## Searching with Numbers

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## Motivation

- A large fraction of useful web consists of specification documents
- Current search technology is inadequate for retrieving speciffeation documents


## Specfication Documents

- Consist of <attribute name, value> pairs embedded in text
- Examples:
- Data sheets for electronic parts
- classified Ads
$>$ product catalogs


## Sources of Problems

- Synonyms for attribute names and units. - "lb" and "pounds", but no "lbs" or "pound".
- Attribute names are often missing.
$>$ No "Speed", just "MHz Pentium III"
- No "Memory", just "MB SDRAM"
- Accurate data extraction is hard, e.g. partial datasheet for Cypress CY7C225A PROM:

> - High Speed
> - 18 ns address set-up
> - 12 ns clock to output
> - Low Power
> - 495 mW (commercial)
> - 660 mW (military)

## An end run!

- Use a simple regular expression extractor to get numbers
- Do simple data extraction to get hints, e.g. $>$ Hint for unit: the word following the number. - Hint for attribute name: $k$ following numbers.

$$
256 \text { MB SDRAM memory }
$$

Unit Hint: MB

Attribute Hint: SDRAM, Memory

- Use only numbers in the queries
- Treat any attribute name in the query also as hint


## Documents and Queries

Document $\mathrm{D}=\left\{\left\langle\mathrm{n}_{\mathrm{i}}, \mathrm{H}_{\mathrm{i}}\right\rangle \mid \mathrm{n}_{\mathrm{i}} \in \mathrm{N}, \mathrm{H}_{\mathrm{i}} \in \mathrm{A}, 1 \leq \mathrm{i} \leq \mathrm{m}\right\}$
Query $\mathrm{Q}=\left\{\left\langle\mathrm{q}_{\mathrm{i}}, \mathrm{A}_{\mathrm{i}}\right\rangle \mid \mathrm{n}_{\mathrm{i}} \in \mathrm{N}, \mathrm{A}_{\mathrm{i}} \in \mathrm{A}, 1 \leq \mathrm{i} \leq \mathrm{k}\right\}$
$H_{i}$ and $A_{i}$ are hints
$D=\{\langle 256,\{\mathrm{MB}$, SDRAM, Memory $\}\rangle,\langle 700,\{\langle\mathrm{MHz}, \mathrm{CPU}\rangle\}\}$ $\mathrm{Q}=\langle 200 \mathrm{MB}, 750 \mathrm{MHz}\rangle$

Document $\mathrm{D}=\left\{\mathrm{n}_{\mathrm{i}} \mid \mathrm{n}_{\mathrm{i}} \in \mathrm{N}, 1 \leq \mathrm{i} \leq \mathrm{m}\right\}$ Query $\mathrm{Q}=\left\{\mathrm{q}_{\mathrm{i}} \mid \mathrm{n}_{\mathrm{i}} \in \mathrm{N}, 1 \leq \mathrm{i} \leq \mathrm{k}\right\}$
No hints with Documents and Queries $\mathrm{D}=\{256,700\} \quad \mathrm{Q}=\{200,750\}$

## Can it work?

- Yes!!!!!
- Provided data is non-reflective
- Reflectivity can be computed a priori for a given data set and provides estimate of exprected accuracy.


# Sesirch thgines 'rest Numbers as Strings 

- Search for 6798.32
- Lunar Nutation Cycle
- Returns 2 pages on Goggle
- However, search for 6798.320 yielded no page on Google (and all other search engines)


## Refilectivity

Non-reflective

$$
\langle\mathrm{x}=\mathrm{i}, \mathrm{y}=\mathrm{j}\rangle=>\nexists\langle\mathrm{x}=\mathrm{j}, \mathrm{y}=\mathrm{i}\rangle
$$




Low Reflectivity



Hiah Reflectivity

## Non-reflectivity in real life

- Non-overlapping attributes:
- Memory: 64-512 MIb, Disk: 10-40 Gb
- Correlations:
-Memory: 64-512 Mlb, Disk: 10 - 100 Gb still fine.
- Clusters


## Reflectivity

-D : set of m-dimensional points $n^{i}$ : coordinates of point $x^{i}$ $\bar{\theta}\left(n^{i}\right)$ : number of points within distance $r$ of $n^{i}$

- Reflections(x'): permutations of $n^{i}$ $\rho\left(\mathrm{n}^{\mathrm{i}}\right)$ : number of points in $D$ that have at least one reflection within distance $r$ of $\underline{n}^{i}$
- Reflectivity $(\mathbf{m}, \mathbf{r})=1-1 /|D| \Sigma_{\text {weo }} \theta\left(\underline{n}^{i}\right) / \rho\left(\underline{n}^{i}\right)$
- See the paper for reflectivity of $D$ over $k$ k-dimensional subspaces
- Non-reflectivity = 1-Reflectivity


