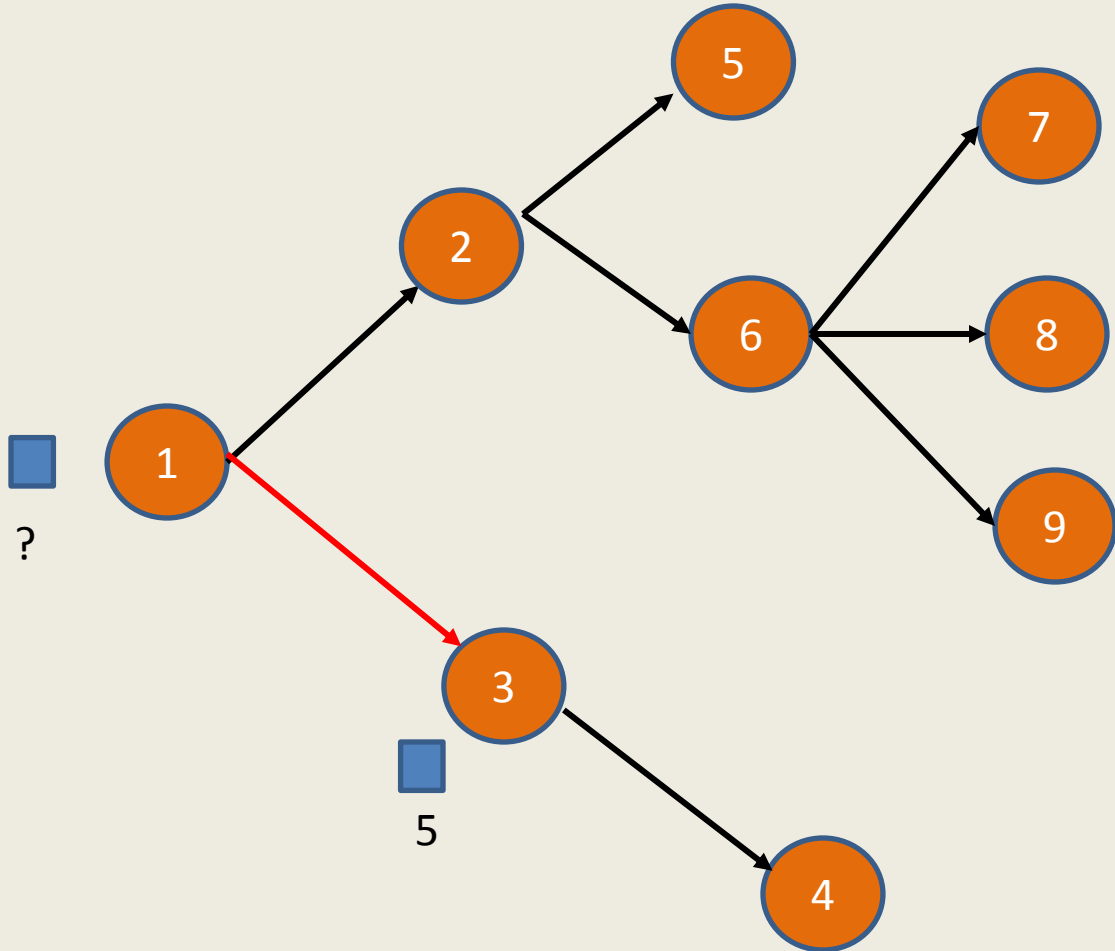


# An illustration of TrustWalker



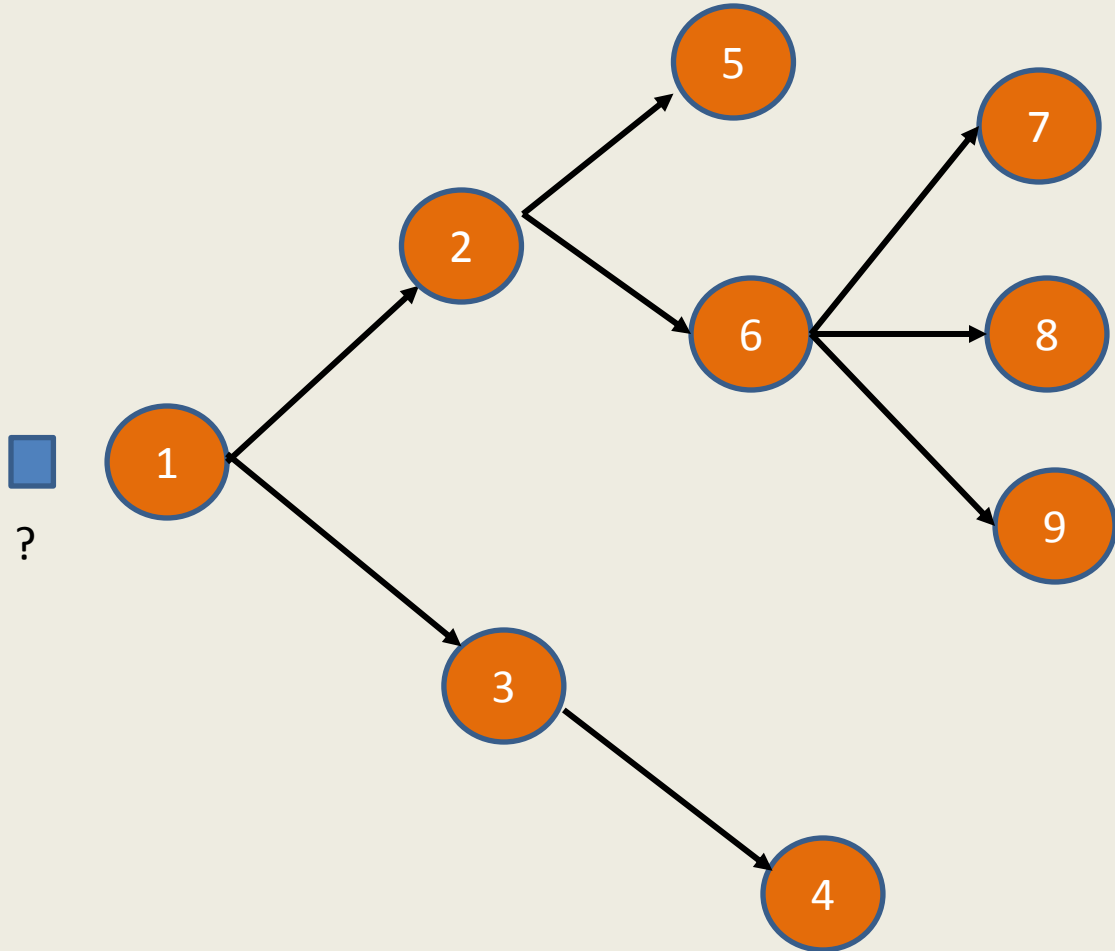
# An illustration of TrustWalker

R1=5



# An illustration of TrustWalker

R1=5

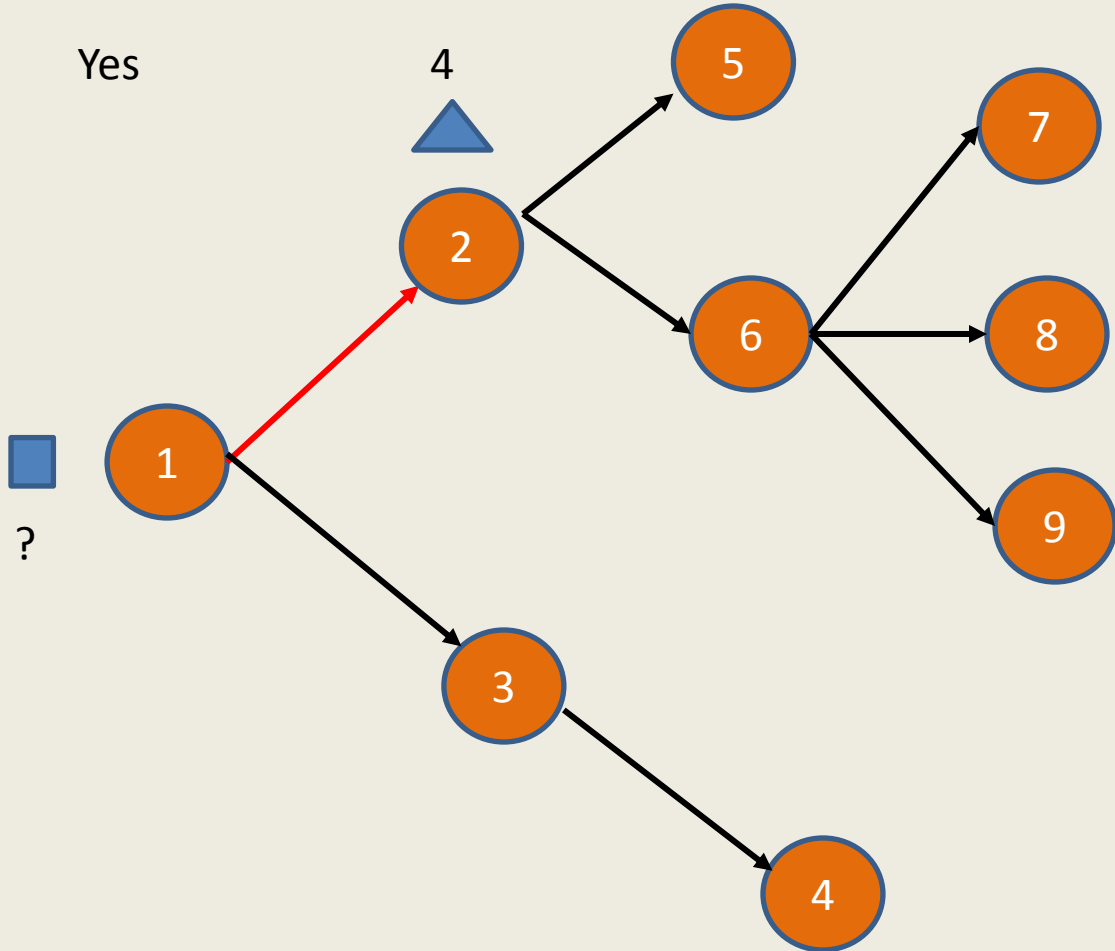


# An illustration of TrustWalker

Continue?

R1=5

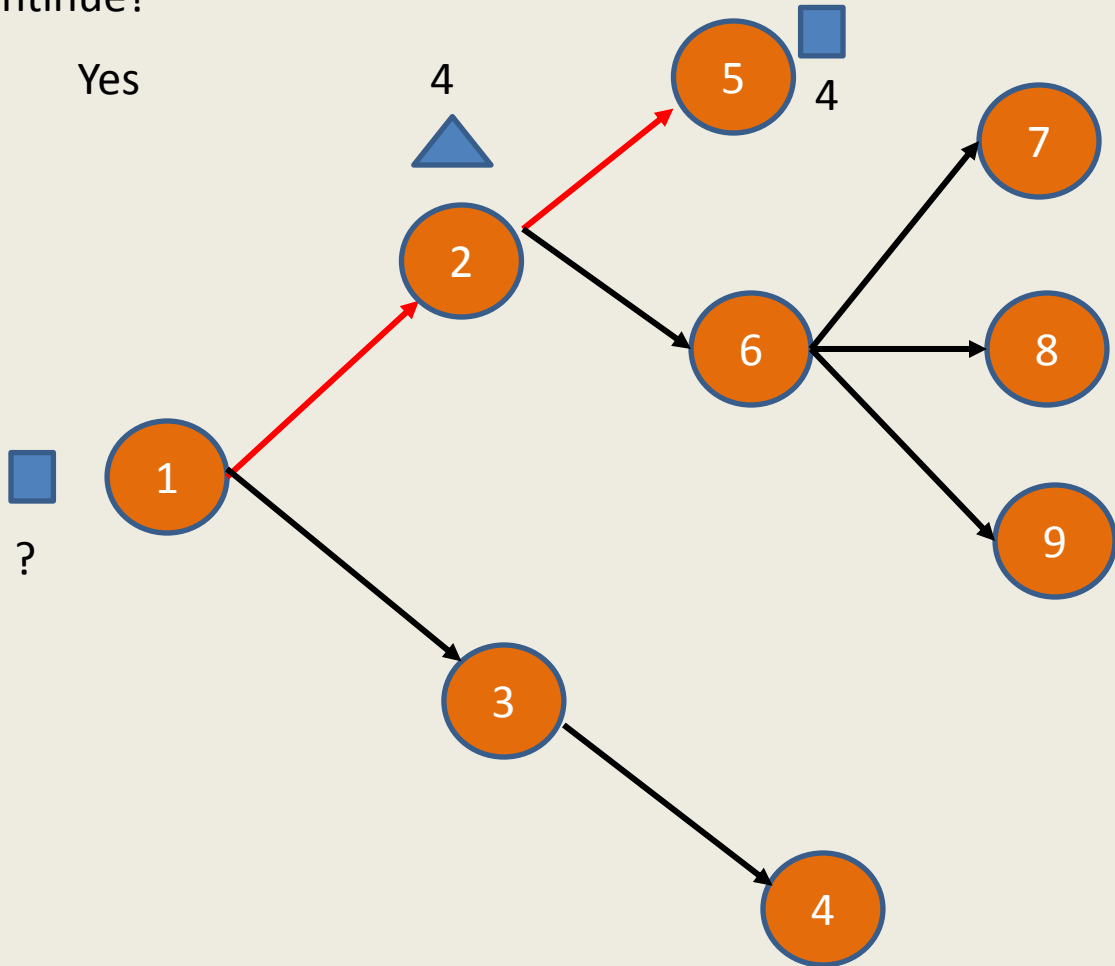
Yes



# An illustration of TrustWalker

Continue?

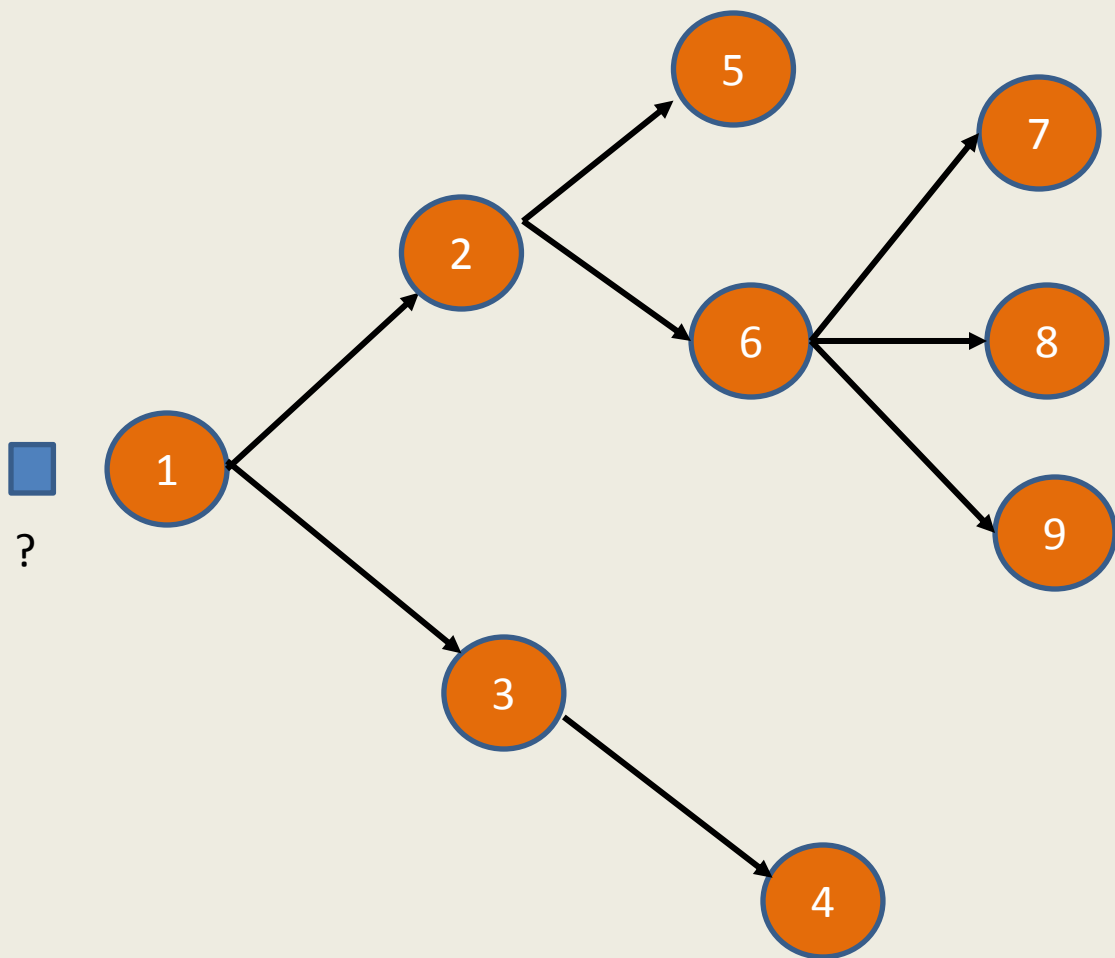
Yes



R1=5

R2=4

# An illustration of TrustWalker



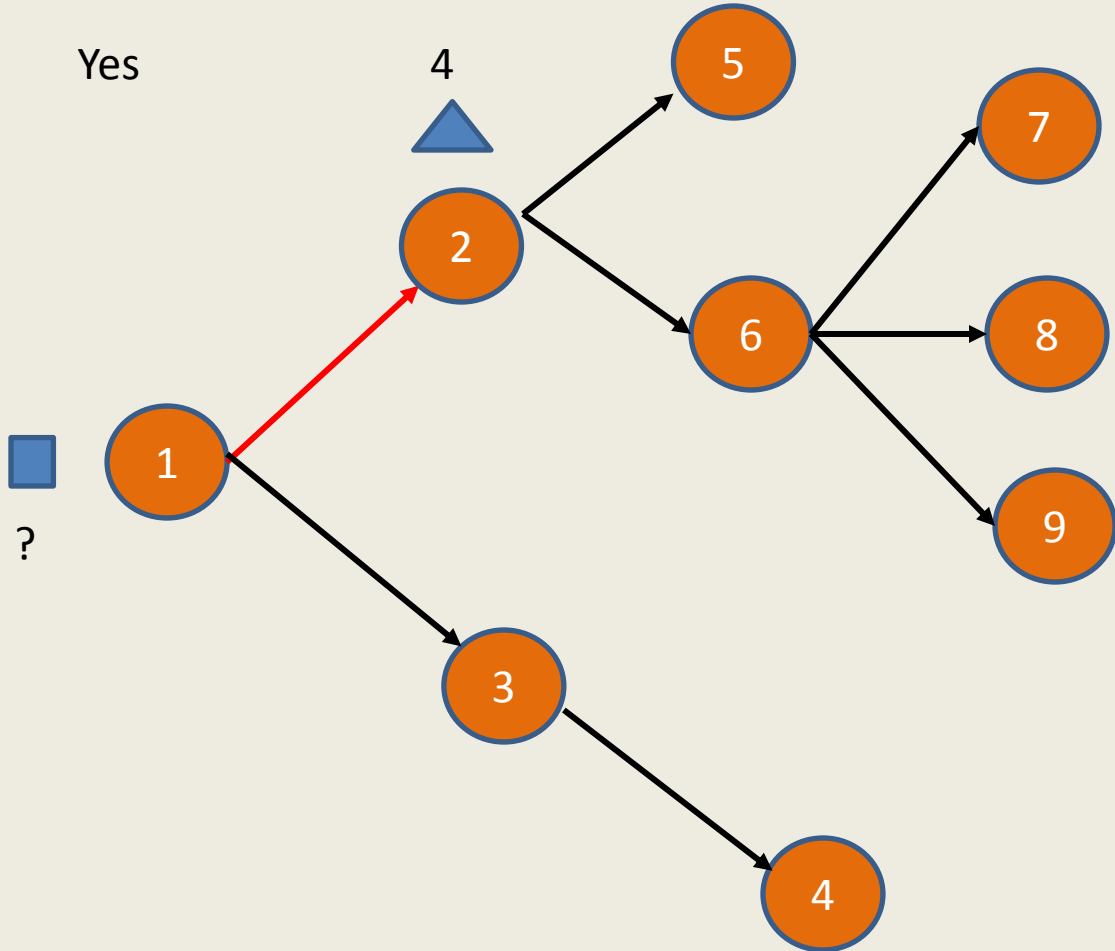
R1=5

R2=4

# An illustration of TrustWalker

Continue?

Yes



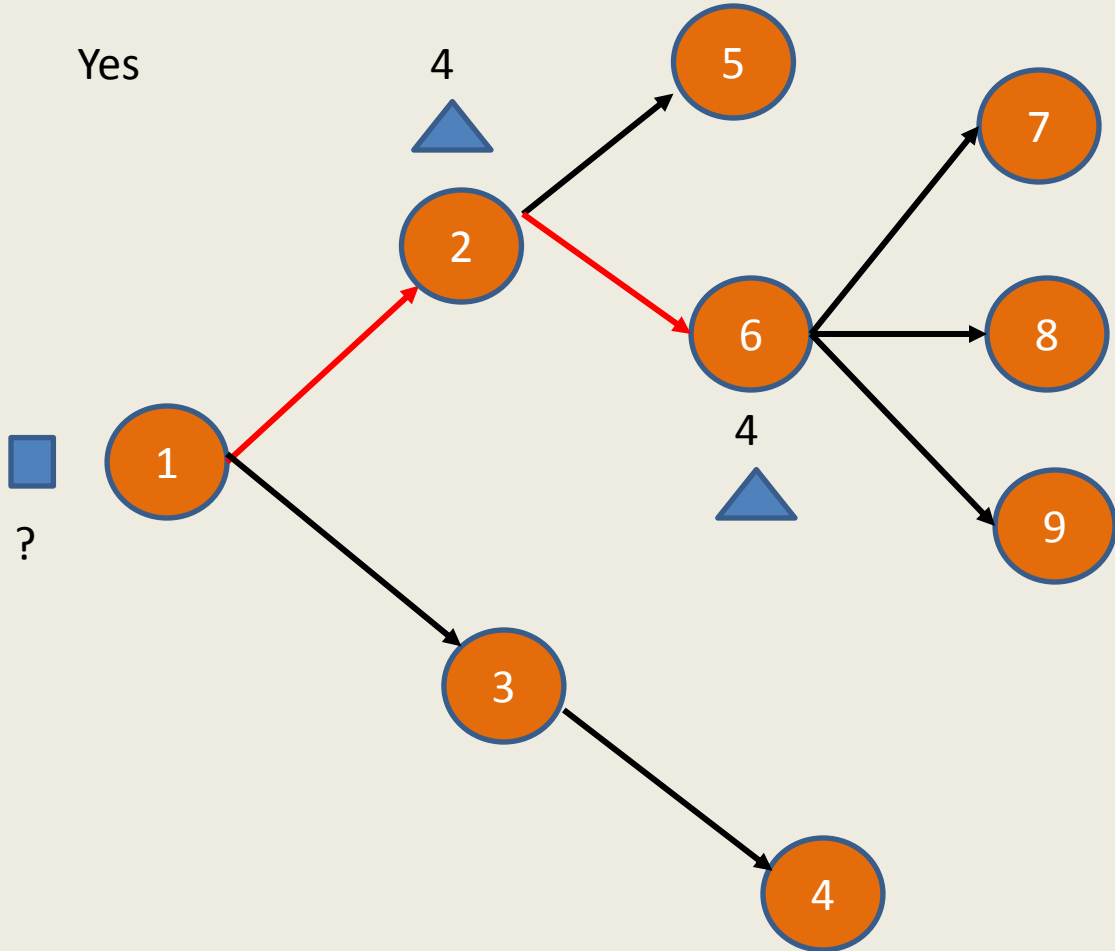
R1=5

R2=4

# An illustration of TrustWalker

Continue?

Yes



R1=5

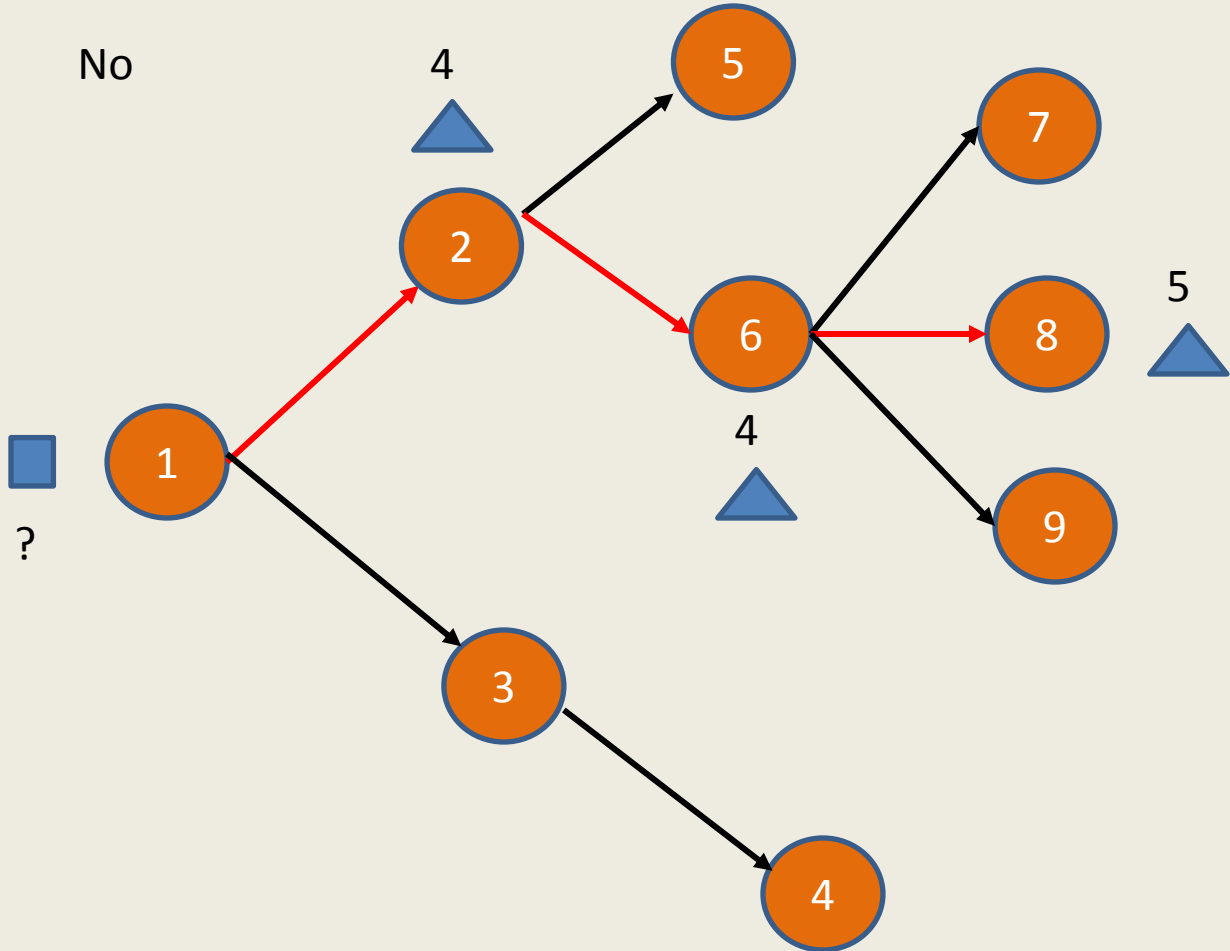
R2=4



# An illustration of TrustWalker

Continue?