## Basic Idea

- Consider co-ordinates of a point
- If there is no data point at the permutations of its co-ordinates, this point is non-reflective
- Only a few data points at the permutations of its co-ordinates => point is largely non-refiective
- Compute refilectivity as this ratio summed over all the points
- Consider neighborhood of a point in the above calculation


## Algorithms

- How to compute match score (rank) of a document for a given query?
- How to limit the number of documents for which the match score is computed?


## Match Score of a Document

- Select $k$ numbers from $D$ yielding minimum distance between $Q$ and $D$ :
$-F(Q, D)=\left(\sum_{i=1}^{k} W\left(q_{i}, n_{i}\right)^{D}\right)^{1 / p}$
- Map problem to Bipartite Matching in graph G:
- $k$ source nodes: corresponding to query numbers
- $m$ target nodes: corresponding to document numbers
- An edge from each source to $k$ nearest targets. Assign weight $w\left(q_{i}, n_{j}\right)^{\nu}$ to the edge $\left(q_{i}, n_{j}\right)$.


## Bipartite Matching

- The optimum solution to the minimum weight bipartite graph matching problem matches each number in $Q$ with a distinct number in $D$ such that the distance score $\mathrm{F}(\mathrm{O}, \mathrm{D})$ is minimized.
- The minimum score gives the rank of the document D for the Query Q.
- Assuming F to be $L_{1}$ and $w\left(q_{i}, n_{j}\right):=\left|q_{i}-n_{i}\right| /\left|q_{i}+\varepsilon\right|$ : Doc:

Query:


## Limiting the Set of Documents

Similar to the score aggregation problem [Dagin, PODS 96]

- Proposed algorithm is an adaptation of the TA algorithm in [Fagin-Lotem-Naor, PODS 01]


## Limiting the Set of Documents



| 25/.25 | D5 | D7 | D9 |
| :---: | :---: | :---: | :---: |
| 10\%.5 | D3 |  |  |
| 35/.75 | D6 | D8 |  |

- Make k conceptual sorted lists, one for each query term [use: documents = index(number)]
- Do a round robin access to the lists. For each document found, compute its distance $\mathrm{F}(\mathrm{D}, \mathrm{Q})$
- Let $n_{i}:=$ number last looked at for query term $q_{i}$ Let $\tau:=\left(\sum_{i=1}^{k} \mathrm{w}\left(\mathrm{q}_{\mathrm{i}}, \mathrm{n}_{\mathrm{i}}\right)^{\mathrm{p}}\right)^{1 / \mathrm{p}}$
- Halt when t documents found whose distance $\leq \tau$
$\nabla \tau$ is lowerbound on distance of unseen documents


## Evalugtion MIetric

$\Delta$ Benchmark: Set of answers when attribute names are precisely known in the document and query

- What fraction of the top 10 "true" answers are present in the top 10 answers when attribute names are unknown in both document and query?


## Accuracy Results



## Refilectivity estimates accuracy

- Non-reflectivity closely tracked accuracy for all nine data sets
- Non-reflectivity arises due to clustering and
correlations in real data (Randomised non-reflectivity: value obtained after permuting values in the columns)


Accuracy
-- Non-Reflectivity
—— Randomized Non-Reflectivity

## Incorporating Flints

$\Delta L_{I}=\sum w\left(q_{i}, n_{i}\right)+B v\left(A_{i}, H_{i}\right)$
$>\nu\left(A_{i}, H_{i}\right):$ distance between attribute name (or unit) for $q_{i}$ and set of hints for $n_{i}$
$>$ B: relative importance of number match vs. name/unit match

## Balance between Number Match of Hint Match

- Weightage to hints should depend on the accuracy of hints
- Use tune set to determine B on per dataset basis



## Efifectiveness of Hints

- Improvement in accuracy depends on how good are hints



## Iffectiveness of Indexing

- 1 million docs:
-1 sec for qsive $=5$
-.03 sec for qsize=1



## Summary

- Allows querying using only numbers or numbers + hints.
- Data can come from raw text (e.g. product descriptions) or databases.
- End run around data extraction. - Use simple extractor to generate hints.
- Can ascertain apriori when the technique will be effiective

Future Work

- Integration with classic IR (key word search)
$>$ PROM speed 20 ns power 500 mW
- Extension to non-numeric values