No

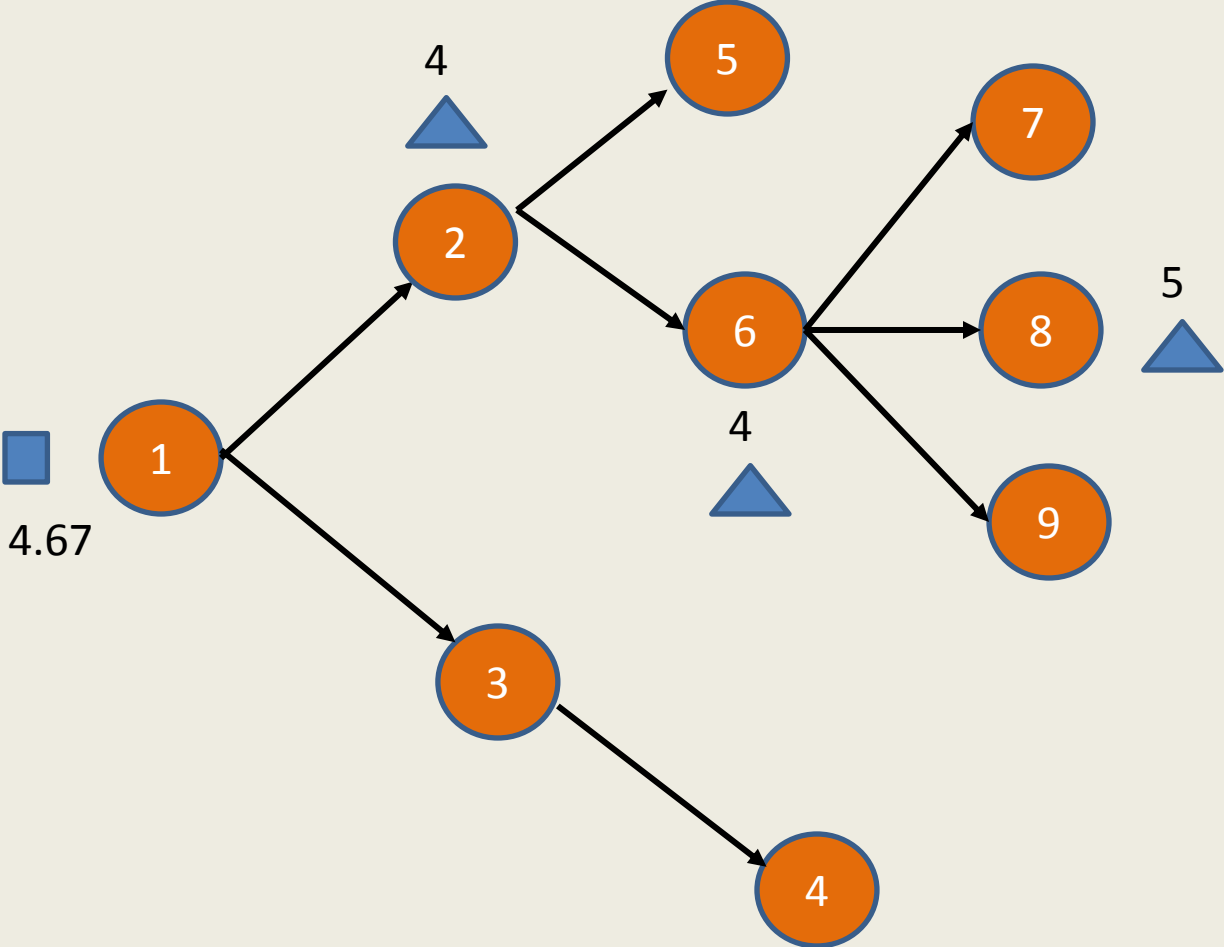


R1=5

R2=4

R3=5

# An illustration of TrustWalker



R1=5

R2=4

R3=5

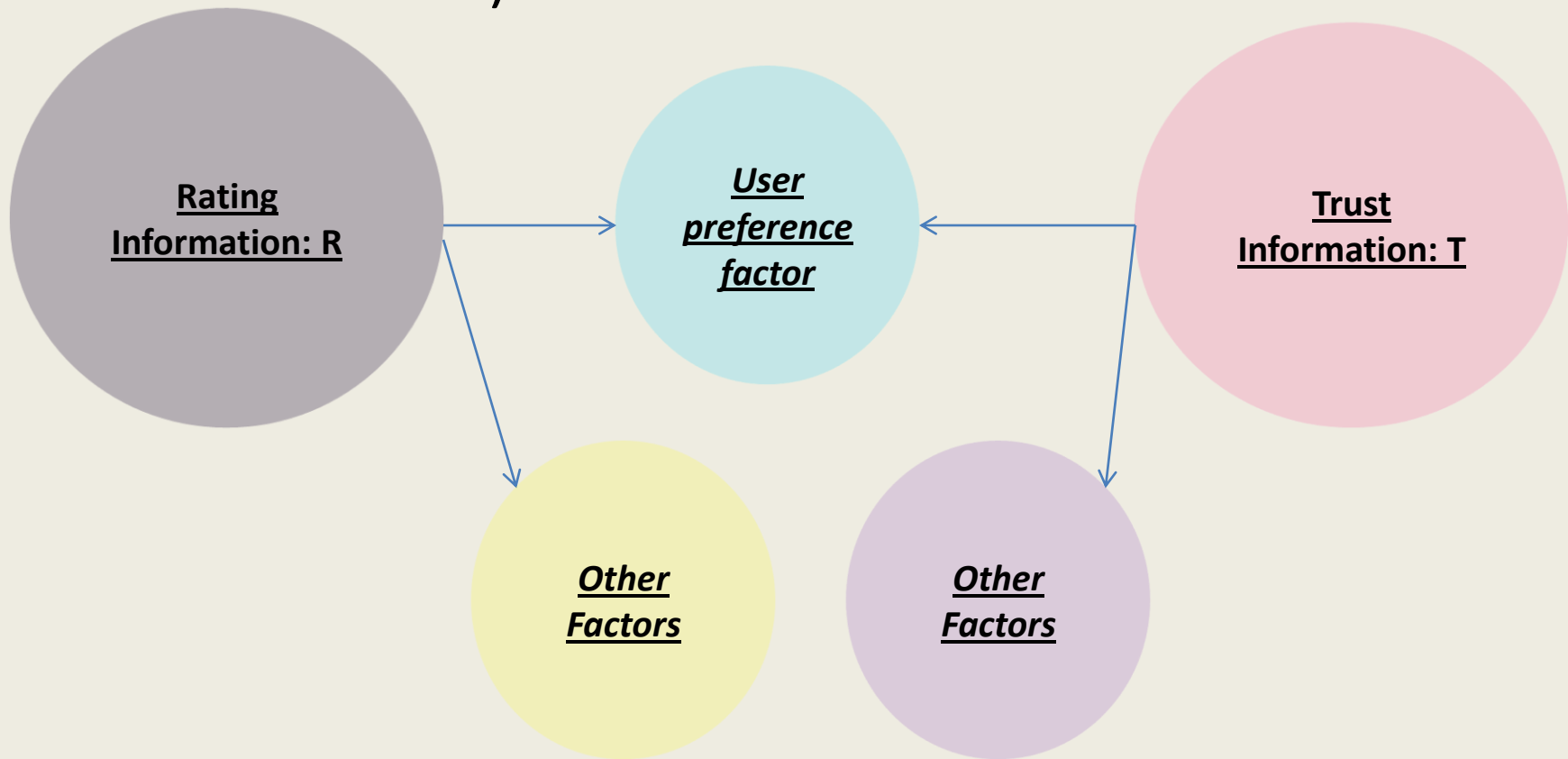
# Model-based Trust-aware Recommendation

---

- Model-based trust-aware recommender systems choose model-based CF methods as their basic models
  - Matrix factorization is widely chosen as the basic model
  
- There are three common ways to integrate trust information under the matrix factorization framework
  - Co-factorization methods
  - Ensemble methods
  - Regularization methods

# Co-factorization Methods

A user shares the same user preference factor in the rating space (rating information) and the social space (social information)

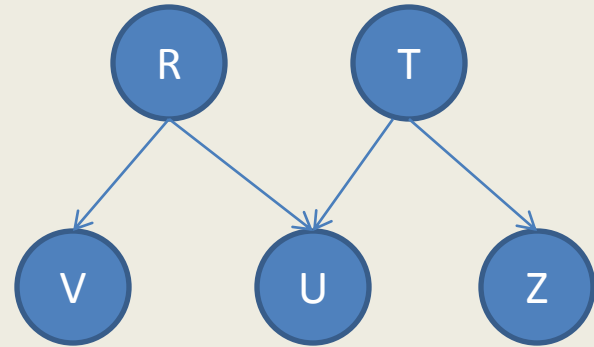


# Representative Systems

- SoRec [Ma et al., 2008]

$$R_{ij} = U_i V_j^T$$

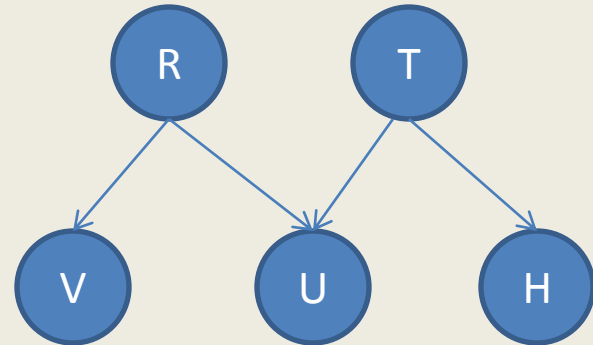
$$T_{ij} = U_i Z_j^T$$



- LOCABAL [Tang et al., 2013]

$$R_{ij} = U_i V_j^T$$

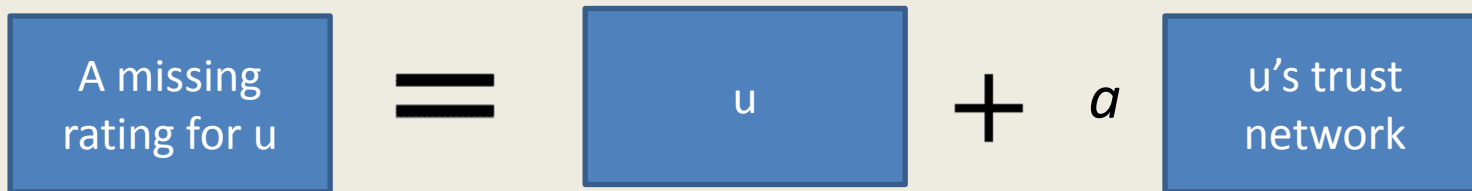
$$T_{ij} = U_i H U_j^T$$



Co-factorization methods can jointly predict missing ratings and trust relations.

# Ensemble Methods

- Users and their social networks should have similar ratings on items
- A missing rating for a given user is predicted as a combination of ratings from the user and her trust network



# Representative Systems

- STE - Ensemble of predicted ratings [Ma et al., 2009a]

$$R_{ij} = U_i V_j^T + \alpha \sum_{u_k \in N(u_i)} T_{ik} U_k V_j^T$$

- mTrust – Ensemble of predicted ratings and observed ratings from her trust network [Tang et al., 2012]

$$R_{ij} = U_i V_j^T + \alpha \frac{\sum_{u_k \in N(u_i)} T_{ik} R_{jk}}{\sum_{u_k \in N(u_i)} T_{ik}}$$

-  $T_{ik}$  is the trust strength between the i-th user and k-th user

# Regularization Methods

- Regularization methods focus on a user's preference and assume that a user's preference should be similar to that of her social network.
- Regularization methods add a regularization term to force users' preferences to be close to those of trust networks.





# Representative systems

- SocialMF – a user's preference should be close to that of her social network [Jamali and Ester, 2010]

$$\min \sum_i \left\| U_i - \sum_{u_k \in N(u_i)} T_{ik} U_k \right\|$$

- SoReg – two connected users should have similar preferences [Ma et al., 2011]

$$\min \sum_i \sum_{u_k \in N(u_i)} T_{ik} \left\| U_i - U_k \right\|$$

# Prediction Accuracy Evaluation

- Root Mean Squared Error (RMSE)

$$RMSE = \sqrt{\frac{\sum_{\langle u_i, v_j \rangle \in O} (\hat{R}_{ij} - R_{ij})^2}{|O|}}$$

- Mean Absolution Error (MAE)

$$MAE = \frac{\sum_{\langle u_i, v_j \rangle \in O} |\hat{R}_{ij} - R_{ij}|}{|O|}$$

– Small improvement in RMSE or MAE terms can have a significant impact on the quality of the top-few recommendation [Koren, 2008]

# Ranking Accuracy Evaluation

---

## ■ Recall

- How many of acquired items were recommended
- Recall@N: how many top-N acquired items are recommended

## ■ Precision

- How many recommended items are acquired
- Precision@N: how many top-N recommended items are acquired

Long recommendation lists typically improve recall while reducing precision

# Coverage Evaluation

---

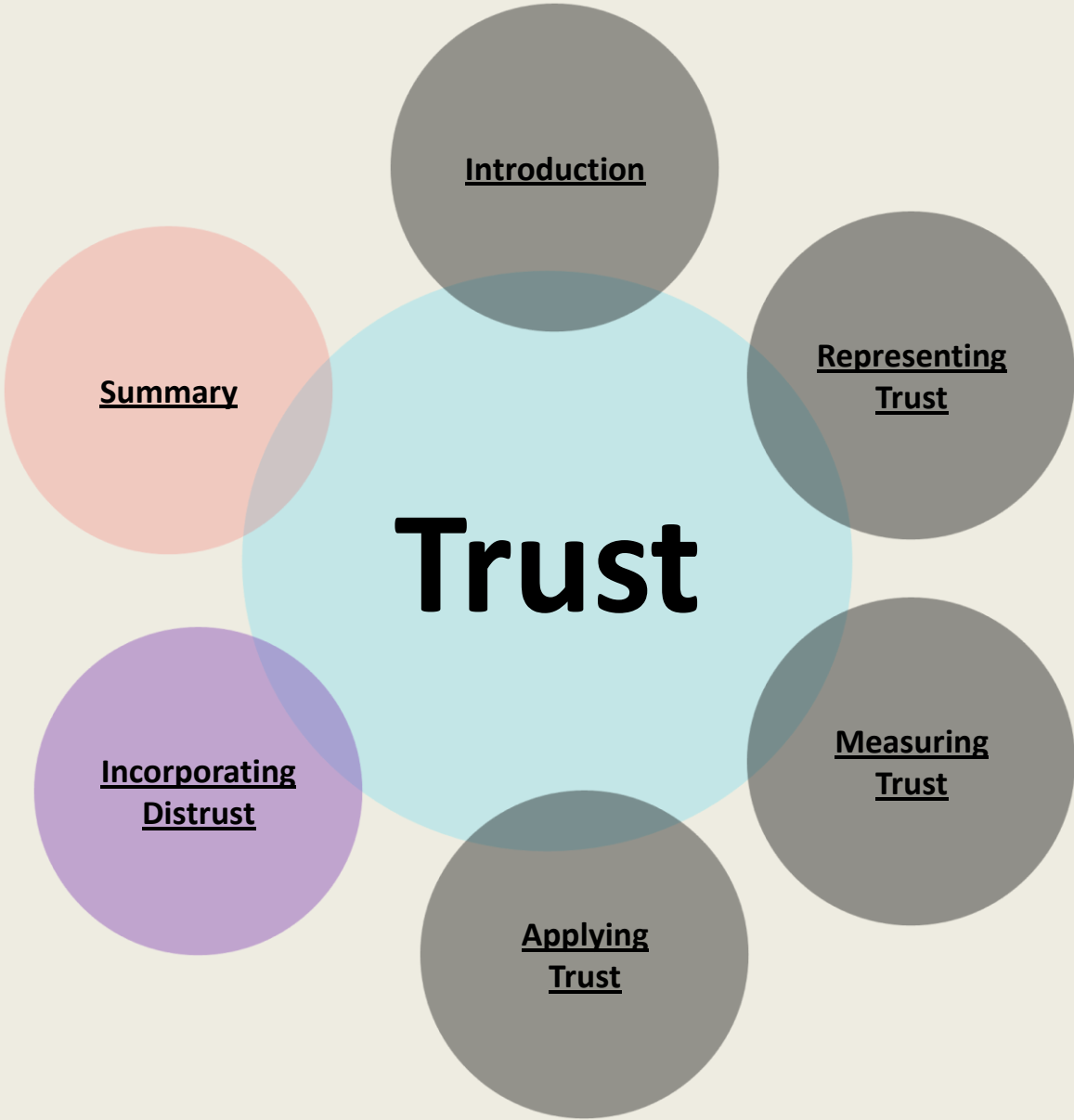
- **Item coverage**

- The proportion of items that the recommendation system can recommend

- **User coverage**

- The proportion of items that the recommendation system can recommend

# Incorporating Distrust



# Distrust in Social Sciences

---

- Distrust can be as important as trust
- Both trust and distrust help a decision maker reduce the uncertainty and vulnerability associated with decision consequences
- Distrust may exert an equally important, if not more, critical role as trust in consumer decisions

# Understandings of Distrust from Social Sciences

---

- Distrust is the negation of trust [Jøsang et al.,2003]
  - Low trust is equivalent to high distrust
  - The absence of distrust means high trust
  - Lack of the studying of distrust matters little
- Distrust is a new dimension of trust [Lewicki et al., 1998]
  - Trust and distrust are two separate concepts
  - Trust and distrust can co-exist
  - A study ignoring distrust would yield an incomplete estimate of the effect of trust

# Distrust in Social Media

---

- Distrust is rarely studied in social media
  - Social media data is based on passive observations
  - Lack of some information social sciences use to study distrust
  - Lack of computational understanding of distrust with social media data
  
- Let us first examine the properties of distrust before going to the computational understanding of distrust



# Examining Properties of Distrust

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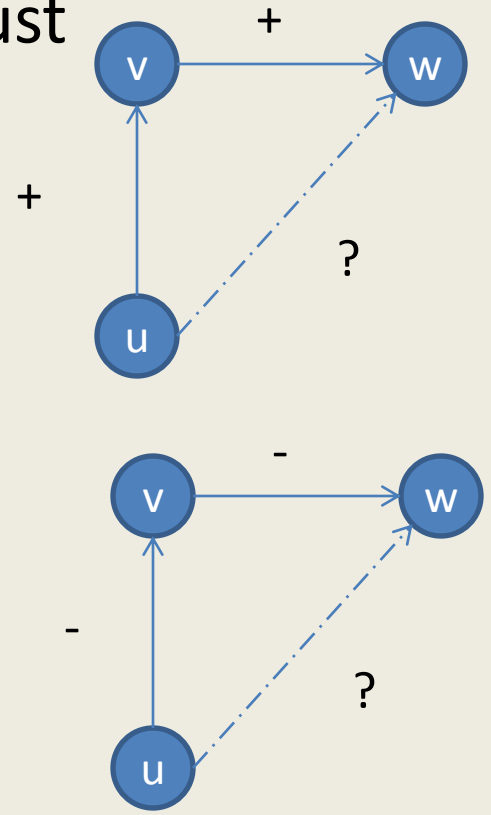
- Properties of trust are systematically and extensively studied
  - Transitivity, asymmetry, and homophily
- Properties of distrust are rarely studied with social media data
- Can we simply or conversely extend the properties of trust to those of distrust ?
  - We study the properties of distrust in parallel to those of trust

# Transitivity [Tang and Liu, 2014]

- Trust is transitive (1<sup>st</sup> table); how about distrust?
- For distrust (2<sup>nd</sup> table), #u+w is comparable to #u-w
- Transitivity may not be applicable to distrust

Trust		
Types	Number	Percentage
$\langle u+v, v+w \rangle, u+w$	3,320,991	97.75%
$\langle u+v, v+w \rangle, u-w$	76,613	2.25%

Distrust		
Types	Number	Percentage
$\langle u-v, v-w \rangle, u+w$	38,729	59.73%
$\langle u-v, v-w \rangle, u-w$	26,114	40.27%



u+v and u-v represent trust and distrust relations between u and v, respectively

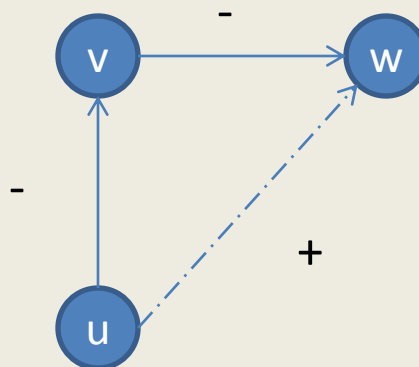
# Understanding (-,-,+) and (-,-,-) [Guha et al., 2004]

- User u disagrees with the statement of user v

–  $\langle u-v, v-w \rangle \rightarrow \langle u+w \rangle$

– My enemy's enemy is my friend

– Structural balance

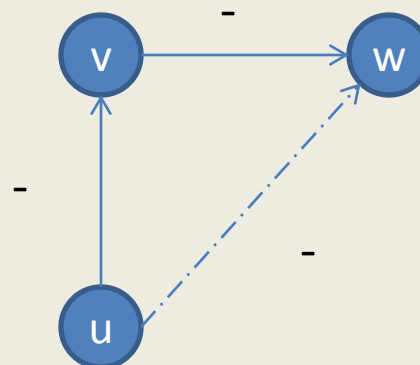


- User u thinks user v's judgments are inferior to her own

–  $\langle u-v, v-w \rangle \rightarrow \langle u-w \rangle$

– Status theory

- So, it is more complicated than it appears and further research is needed



# Asymmetry [Tang and Liu, 2014]

- Trust is asymmetric
  - 37.61% of relations are mutual-trust
  - Hence,  $u+v$  is not equivalent to  $v+u$ , or  $v+u \neq u+v$
- Distrust is even more skewed
  - Only 5.86% of relations are mutual-distrust
  - That is, we are more confident that  $v-u \neq u-v$

	$v+u(\%)$	$v-u(\%)$	$v?u(\%)$
$u+v$	136,806(37.61)	967(0.27)	226,000(62.13)
$u-v$	967(2.09)	2,623(5.86)	42,606(92.23)

# Homophily [Tang and Liu, 2014]

- Users with distrust relations are more likely to be similar than two randomly chosen users

	CI	COSINE	COSINE-CI
Distrust ( $s_d$ )	0.4994	0.0105	0.0142
Trust $s_t$	0.6792	0.0157	0.0166
Random Pairs ( $s_r$ )	0.1247	0.0027	0.0032
P1	9.57e-87	1.19e-120	4.88e-45
P2	1.71e-132	5.83e-157	3.72e-108
P3	7.84e-23	1.99e-19	9.32e-17

CI: Commonly-rated Items

COSINE: Rating-cosine similarity

COSINE-CI: Rating-cosine similarity of commonly rated items

P1- P-values:  $H_0: s_d \leq s_r$ ;  $H_1: s_d > s_r$

P2- P-values:  $H_0: s_t \leq s_r$ ;  $H_1: s_t > s_r$

P3- P-values:  $H_0: s_t \leq s_d$ ;  $H_1: s_t > s_d$

- Distrust is not a dissimilarity measurement

# Computational Understanding of Distrust

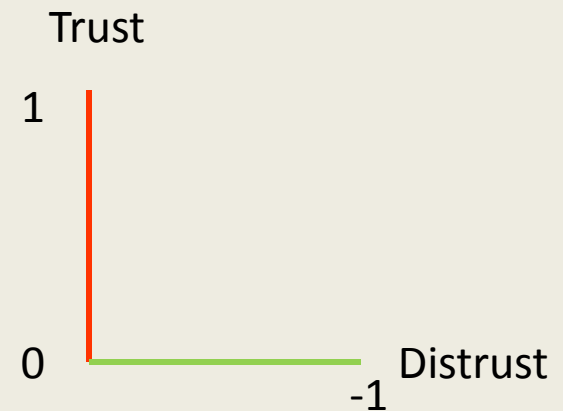
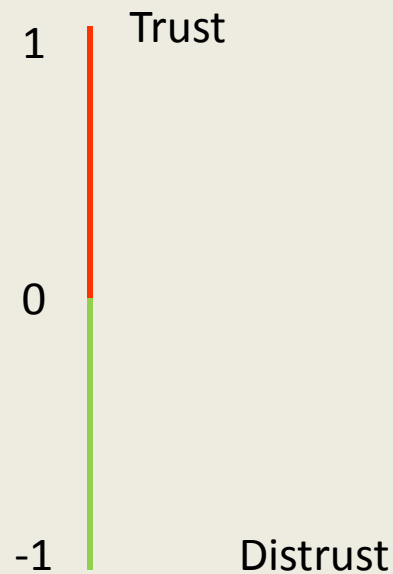
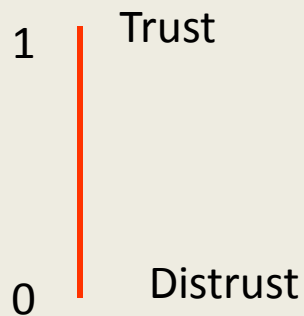
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- We leverage machine learning and data mining techniques to design computational tasks to help us understand distrust with passively observed social media data
- **Task 1:** Is distrust the negation of trust?
  - If distrust is the negation of trust, distrust should be predictable from only trust
- **Task 2:** Can we predict trust better with distrust?
  - If distrust is a new dimension of trust, distrust should have added value on trust and can improve trust prediction
- The first step to understand distrust is to make distrust computable by incorporating distrust in trust models

# Distrust in Trust Representations

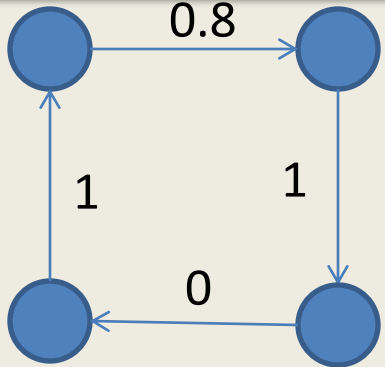
There are three major ways to incorporate distrust in trust representation

- Considering low trust as distrust
- Extending negative values in trust representations
- Adding a dimension in trust representations

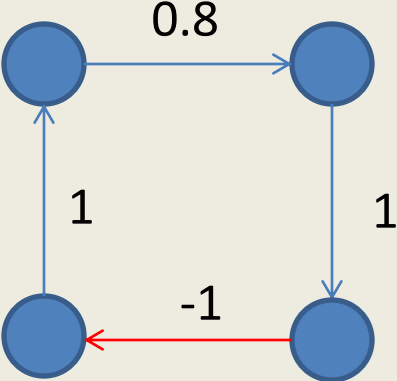


# A Network Illustration of Distrust in Trust Representations

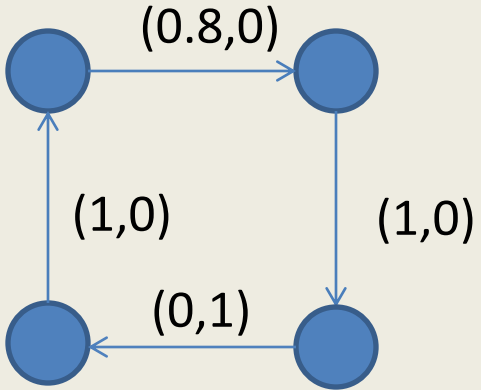
- Considering low trust as distrust
  - Weighted unsigned network



- Extending negative values in trust representations
  - Weighted signed network



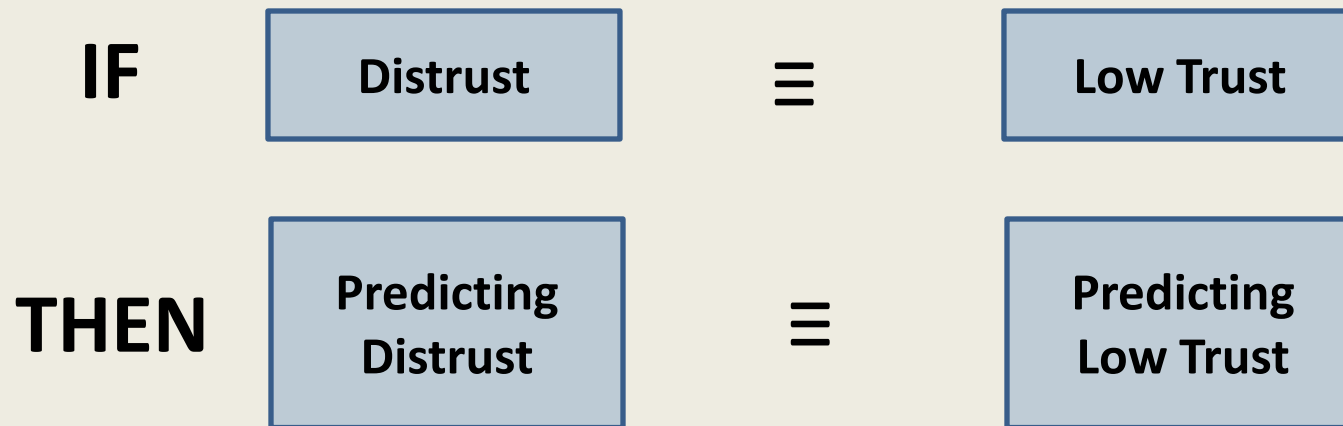
- Adding a dimension in trust representations
  - Two-dimensional unsigned network





# Task 1: Is Distrust the Negation of Trust?

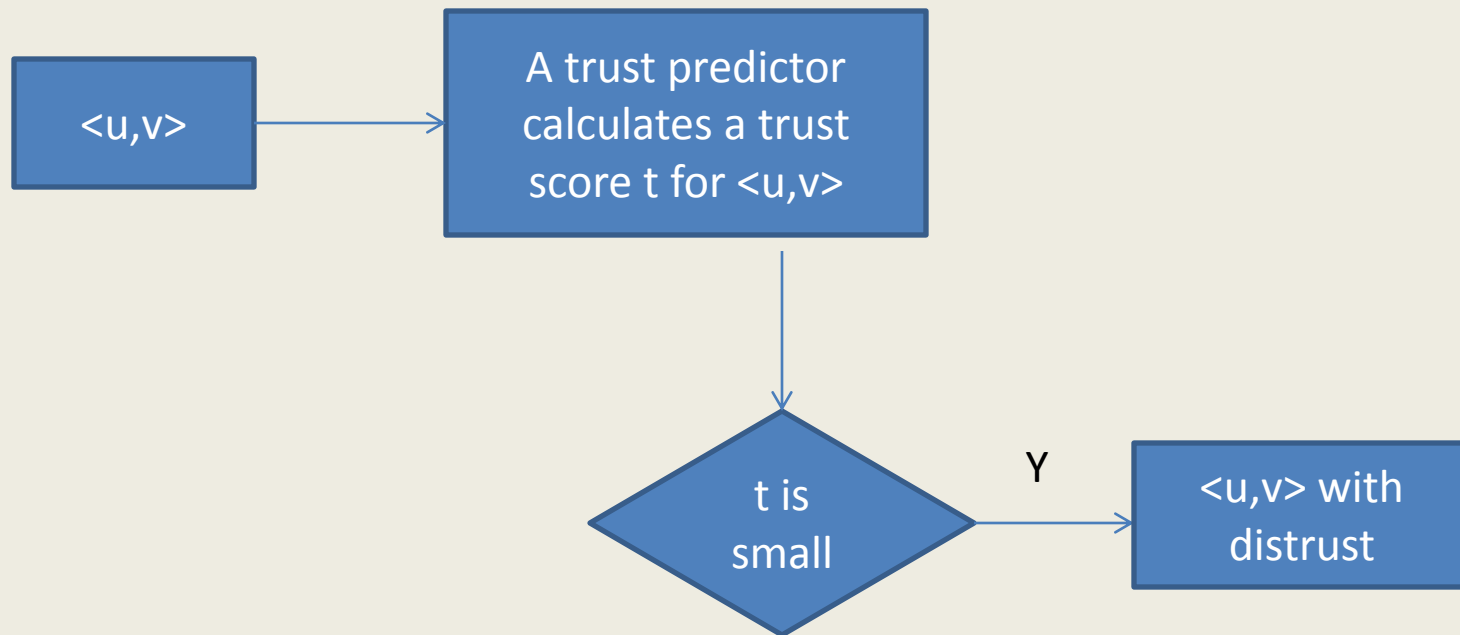
- If distrust is the negation of trust, low trust is equivalent to distrust and distrust should be predictable from trust



- Given the transitivity of trust, we resort to trust prediction algorithms to compute trust scores for pairs of users in the same trust network

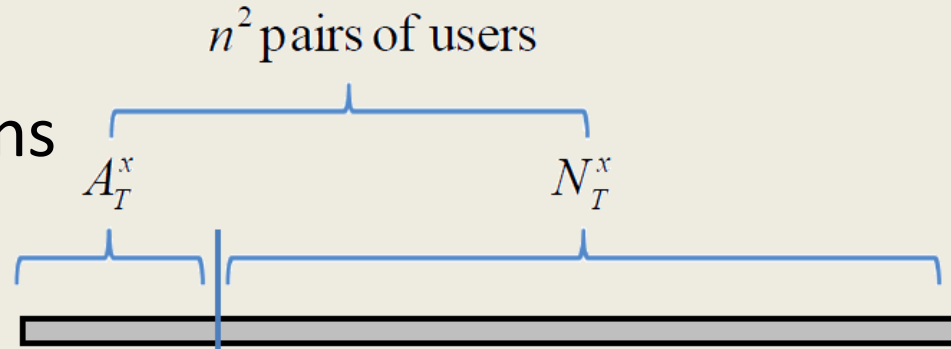
# Algorithm for Task 1

- A trust predictor is chosen to calculate trust scores for pairs of users without trust relations
- Pairs of users with low trust scores are suggested as distrust



# Experimental Settings for Task 1

- Each time we choose  $x\%$  of pairs of users with trust relations as  $A_T^x$



- Through Task 1 with  $A_T^x$ , we predict  $|D|$  pairs of users with low trust  $P$  from  $N_T^x$  as distrust
  - $D$  is the set of pairs with distrust as ground truth in the data set

- The performance is computed as

$$PA = \frac{|D \cap P|}{|D|}$$

# Evaluation of Task 1

- The performance of using low trust to predict distrust is consistently worse than randomly guessing
- Task 1 fails to predict distrust with only trust and distrust is not the negation of trust

x (%)	dTP ( $\times 10^{-5}$ )	dMF ( $\times 10^{-5}$ )	dTP-MF ( $\times 10^{-5}$ )	Random ( $\times 10^{-5}$ )
50	4.8941	4.8941	4.8941	5.6824
55	5.6236	5.6236	5.6236	8.1182
60	7.1885	7.1885	7.1885	15.814
65	11.985	11.985	11.985	19.717
70	13.532	13.532	13.532	18.826
80	10.844	10.844	10.844	16.266
90	12.720	12.720	12.720	25.457
100	14.237	14.237	14.237	29.904

dTP: It uses trust propagation to calculate trust scores for pairs of users

dMF: It uses the matrix factorization based predictor to compute trust scores for pairs of users

dTP-MF: It is the combination of dTP and dMF using OR

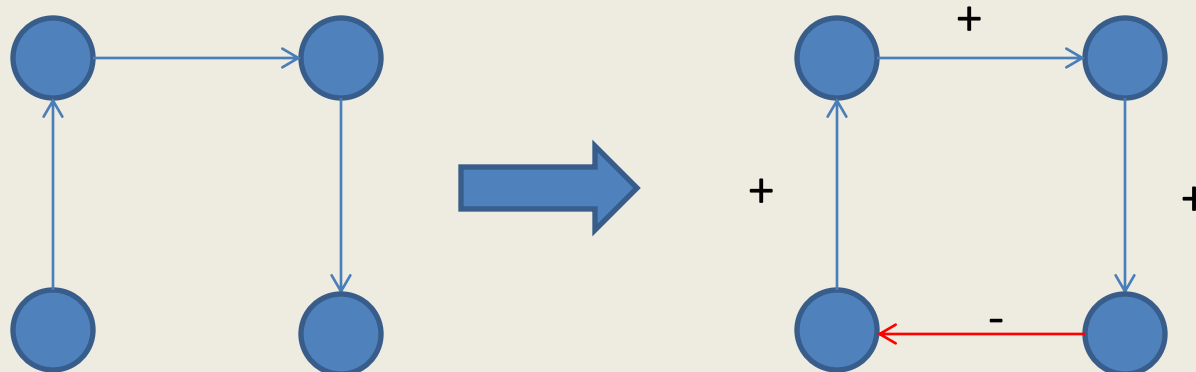
## Task 2: Can we predict Trust better with Distrust

---

- If distrust is a new dimension of trust, distrust should provide additional information about users, and could have added value beyond trust
- We seek answer to whether using both trust and distrust information can help achieve better performance than using only trust information
- Task 2 is to incorporate distrust into trust measurements

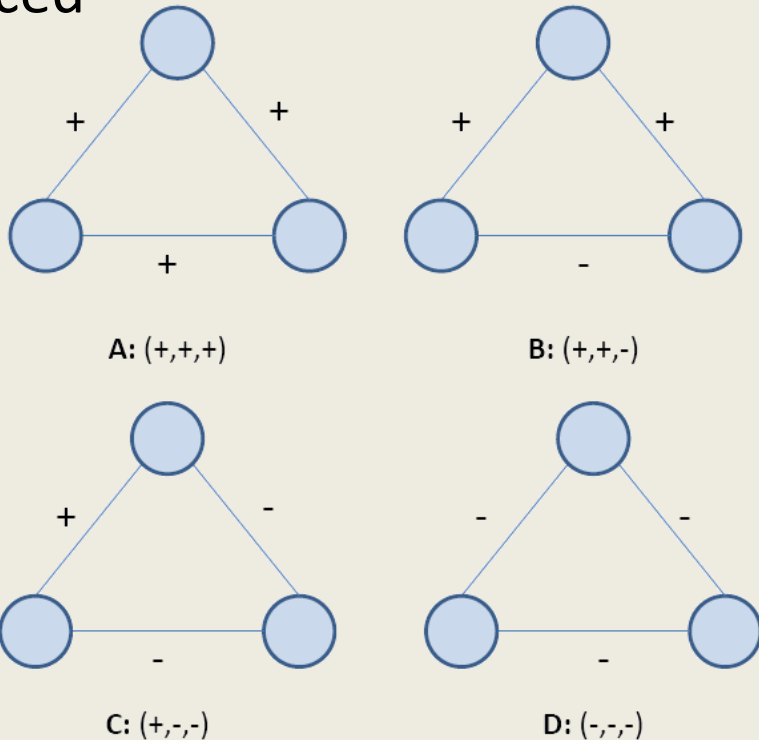
# Distrust in Trust Metrics

- Most trust and distrust metrics are based on the model by extending negative values to trust models to incorporate distrust
- The introduction of distrust in trust networks converts unsigned trust networks to signed trust and distrust networks
  - Social theories for signed network such as balance theory and status theory can be used to understand trust and distrust



# Balance Theory [ Heider, 1946]

- Balance theory suggests that “the friend of my friend is my friend” and “the enemy of my enemy is my friend”
- For a triad, there are four possible sign combinations A(+,+,+), B(+,+,-) C(+,-,-) and D(-,-,-), but only A(+,+,+) and C(+,-,-) are balanced



Balance theory is developed for undirected networks and can be applied to directed networks by ignoring their directions.

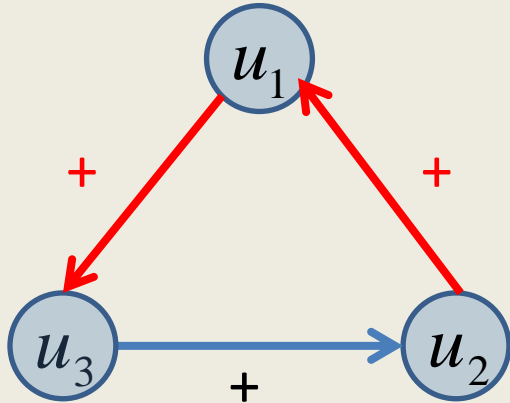
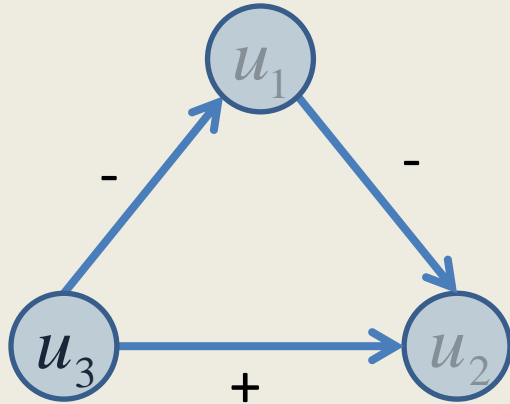
# Status Theory [Leskovec et al., 2010a]

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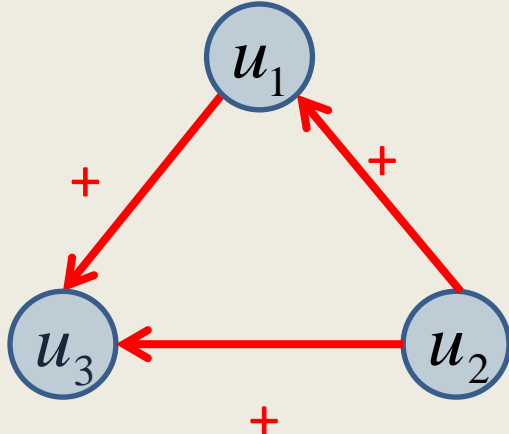
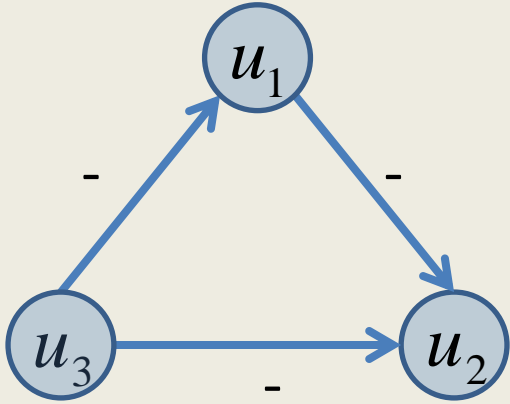
- Status theory is developed for directed networks
- A positive link from  $u$  to  $v$  indicates that  $u$  has a higher status than  $v$
- A negative link from  $u$  to  $v$  indicates that  $u$  has a lower status than  $v$
- For a triad, status theory suggests that if we take each negative relation, reverse its direction, and flip its sign to positive, then the resulting triangle (with all positive edge signs) should be acyclic



# Status theory



Cyclic,  
invalid



Acyclic,  
valid

# Trust and Distrust Propagation [Guha et al., 2004]

- A single step of distrust propagation in trust propagation

Trust propagation: 
$$\mathbf{C} = \alpha_1 \mathbf{T} + \alpha_2 \mathbf{T}^\top \mathbf{T} + \alpha_3 \mathbf{T}^\top + \alpha_4 \mathbf{T} \mathbf{T}^\top$$

One step distrust propagation: 
$$\tilde{\mathbf{G}} = \sum_{k=1}^K \gamma^k \mathbf{C}^k (\mathbf{T} - \mathbf{D})$$

- Multiple steps of distrust propagation in trust propagation

Trust and distrust propagation: 
$$\mathbf{E} = \alpha_1 \mathbf{F} + \alpha_2 \mathbf{F}^\top \mathbf{F} + \alpha_3 \mathbf{F}^\top + \alpha_4 \mathbf{F} \mathbf{F}^\top$$

Propagation aggregation: 
$$\tilde{\mathbf{G}} = \sum_{k=1}^K \gamma^k \mathbf{E}^k$$

# Trust and Distrust Matrix Factorization [Tang and Liu, 2014]

- For each user  $u_i$ , we introduce one dimensional latent variable  $r_i$ , and then  $F_{ij}$  is modeled as  $F_{ij} = r_i r_j$  to capture balance theory
  - Distrust relations are represented by negative values in  $\mathbf{F} = \mathbf{T}-\mathbf{D}$
- With modeling balance theory, trust and distrust matrix factorization disMF models  $F_{ij}$  as

$$F_{ij} = U_i V U_j^T + \lambda r_i r_j$$

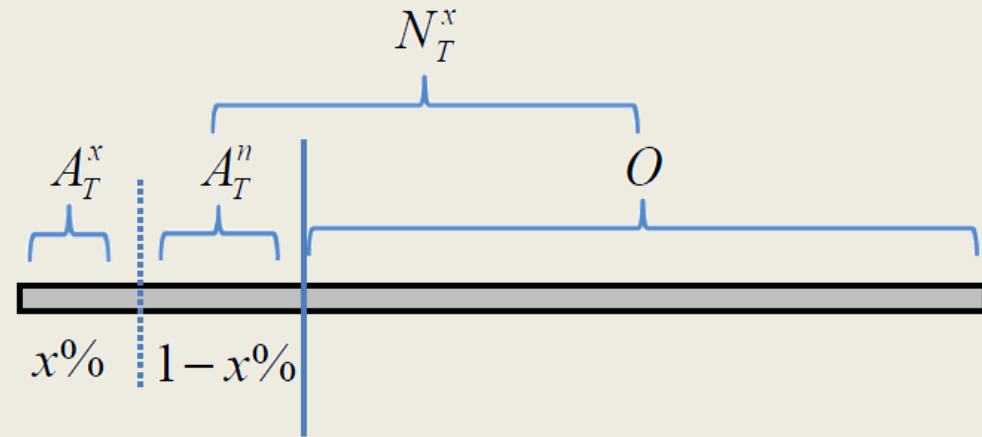
$U_i V U_j^T$  models correlation between user preferences

$r_i r_j$  models balance theory

$\lambda$  controls contributions from balance theory

# Experimental Settings for Task 2

- Each time we choose  $x\%$  of pairs of users with trust relations  $A_T^x$  as old trust relations and the remaining as new trust relations  $A_T^n$



- Through Task 2 with  $A_T^x$  and  $D$ , we predict  $|A_T^n|$  pairs of users  $P$  from  $N_T^x$  as trust
- $D$  is the set of pairs with distrust as ground truth in the data set

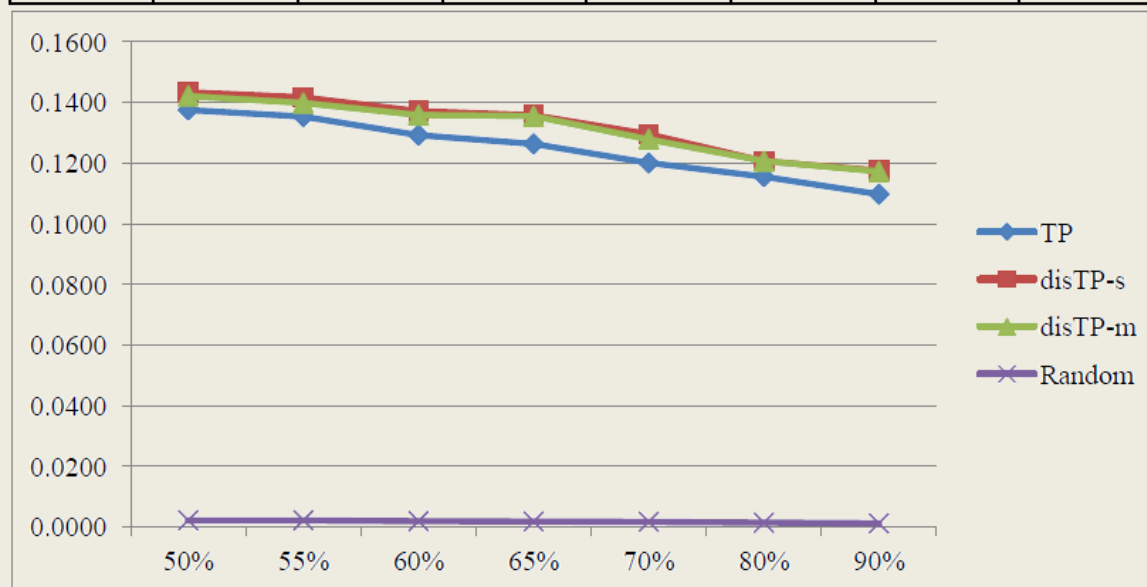
- The performance is computed as

$$PA = \frac{|A_T^n \cap P|}{|A_T^n|}$$

# Evaluation of Trust and Distrust Propagation

- Incorporating distrust propagation into trust propagation can improve the performance of trust measurement
- One step distrust propagation usually outperforms multiple step distrust propagation

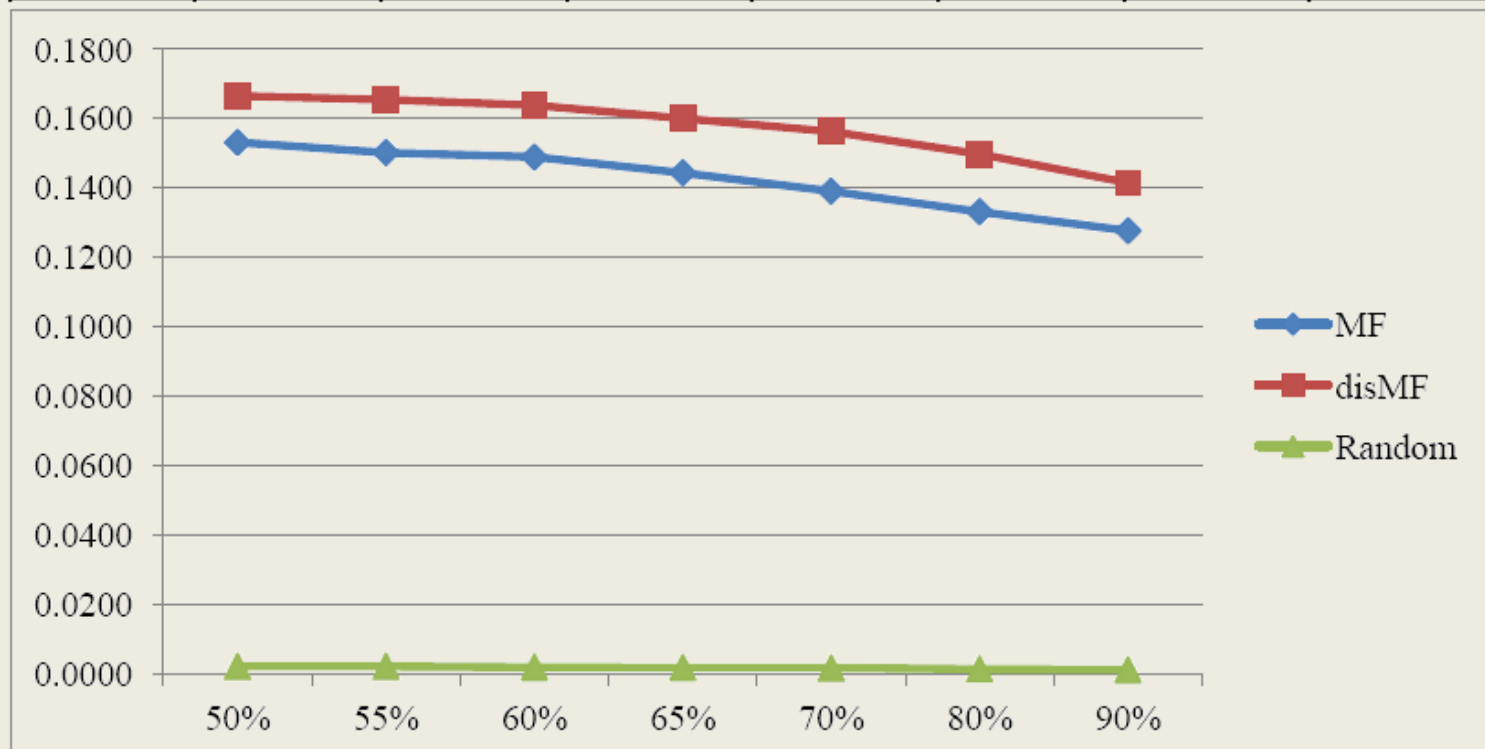
	50%	55%	60%	65%	70%	80%	90%
TP	<b>0.1376</b>	0.1354	0.1293	0.1264	0.1201	0.1156	0.1098
disTP-s	<b>0.1435</b>	0.1418	0.1372	0.1359	0.1296	0.1207	0.1176
disTP-m	<b>0.1422</b>	0.1398	0.1359	0.1355	0.1279	0.1207	0.1173
Random	<b>0.0023</b>	0.0023	0.0020	0.0019	0.0018	0.0015	0.0013



# Evaluation of Trust and Distrust Matrix Factorization

- Incorporating distrust with balance theory can significantly improve the performance of trust prediction

	50%	55%	60%	65%	70%	80%	90%
MF	<b>0.1531</b>	0.1502	0.1489	0.1444	0.1391	0.1332	0.1277
disMF	<b>0.1665</b>	0.1654	0.1639	0.1601	0.1563	0.1498	0.1415
Random	<b>0.0023</b>	0.0023	0.0020	0.0019	0.0018	0.0015	0.0013



# Findings from Task 1 and Task 2

---

- Task 1 shows that distrust is not the negation of trust
  - Low trust is not equivalent to distrust
  - Distrust is not the negation of trust
- Task 2 shows that the performance of trust prediction is improved by incorporating distrust
  - Distrust has added value in addition to trust
  - Incorporating distrust can improve trust computation

# Distrust in Trust-aware Recommender Systems

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- Genuine distrust information tends to be more noticeable and credible, and weighed more in decision making than trust information of a similar magnitude
- Users might or might not accept recommendations from their trusted users, but will certainly exclude recommendations from their distrusted users



# Distrust in Memory-based Trust-aware Systems [Victor et al., 2009]

- Distrust as a filter

- Use distrust to filter out “unwanted” users in the recommendation processes

$$\hat{r}_{u,i} = \bar{r}_u + \frac{\sum_{v \notin \mathcal{D}} (r_{v,i} - \bar{r}_v) \times t_{u,v}}{\sum t_{u,v}}$$

- Distrust as a dissimilarity measure

- Consider distrust scores as negative weights

$$\hat{r}_{u,i} = \bar{r}_u + \frac{\sum_{v \notin \mathcal{D}} (r_{v,i} - \bar{r}_v) \times t_{u,v}}{\sum t_{u,v}} - \frac{\sum_{v \in \mathcal{D}} (r_{v,i} - \bar{r}_v) \times d_{u,v}}{\sum d_{u,v}}$$

# Distrust in Model-based Trust-aware systems

[Ma et al., 2009]

- Users with distrust relations should have very different user preferences

$$\max \sum_i \sum_{u_k \in D(u_i)} D_{ik} \| U_i - U_k \|$$

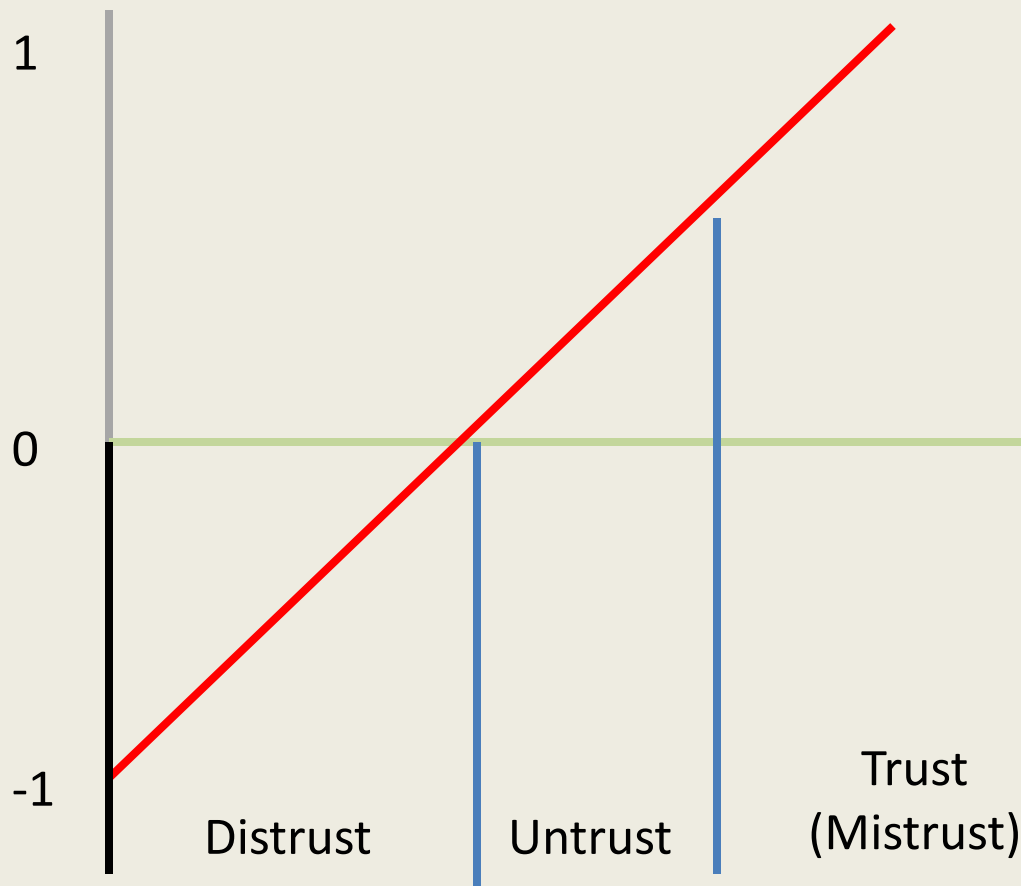
- Distrust is considered a dissimilarity measure
- Forcing users preference of two users with a distrust relation far away from each other

# Mistrust, Untrust, and Distrust [Marsh and Dibben, 2005]

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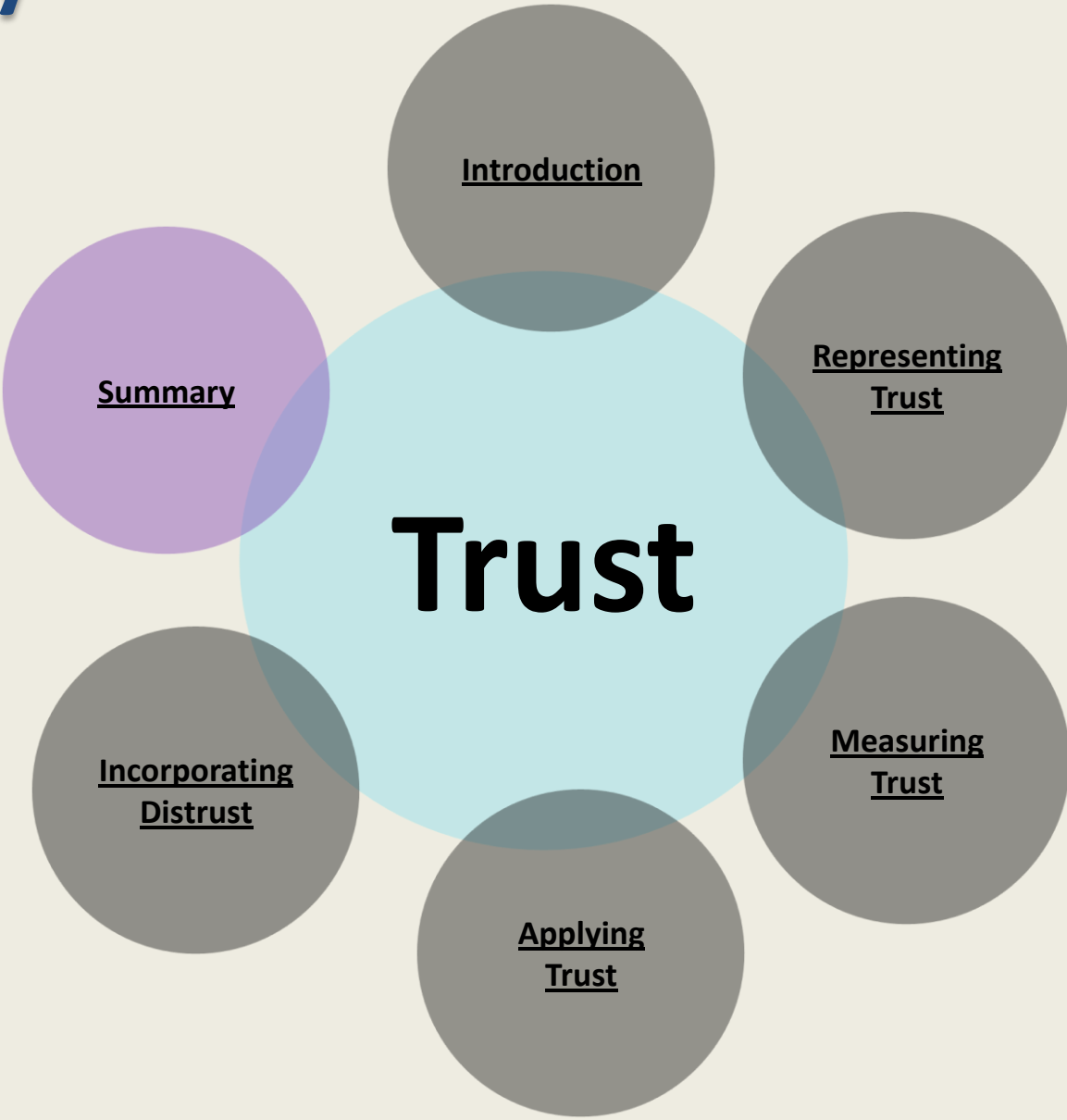
- Mistrust is misplaced trust
  - A trustee betrays the trust of the trustor
- Untrust is a measure of how little the trustee is actually trusted
  - The trustor has little confidence in the trustee
- Distrust is a measure of how much the trustor believes that the trustee will actively work against them in a given situation

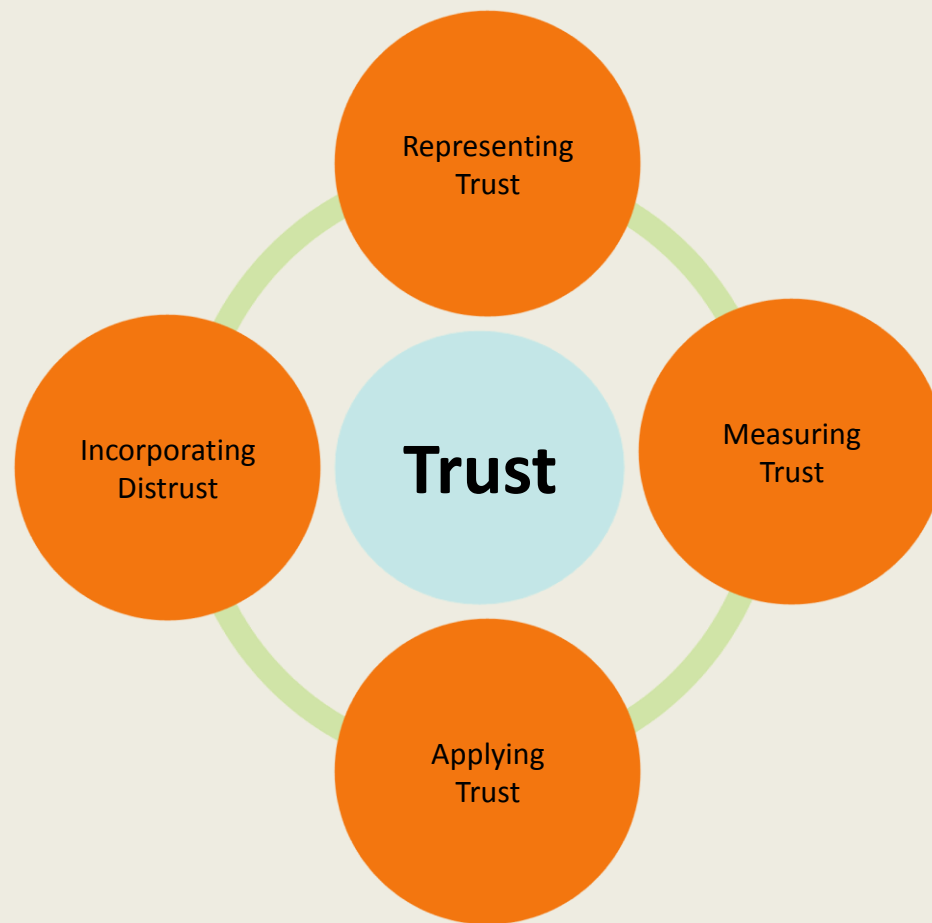
# Illustration of Mistrust, Untrust, and Distrust [Marsh and Dibben, 2005]

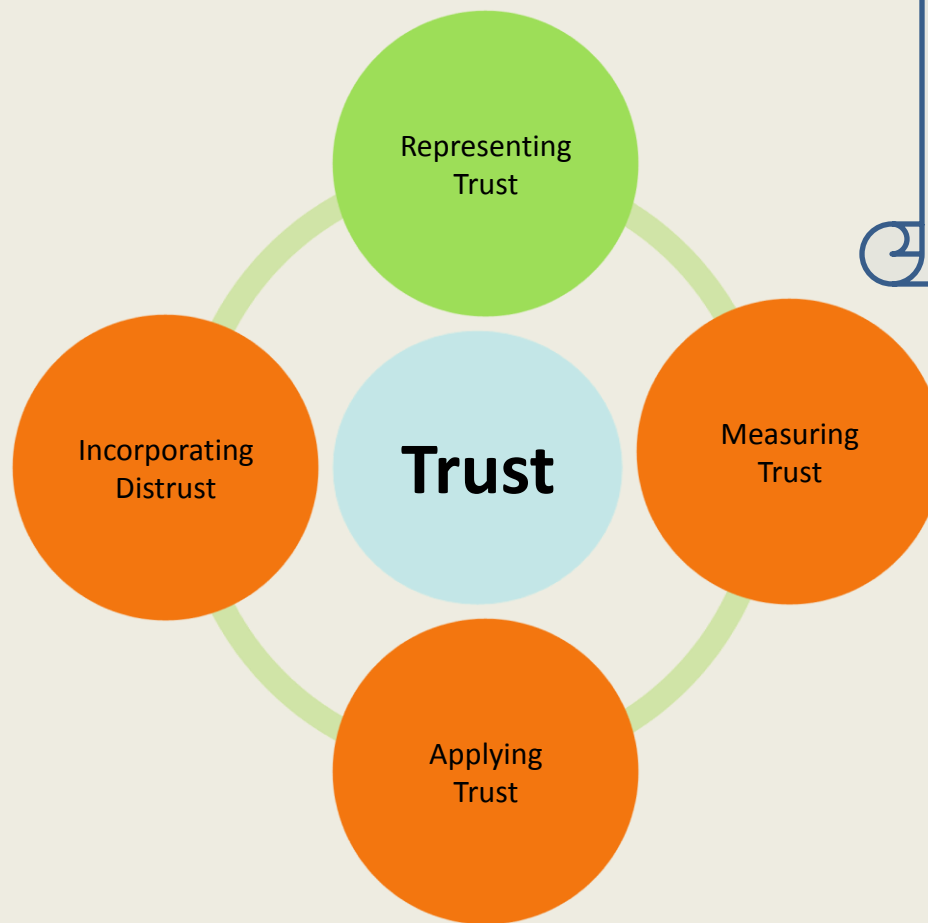


- Untrust is still a positive measurement
- While distrust is a negative measurement

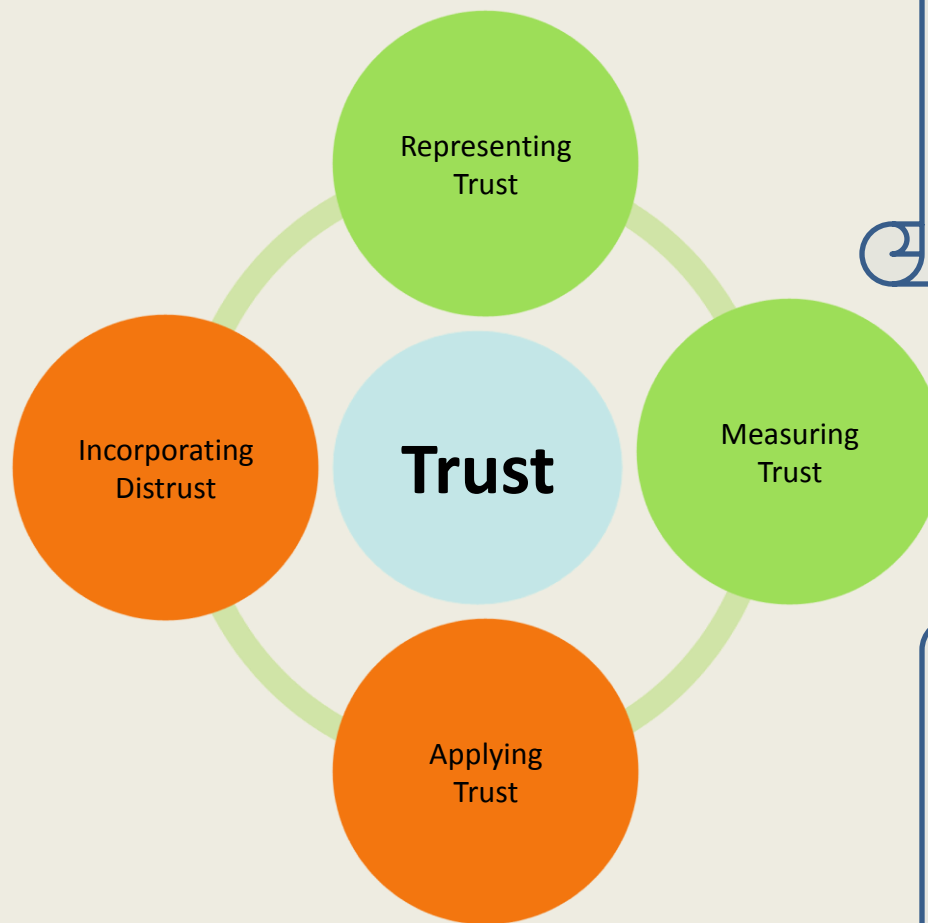
# Summary







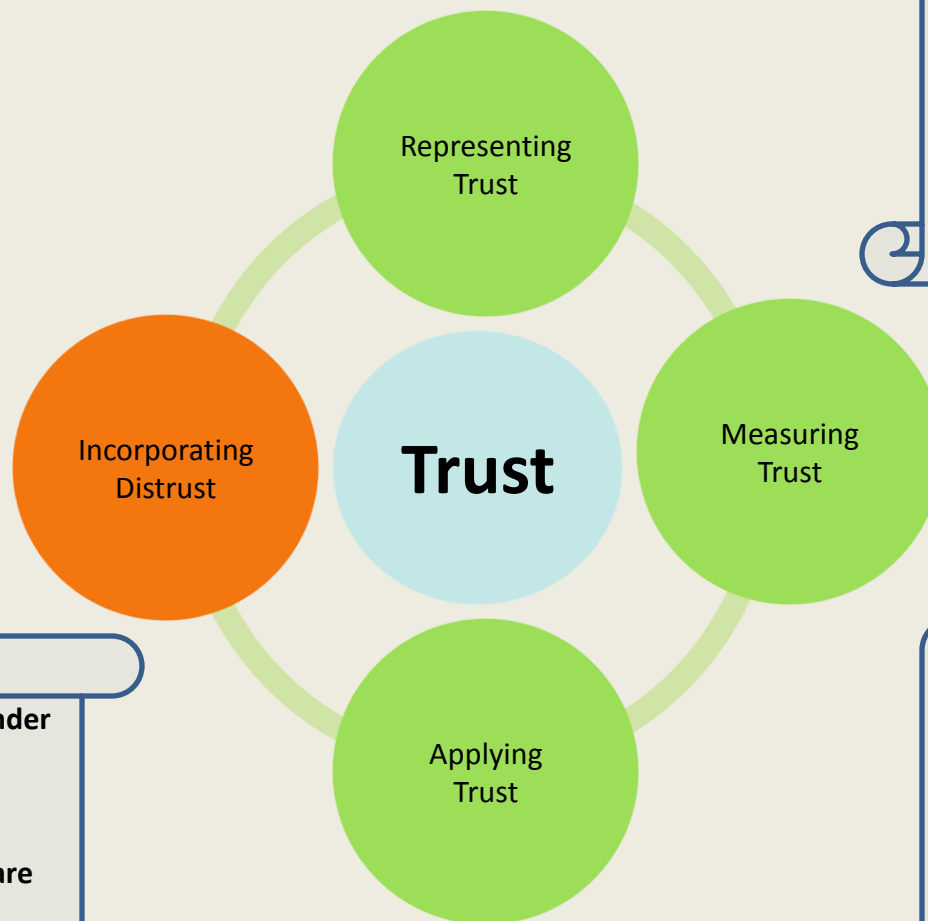
- Properties of Trust
- Classifications of Trust Representations
- Probabilistic vs Gradual Trust Representations
- Single vs Multi-dimensional Trust Representations
- Trust vs Trust and Distrust Representations



- Properties of Trust
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- Probabilistic vs Gradual Trust Representations
- Single vs Multi-dimensional Trust Representations
- Trust vs Trust and Distrust Representations

- Classifications of Trust Metrics
- Global and Local Trust Metrics
- Supervised and Unsupervised Trust Metrics
- Binary and Continuous Trust Metrics
- Evaluation





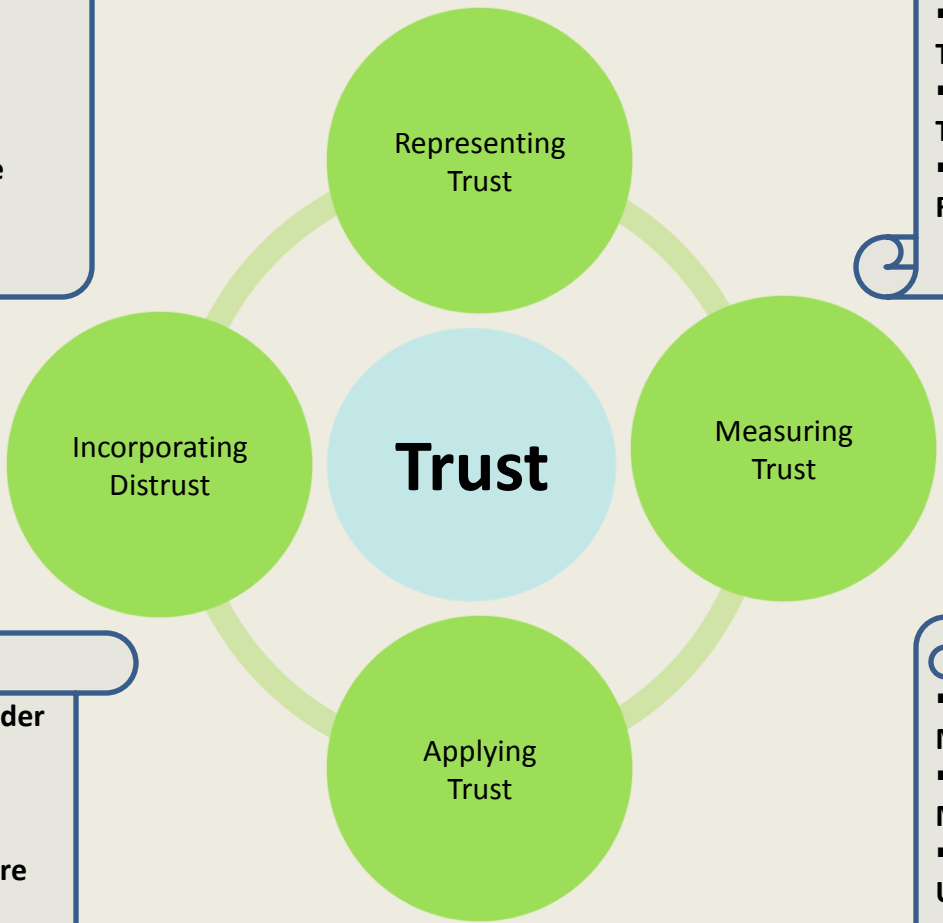
- Properties of Trust
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- Probabilistic vs Gradual Trust Representations
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- Trust-aware Recommender Systems
- Opportunities and Challenges
- Model-based Trust-aware Recommender Systems
- Memory-based Trust-aware Recommender Systems
- Evaluation

- Classifications of Trust Metrics
- Global and Local Trust Metrics
- Supervised and Unsupervised Trust Metrics
- Binary and Continuous Trust Metrics
- Evaluation

- Trust in Social Sciences
- Computational Understanding of Distrust
- Distrust in Trust Representations
- Distrust in Trust Measurements
- Distrust in Trust-aware Recommender Systems

- Properties of Trust
- Classifications of Trust Representations
- Probabilistic vs Gradual Trust Representations
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- Trust-aware Recommender Systems
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# Research Directions in Measuring Trust

- Solving data sparsity problem in trust measurements
  - Power-law-like distributions suggest that most of users only have few trust relations
  - Most of existing algorithms might fail for users with few trust relations
  - Integrating multiple sources such as item and helpfulness ratings in Epinions might help
  - Incorporating social theories such as homophily and influence
- Measuring trust when trust is not explicitly available
  - There are no explicit trust relations in some social media websites such as Twitter
  - Large amounts of user generated content and user interactions are available
  - Can we measure implicit trust with available data?

# Research Directions in Trust-aware Recommendation

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- Capturing multi-faceted trust and trust evolution
  - Trust relations under different contexts may differ
  - Trust relations may change over time
- Incorporating cross-media data
  - Trust relations on one site are often sparse and incomplete
  - Integrating data from multiple sites may provide a comprehensive and complete view about users
- Exploiting weak trust relations
  - Weak tie theory suggests that it is more often that novel information flows through weak rather than strong ties

# Research Directions in Incorporating Distrust

- Predicting distrust with publicly available data
  - Trust is a desired property while distrust is an unwanted one for most social networking sites or services
  - Various online services implement trust mechanisms
  - Few of them allow online users to specify distrust relations
  - Distrust relations are usually not available publicly
  - Interaction data is, however, pervasively available, which might indicate distrust relations
- Exploiting distrust in trust applications
  - Using distrust for recommendation is still an open problem
  - Effects of distrust in information propagation
  - Distrust in content filtering
  - Distrust in e-commerce

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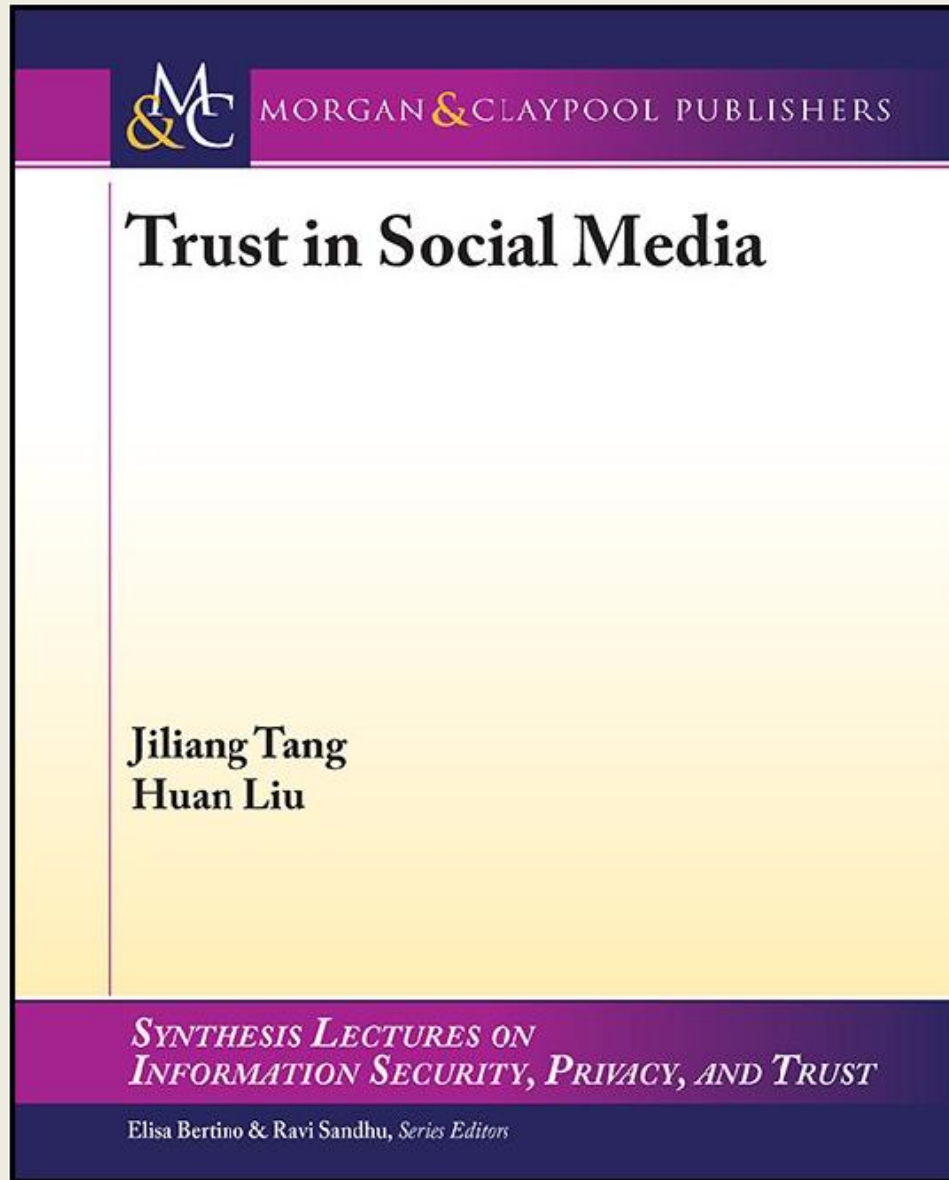
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# A book based on this tutorial



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